

PC Assembly Language

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Preface

Purpose

The purpose of this book is to give the reader a better understanding of how computers really work at a lower level than in programming languages like Pascal. By gaining a deeper understanding of how computers work, the reader can often be much more productive developing software in higher level languages such as C and C++. Learning to program in assembly language is an excellent way to achieve this goal. Other PC assembly language books still teach how to program the 8086 processor that the original PC used in 1980! This book instead discusses how to program the 80386 and later processors in protected mode (the mode that Windows runs in). There are several reasons to do this:

1. It is easier to program in protected mode than in the 8086 real mode that other books use.
2. All modern PC operating systems run in protected mode.
3. There is free software available that runs in this mode.

The lack of textbooks for protected mode PC assembly programming is the main reason that the author wrote this book.

As alluded to above, this text makes use of Free/Open Source software: namely, the NASM assembler and the DJGPP C/C++ compiler. Both of these are available to download off the Internet. The text also discusses how to use NASM assembly code under the Linux operating system and with Borland's and Microsoft's C/C++ compilers under Windows.

Be aware that this text does not attempt to cover every aspect of assembly programming. The author has tried to cover the most important topics that *all* programmers should be acquainted with.

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Resources on the Internet

Author’s page	http://www.drpaulcarter.com/
NASM	http://nasm.2y.net/
DJGPP	http://www.delorie.com/djgpp
USENET	comp.lang.asm.x86

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Chapter 1

Introduction

1.1 Number Systems

Memory in a computer consists of numbers. Computer memory does not store these numbers in decimal (base 10). Because it greatly simplifies the hardware, computers store all information in a binary (base 2) format. First let's review the decimal system.

1.1.1 Decimal

Base 10 numbers are composed of 10 possible digits (0-9). Each digit of a number has a power of 10 associated with it based on its position in the number. For example:

$$234 = 2 \times 10^2 + 3 \times 10^1 + 4 \times 10^0$$

1.1.2 Binary

Base 2 numbers are composed of 2 possible digits (0 and 1). Each digit of a number has a power of 2 associated with it based on its position in the number. (A single binary digit is called a bit.) For example:

$$\begin{aligned} 11001_2 &= 1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 \\ &= 16 + 8 + 1 \\ &= 25 \end{aligned}$$

This shows how binary may be converted to decimal. Table 1.1 shows how the first few binary numbers are converted.

Figure 1.1 shows how individual binary digits (*i.e.*, bits) are added. Here's an example:

Decimal	Binary		Decimal	Binary
0	0000		8	1000
1	0001		9	1001
2	0010		10	1010
3	0011		11	1011
4	0100		12	1100
5	0101		13	1101
6	0110		14	1110
7	0111		15	1111

Table 1.1: Decimal 0 to 15 in Binary

No previous carry				Previous carry			
0	0	1	1	0	0	1	1
+0	+1	+0	+1	+0	+1	+0	+1
0	1	1	0	1	0	0	1
			c		c	c	c

Figure 1.1: Binary addition (*c* stands for *carry*)

$$\begin{array}{r}
 11011_2 \\
 +10001_2 \\
 \hline
 101100_2
 \end{array}$$

Consider the following binary division:

$$1101_2 \div 10_2 = 110_2 r 1$$

This shows that dividing by two in binary shifts all the bits to the right by one position and moves the original rightmost bit into the remainder. (Analogously, dividing by ten in decimal shifts all the decimal digits to the right by one and moves the original rightmost digit into the remainder.) This fact can be used to convert a decimal number to its equivalent binary representation as Figure 1.2 shows. This method finds the rightmost digit first, this digit is called the *least significant bit* (lsb). The leftmost digit is called the *most significant bit* (msb). The basic unit of memory consists of 8 bits and is called a *byte*.

1.1.3 Hexadecimal

Hexadecimal numbers use base 16. Hexadecimal (or *hex* for short) can be used as a shorthand for binary numbers. Hex has 16 possible digits. This

Decimal	Binary
$25 \div 2 = 12 r 1$	$11001 \div 10 = 1100 r 1$
$12 \div 2 = 6 r 0$	$1100 \div 10 = 110 r 0$
$6 \div 2 = 3 r 0$	$110 \div 10 = 11 r 0$
$3 \div 2 = 1 r 1$	$11 \div 10 = 1 r 1$
$1 \div 2 = 0 r 1$	$1 \div 10 = 0 r 1$

Figure 1.2: Decimal conversion

$589 \div 16 = 36 r 13$
$36 \div 16 = 2 r 4$
$2 \div 16 = 0 r 2$

Figure 1.3:

creates a problem since there are no symbols to use for these extra digits after 9. By convention, letters are used for these extra digits. The 16 hex digits are 0-9 then A, B, C, D, E and F. The digit A is equivalent to 10 in decimal, B is 11, etc. Each digit in a hex number has a power of 16 associated with it. Example:

$$\begin{aligned}
 2BD_{16} &= 2 \times 16^2 + 11 \times 16^1 + 13 \times 16^0 \\
 &= 512 + 176 + 13 \\
 &= 701
 \end{aligned}$$

To convert from decimal to hex, use the same idea that was used for binary conversion except divide by 16. See Figure 1.3 for an example.

Thus, $589 = 24D_{16}$. The reason that hex is useful is that there is a very simple way to convert between hex and binary. Binary numbers get large and cumbersome quickly. Hex provides a much more compact way to represent binary.

To convert a hex number to binary, simply convert each hex digit to a 4-bit binary number. For example, $24D_{16}$ is converted to $0010\ 0100\ 1101_2$. Note that the leading zero's of the 4-bits are important! Converting from

word	2 bytes
double word	4 bytes
quad word	8 bytes
paragraph	16 bytes

Table 1.2: Units of Memory

binary to hex is just as easy. Just do the reverse conversion. Convert each 4-bit segments of the binary to hex. Remember to start from the right end, not the left end of the binary number. Example:

$$\begin{array}{cccccc} 110 & 0000 & 0101 & 1010 & 0111 & 1110_2 \\ 6 & 0 & 5 & A & 7 & E_{16} \end{array}$$

A 4-bit number is called a *nibble*. Thus each hex digit corresponds to a nibble. Two nibbles make a byte and so a byte can be represented by a 2-digit hex number. A byte's value ranges from 0 to 11111111 in binary, 0 to FF in hex and 0 to 255 in decimal.

1.2 Computer Organization

1.2.1 Memory

The basic unit of memory is a byte. A computer with 32 Meg of RAM can hold roughly 32 million bytes of information. Each byte in memory is labeled by an unique number know as its address as Figure 1.4 shows.

Address	0	1	2	3	4	5	6	7
Memory	2A	45	B8	20	8F	CD	12	2E

Figure 1.4: Memory Addresses

All data in memory is numeric. Characters are stored by using a *character code*. The PC uses the most common character code known as *ASCII* (American Standard Code for Information Interchange). Often memory is used in larger chunks than single bytes. Names have been given to these larger sections of memory as Table 1.2 shows.

1.2.2 The CPU

The Central Processing Unit (CPU) is the hardware that directs the execution of instructions. The instructions that CPU's perform are generally

very simple. Instructions may require the data they act on to be in special storage locations in the CPU itself called *registers*. The CPU can access data in registers much faster than data in RAM memory. However, the number of registers in a CPU is limited, so the programmer must take care to keep only currently used data in registers.

The instructions a type of CPU executes make up the CPU's *machine language*. Machine programs have a much more basic structure than higher-level languages. Machine language instructions are encoded as raw numbers, not in friendly text formats. A CPU must be able to decode an instruction's purpose very quickly to run efficiently. Machine language is designed with this goal in mind, not to be easily deciphered by humans. Programs written in other languages must be converted to the native machine language of the CPU to run on the computer. A *compiler* is a program that translates programs written in a programming language into the machine language of a particular computer architecture. In general, every type of CPU has its own unique machine language. This is one reason why programs written for a Mac can not run on an IBM-type PC.

1.2.3 The 80x86 family of CPUs

IBM-type PC's contain a CPU from Intel's 80x86 family (or a clone of one). The CPU's in this family all have some common features including a base machine language. However, the more recent members greatly enhance the features.

8088,8086: These CPU's from the programming standpoint are identical. They were the CPU's used in the earliest PC's. They provide several 16-bit registers: AX, BX, CX, DX, SI, DI, BP, SP, CS, DS, SS, ES, IP, FLAGS. They only support up to one megabyte of memory and only operate in *real mode*. In this mode, a program may access any memory address, even the memory of other programs! This makes debugging and security very difficult! Also, program memory has to be divided into *segments*. Each segment can not be larger than 64K.

80286: This CPU was used in AT class PC's. It adds some new instructions to the base machine language of the 8088/86. However, it's main new feature is *16-bit protected mode*. In this mode, it can access up to 16 megabytes and protect programs from accessing each other's memory. However, programs are still divided into segments that could not be bigger than 64K.

80386: This CPU greatly enhanced the 80286. First, it extends many of the registers to hold 32-bits (EAX, EBX, ECX, EDX, ESI, EDI, EBP, ESP, EIP) and adds two new 16-bit registers FS and GS. It also adds

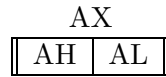


Figure 1.5: The AX register

a new *32-bit protected mode*. In this mode, it can access up to 4 gigabytes. Programs are again divided into segments, but now each segment can also be up to 4 gigabytes in size!

80486/Pentium/Pentium Pro: These members of the 80x86 family add very few new features. They mainly speed up the execution of the instructions.

Pentium MMX: This processor adds the MMX (MultiMedia eXtensions) instructions to the Pentium. These instructions can speed up common graphics operations.

Pentium II: This is the Pentium Pro processor with the MMX instructions added. (The Pentium III is essentially just a faster Pentium II.)

1.2.4 8086 16-bit Registers

The original 8086 CPU provided four 16-bit general purpose registers: AX, BX, CX and DX. Each of these registers could be decomposed into two 8-bit registers. For example, the AX register could be decomposed into the AH and AL registers as Figure 1.5 shows. The AH register contains the upper (or high) 8 bits of AX and AL contains the lower 8 bits of AX. Often AH and AL are used as independent one byte registers; however, it is important to realize that they are not independent of AX. Changing AX's value will change AH and AL and *vis versa*. The general purpose registers are used in many of the data movement and arithmetic instructions.

There are two 16-bit index registers: SI and DI. They are often used as pointers, but can be used for many of the same purposes as the general registers. However, they can not be decomposed into 8-bit registers.

The 16-bit BP and SP registers are used to point to data in the machine language stack. These will be discussed later.

The 16-bit CS, DS, SS and ES registers are *segment registers*. They denote what memory is used for different parts of a program. CS stands for Code Segment, DS for Data Segment, SS for Stack Segment and ES for Extra Segment. ES is used as a temporary segment register. The details of these registers are in Sections 1.2.6 and 1.2.7.

The Instruction Pointer (IP) register is used with the CS register to keep track of the address of the next instruction to be executed by the

CPU. Normally, as an instruction is executed, IP is advanced to point to the next instruction in memory.

The FLAGS register stores important information about the results of a previous instruction. This results are stored as individual bits in the register. For example, the Z bit is 1 if the result of the previous instruction was zero or 0 if not zero. Not all instructions modify the bits in FLAGS, consult the table in the appendix to see how individual instructions affect the FLAGS register.

1.2.5 80386 32-bit registers

The 80386 and later processors have extended registers. For example, the 16-bit AX register is extended to be 32-bits. To be backward compatible, AX still refers to the 16-bit register and EAX is used to refer to the extended 32-bit register. AX is the lower 16-bits of EAX just as AL is the lower 8-bits of AX (and EAX). There is no way to access the upper 16-bits of EAX directly.

The segment registers are still 16-bit in the 80386. There are also two new segment registers: FS and GS. Their names do not stand for anything. They are extra temporary segment registers (like ES).

1.2.6 Real Mode

In real mode, memory is limited to only one megabyte (2^{20} bytes). Valid address range from (in hex) 00000 to FFFFF. These addresses require a 20-bit number. Obviously, a 20-bit number will not fit into any of the 8086's 16-bit registers. Intel solved this problem, by using two 16-bit values determine an address. The first 16-bit value is called the *selector*. Selector values must be stored in segment registers. The second 16-bit value is called the *offset*. The physical address referenced by a 32-bit *selector:offset* pair is computed by the formula

$$16 * \text{selector} + \text{offset}$$

Multiplying by 16 in hex is easy, just add a 0 to the right of the number. For example, the physical addresses referenced by 047C:0048 is given by:

$$\begin{array}{r} 047C0 \\ +0048 \\ \hline 04808 \end{array}$$

In effect, the selector value is a paragraph number (see Table 1.2).

Real segmented addresses have disadvantages:

So where did the infamous DOS 640K limit come from? The BIOS required some of the 1M for it's code and for hardware devices like the video screen.

- A single selector value can only reference 64K of memory (the upper limit of the 16-bit offset). What if a program has more than 64K of code? A single value in CS can not be used for the entire execution of the program. The program must be split up into sections (called *segments*) less than 64K in size. When execution moves from one segment to another, the value of CS must be changed. Similar problems occur with large amounts of data and the DS register. This can be very awkward!
- Each byte in memory does not have a unique segmented address. The physical address 04808 can be referenced by 047C:0048, 047D:0038, 047E:0028 or 047B:0058. This can complicate the comparison of segmented addresses.

1.2.7 16-bit Protected Mode

In the 80286's 16-bit protected mode, selector values are interpreted completely differently than in real mode. In real mode, a selector value is a paragraph number of physical memory. In protected mode, a selector value is an *index* into a *descriptor table*. In both modes, programs are divided into segments. In real mode, these segments are at fixed positions in physical memory and the selector value denotes the paragraph number of the beginning of the segment. In protected mode, the segments are not at fixed positions in physical memory. In fact, they do not have to be in memory at all!

Protected mode uses a technique called *virtual memory*. The basic idea of a virtual memory system is to only keep the data and code in memory that programs are currently using. Other data and code are stored temporarily on disk until they are needed again. In 16-bit protected mode, segments are moved between memory and disk as needed. When a segment is returned to memory from disk, it is very likely that it will be put into a different area of memory that it was in before being moved to disk. All of this is done transparently by the operating system. The program does not have to be written differently for virtual memory to work.

In protected mode, each segment is assigned an entry in a descriptor table. This entry has all the information that the system needs to know about the segment. This information includes: is it currently in memory; if in memory, where is it; access permissions (*e.g.*, read-only). The index of the entry of the segment is the selector value that is stored in segment registers.

One well-known PC columnist called the 286 CPU "brain dead."

One big disadvantage of 16-bit protected mode is that offsets are still 16-bit quantities. As a consequence of this, segment sizes are still limited to at most 64K. This makes the use of large arrays problematic!

1.2.8 32-bit Protected Mode

The 80386 introduced 32-bit protected mode. There are two major differences between 386 32-bit and 286 16-bit protected modes:

1. Offsets are expanded to be 32-bits. This allows an offset to range up to 4 billion. Thus, segments can have sizes up to 4 gigabytes.
2. Segments can be divided into smaller 4K-sized units called *pages*. The virtual memory system works with pages now instead of segments. This means that only parts of segment may be in memory at any one time. In 286 16-bit mode, either the entire segment is in memory or none of it is. This is not practical with the larger segments that 32-bit mode allows.

In Windows 3.x, *standard mode* referred to 286 16-bit protected mode and *enhanced mode* referred to 32-bit mode. Windows 9X, Windows NT, OS/2 and Linux all run in paged 32-bit protected mode.

1.2.9 Interrupts

Sometimes the ordinary flow of a program must be interrupted to process events that require prompt response. The hardware of a computer provides a mechanism called *interrupts* to handle these events. For example, when a mouse is moved, the mouse hardware interrupts the current program to handle the mouse movement (to move the mouse cursor, *etc.*) Interrupts cause control to be passed to an *interrupt handler*. Interrupt handlers are routines that process the interrupt. Each type of interrupt is assigned an integer number. At the beginning of physical memory, a table of *interrupt vectors* resides that contain the segmented addresses of the interrupt handlers. The number of interrupt is essentially an index into this table.

External interrupts are raised from outside the CPU. (The mouse is an example of this type.) Many I/O devices raise interrupts (*e.g.*, keyboard, timer, disk drives, CD-ROM and sound cards). Internal interrupts are raised from within the CPU, either from an error or the interrupt instruction. Error interrupts are also called *traps*. Interrupts generated from the interrupt instruction are called *software interrupts*. DOS uses these types of interrupts to implement its API (Application Programming Interface). More modern operating systems (such as Windows and UNIX) use a C based interface.¹

Many interrupt handlers return control back to the interrupted program when they finish. They restore all the registers to the same values they had before the interrupt occurred. Thus, the interrupted program does runs as if nothing happened (except that it lost some CPU cycles). Traps generally do not return. Often they abort the program.

¹However, they may use a lower level interface at the kernel level.

1.3 Assembly Language

1.3.1 Machine language

Every type of CPU understands its own machine language. Instructions in machine language are numbers stored as bytes in memory. Each instruction has its own unique numeric code called its *operation code* or *opcode* for short. The 80x86 processor's instructions vary in size. The opcode is always at the beginning of the instruction. Many instructions also include data (*e.g.*, constants or addresses) used by the instruction.

Machine language is very difficult to program in directly. Deciphering the meanings of the numerical-coded instructions is tedious for humans. For example, the instruction that says to add the EAX and EBX registers together and store the result back into EAX is encoded by the following hex codes:

```
03 C3
```

This is hardly obvious. Fortunately, a program called an *assembler* can do this tedious work for the programmer.

1.3.2 Assembly language

An assembly language program is stored as text (just as a higher level language program). Each assembly instruction represents exactly one machine instruction. For example, the addition instruction described above would be represented in assembly language as:

```
add eax, ebx
```

Here the meaning of the instruction is *much* clearer than in machine code. The word `add` is a *mnemonic* for the addition instruction. The general form of an assembly instruction is:

```
mnemonic operand(s)
```

An *assembler* is a program that reads a text file with assembly instructions and converts the assembly into machine code. *Compilers* are programs that do similar conversions for high-level programming languages. An assembler is much simpler than a compiler. Every assembly language statement directly represents a single machine instruction. High-level language statements are *much* more complex and may require many machine instructions.

Another important difference between assembly and high-level languages is that since every different type of CPU has its own machine language, it also has its own assembly language. Porting assembly programs between

It took several years for computer scientists to figure out how to even write a compiler!

different computer architectures is *much* more difficult than in a high-level language.

This book's examples uses the Netwide Assembler or NASM for short. It is freely available off the Internet (URL: <http://www.web-sites.co.uk/nasm/>). More common assemblers are Microsoft's Assembler (MASM) or Borland's Assembler (TASM). There are some differences in the assembly syntax for MASM/TASM and NASM.

1.3.3 Instruction operands

Machine code instructions have varying number and type of operands; however, in general, each instruction itself will have a fixed number of operands (0 to 3). Operands can have the following types:

register: These operands refer directly to the contents of the CPU's registers.

memory: These refer to data in memory. The address of the data may be a constant hardcoded into the instruction or may be computed using values of registers. Address are always offsets from the beginning of a segment.

immediate: These are fixed values that are listed in the instruction itself. They are stored in the instruction itself (in the code segment), not in the data segment.

implied: These operands are not explicitly shown. For example, the increment instruction adds one to a register or memory. The one is implied.

1.3.4 Basic instructions

The most basic instruction is the MOV instruction. It moves data from one location to another (like the assignment operator in a high-level language). It takes two operands:

```
mov dest, src
```

The data specified by *src* is copied to *dest*. One restriction is that both operands may not be memory operands. This points out another quirk of assembly. There are often somewhat arbitrary rules about how the various instructions are used. The operands must also be the same size. The value of AX can not be stored into BL.

Here is an example (semicolons start a comment):

```

mov    eax, 3    ; store 3 into EAX register (3 is immediate operand)
mov    bx, ax    ; store the value of AX into the BX register

```

The ADD instruction is used to add integers.

```

add    eax, 4    ; eax = eax + 4
add    al, ah    ; al = al + ah

```

The SUB instruction subtracts integers.

```

sub    bx, 10    ; bx = bx - 10
sub    ebx, edi  ; ebx = ebx - edi

```

The INC and DEC instructions increment or decrement values by one. Since the one is an implicit operand, the machine code for INC and DEC is smaller than for the equivalent ADD and SUB instructions.

```

inc    ecx      ; ecx++
dec    dl       ; dl--

```

1.3.5 Directives

A *directive* is an artifact of the assembler not the CPU. They are generally used to either instruct the assembler to do something or inform the assembler of something. They are not translated into machine code. Common uses of directives are:

- define constants
- define memory to store data into
- group memory into segments
- conditionally include source code
- include other files

NASM code passes through a preprocessor just like C. It has many of the same preprocessor commands as C. However, NASM's preprocessor directives start with a % instead of a # as in C.

The equ directive

The equ directive can be used to define a *symbol*. Symbols are named constants that can be used in the assembly program. The format is:

```
symbol equ value
```

Symbol values can *not* be redefined later.

Unit	Letter
byte	B
word	W
double word	D
quad word	Q
ten bytes	T

Table 1.3: Letters for RESX and DX Directives

The %define directive

This directive is similar to C's #define directive. It is most commonly used to define constant macros just as in C.

```
%define SIZE 100
    mov    eax, SIZE
```

The above code defines a macro named `SIZE` and uses in a `MOV` instruction. Macros are more flexible than symbols in two ways. Macros can be redefined and can be more than simple constant numbers.

Data directives

Data directives are used in data segments to define room for memory. There are two ways memory can be reserved. The first way only defines room for data; the second way defines room and an initial value. The first method uses one of the `RESX` directives. The `X` is replaced with a letter that determines the size of the object (or objects) that will be stored. Table 1.3 shows the possible values.

The second method (that defines an initial value, too) uses one of the `DX` directives. The `X` letters are the same as the `RESX` directives.

It is very common to mark memory locations with *labels*. Labels allow one to easily refer to memory locations in code. Below are several examples:

```
L1    db    0          ; byte labeled L1 with initial value 0
L2    dw    1000       ; word labeled L2 with initial value 1000
L3    db    110101b    ; byte initialized to binary 110101 (53 in decimal)
L4    db    12h        ; byte initialized to hex 12 (18 in decimal)
L5    db    17o        ; byte initialized to octal 17 (15 in decimal)
L6    dd    1A92h      ; double word initialized to hex 1A92
L7    resb  1          ; 1 uninitialized byte
L8    db    "A"        ; byte initialized to ASCII code for A (65)
```

Double quotes and single quotes are treated the same. Consecutive data definitions are stored sequentially in memory. That is, the word `L2` is stored immediately after `L1` in memory. Sequences of memory may also be defined.

```

L9   db      0, 1, 2, 3           ; defines 4 bytes
L10  db      "w", "o", "r", 'd', 0 ; defines a C string = "word"
L11  db      'word', 0           ; same as L10

```

For large sequences, NASM's `TIMES` directive is often useful. This directive repeats its operand a specified number of times. For example,

```

L12  times 100 db 0               ; equivalent to 100 (db 0)'s
L13  resw   100                   ; reserves room for 100 words

```

Remember that labels can be used to refer to data in code. There are two ways that a label can be used. If a plain label is used, it is interpreted as the address (or offset) of the data. If the label is placed inside square brackets (`[]`), it is interpreted as the data at the address. In other words, one should think of a label as a *pointer* to the data and the square brackets dereferences the pointer just as the asterisk does in C. (MASM/TASM follow a different convention.) In 32-bit mode, addresses are 32-bit. Here is some example code:

```

1   mov     al, [L1]              ; copy byte at L1 into AL
2   mov     eax, L1               ; EAX = address of byte at L1
3   mov     [L1], ah             ; copy AH into byte at L1
4   mov     eax, [L6]            ; copy double word at L6 into EAX
5   add     eax, [L6]            ; EAX = EAX + double word at L6
6   add     [L6], eax            ; double word at L6 += EAX
7   mov     al, [L6]            ; copy first byte of double word at L6 into AL

```

Line 7 of the examples shows an important property of NASM. The assembler does *not* keep track of the type of data that a label refers to. It is up to the programmer to make sure that he (or she) uses a label correctly. Later it will be common to store addresses of data in registers and use the register like a pointer variable in C. Again, no checking is made that a pointer is used correctly. In this way, assembly is much more error prone than even C.

Consider the following instruction:

```

mov     [L6], 1                  ; store a 1 at L6

```

This statement produces an `operation size not specified` error. Why? Because the assembler does not know whether to store the 1 as a byte, word or double word. To fix this, add a size specifier:

```

mov     dword [L6], 1           ; store a 1 at L6

```

This tells the assembler to store an 1 at the double word that starts at L6. Other size specifiers are: `BYTE`, `WORD`, `QWORD` and `TWORD`.

print_int	prints out to the screen the value of the integer stored in EAX
print_char	prints out to the screen the value of the character with the ASCII value stored in AL
print_string	prints out to the screen the contents of the string at the <i>address</i> stored in EAX. The string must be a C-type string (<i>i.e.</i> , nul terminated).
print_nl	prints out to the screen a new line character.
read_int	reads an integer from the keyboard and stores it into the EAX register.
read_char	reads a single character from the keyboard and stores its ASCII code into the EAX register.

Table 1.4: Assembly I/O Routines

1.3.6 Input and Output

Input and output are very system dependent activities. It involves interfacing with the system's hardware. High level languages, like C, provide standard libraries of routines that provide a simple, uniform programming interface for I/O. Assembly languages provide no standard libraries. They must either directly access hardware (which is a privileged operation in protected mode) or use whatever low level routines that the operating system provides.

It is very common for assembly routines to be interfaced with C. One advantage of this is that the assembly code can use the standard C library I/O routines. However, one must know the rules for passing information between routines that C uses. These rules are too complicated to cover here. (They are covered later!) To simplify I/O, the author has developed his own routines that hide the complex C rules and provide a much more simple interface. Table 1.4 describes the routines provided. All of the routines preserve the value of all registers, except for the read routines. These routines do modify the value of the EAX register. To use these routines, one must include a file with information that the assembler needs to use them. To include a file in NASM, use the `%include` preprocessor directive. The following line includes the file needed by the author's I/O routines:

```
%include "asm_io.inc"
```

To use one of the print routines, one loads EAX with the correct value and uses a `CALL` instruction to invoke it. The `CALL` instruction is equivalent to a function call in a high level language. It jumps execution to another section of code, but returns back to its origin after the routine is over.

The example program below shows several examples of calls to these I/O routines.

1.3.7 Debugging

The author's library also contains some useful routines for debugging programs. These debugging routines display information about the state of the computer without modifying the state. These routines are really *macros* that preserve the current state of the CPU and then make a subroutine call. The macros are defined in the `asm_io.inc` file discussed above. Macros are used like ordinary instructions. Operands of macros are separated by commas.

There are four debugging routines named `dump_regs`, `dump_mem`, `dump_stack` and `dump_math`; they display the values of registers, memory, stack and the math coprocessor, respectively.

dump_regs This macro prints out the values of the registers (in hexadecimal) of the computer to `stdout` (*i.e.*, the screen). It takes a single integer argument that is printed out as well. This can be used to distinguish the output of different `dump_regs` commands.

dump_mem This macro prints out the values of a region of memory (in hexadecimal) and also as ASCII characters. It takes three comma delimited arguments. The first is an integer that is used to label the output (just as `dump_regs` argument). The second argument is the address to display. (This can be a label.) The last argument is the number of 16-byte paragraphs to display after the address. The memory displayed will start on the first paragraph boundary before the requested address.

dump_stack This macro prints out the values on the CPU stack. (The stack will be covered in Chapter 4.) The stack is organized as double words and this routine displays them this way. It takes three comma delimited arguments. The first is an integer label (like `dump_regs`). The second is the number of double words to display *below* the address that the `EBP` register holds and the third argument is the number of double words to display *above* the address in `EBP`.

dump_math This macro prints out the values of the registers of the math coprocessor. It takes a single integer argument that is used to label the output just as the argument of `dump_regs` does.


```
1 int main()  
2 {  
3     int ret_status ;  
4     ret_status = asm_main();  
5     return ret_status ;  
6 }
```

Figure 1.6: `driver.c` code

1.4 Creating a Program

Today, it is unusual to create a stand alone program written completely in assembly language. Assembly is usually used to key certain critical routines. Why? It is *much* easier to program in a higher level language than in assembly. Also, using assembly makes a program very hard to port to other platforms. In fact, it is rare to use assembly at all.

So, why should anyone learn assembly at all?

1. Sometimes code written in assembly can be faster and smaller than compiler generated code.
2. Assembly allows access to direct hardware features of the system that might be difficult or impossible to use from a higher level language.
3. Learning to program in assembly helps one gain a deeper understanding of how computers work.
4. Learning to program in assembly helps one understand better how compilers and high level languages like C work.

These last two points demonstrate that learning assembly can be useful even if one never programs in it later. In fact, the author rarely programs in assembly, but he uses the ideas he learned from it everyday.

1.4.1 First program

The early programs in this text will all start from the simple C driver program in Figure 1.6. It simply calls another function named `asm_main`. This is really a routine that will be written in assembly. There are several advantages in using the C driver routine. First, this lets the C system set up the program to run correctly in protected mode. All the segments and their corresponding segment registers will be initialized by C. The assembly code need not worry about any of this. Secondly, the C library will also be available to be used by the assembly code. The author's I/O routines take

advantage of this. They use C's I/O functions (`printf`, *etc.*). The following shows a simple assembly program.

```
_____ first.asm _____
1 ; file: first.asm
2 ; First assembly program. This program asks for two integers as
3 ; input and prints out their sum.
4 ;
5 ; To create executable using djgpp:
6 ; nasm -f coff first.asm
7 ; gcc -o first first.o driver.c asm_io.o
8
9 %include "asm_io.inc"
10 ;
11 ; initialized data is put in the .data segment
12 ;
13 segment .data
14 ;
15 ; These labels refer to strings used for output
16 ;
17 prompt1 db "Enter a number: ", 0 ; don't forget nul terminator
18 prompt2 db "Enter another number: ", 0
19 outmsg1 db "You entered ", 0
20 outmsg2 db " and ", 0
21 outmsg3 db ", the sum of these is ", 0
22
23 ;
24 ; uninitialized data is put in the .bss segment
25 ;
26 segment .bss
27 ;
28 ; These labels refer to double words used to store the inputs
29 ;
30 input1 resd 1
31 input2 resd 1
32
33 ;
34 ; code is put in the .text segment
35 ;
36 segment .text
37     global _asm_main
38 _asm_main:
39     enter 0,0 ; setup routine
```

```
40     pusha
41
42     mov     eax, prompt1      ; print out prompt
43     call   print_string
44
45     call   read_int          ; read integer
46     mov     [input1], eax    ; store into input1
47
48     mov     eax, prompt2      ; print out prompt
49     call   print_string
50
51     call   read_int          ; read integer
52     mov     [input2], eax    ; store into input2
53
54     mov     eax, [input1]     ; eax = dword at input1
55     add     eax, [input2]     ; eax += dword at input2
56     mov     ebx, eax         ; ebx = eax
57
58     dump_regs 1              ; print out register values
59     dump_mem  2, outmsg1, 1  ; print out memory
60 ;
61 ; next print out result message as series of steps
62 ;
63     mov     eax, outmsg1
64     call   print_string      ; print out first message
65     mov     eax, [input1]
66     call   print_int         ; print out input1
67     mov     eax, outmsg2
68     call   print_string      ; print out second message
69     mov     eax, [input2]
70     call   print_int         ; print out input2
71     mov     eax, outmsg3
72     call   print_string      ; print out third message
73     mov     eax, ebx
74     call   print_int         ; print out sum (ebx)
75     call   print_nl          ; print new-line
76
77     popa
78     mov     eax, 0           ; return back to C
79     leave
80     ret
```

first.asm

Line 13 of the program defines a section of the program that specifies memory to be stored in the data segment (whose name is `.data`). Only initialized data should be defined in this segment. On lines 17 to 21, several strings are declared. They will be printed with the C library and so must be terminated with a *nul* character (ASCII code 0). Remember that is a big difference between `0` and `'0'`.

Uninitialized data should be declared in the bss segment (named `.bss` on line 26). This segment gets its name from an early UNIX-based assembler operator that meant “block started by symbol.” There is also a stack segment too. It will be discussed later.

The code segment is named `.text` historically. It is where instructions are placed. Note that the code label for the main routine (line 38) has an underscore prefix. This is part of the *C calling convention*. This convention specifies the rules C uses when compiling code. It is very important to know this convention when interfacing C and assembly. Later the entire convention will be presented; however, for now, one only needs to know that all C symbols (*i.e.*, functions and global variables) have a underscore prefix appended to them by the C compiler. (This rule is specifically for DOS/Windows, the Linux C compiler does not prepend anything to C symbol names.)

The `global` directive on line 37 tells the assembler to make the `_asm_main` label global. Unlike in C, labels have *internal scope* by default. This means that only code in the same module can use the label. The `global` directive gives the specified label (or labels) *external scope*. This type of label can be accessed by any module in the program. The `asm_io` module declares the `print_int`, *et.al.* labels to be global. This is why one can use them in the `first.asm` module.

1.4.2 Compiler dependencies

The assembly code above is specific to the free GNU²-based DJGPP C/C++ compiler.³ This compiler can be freely downloaded from the Internet. It requires a 386-based PC or better and runs under DOS, Windows 95/98 or NT. This compiler uses object files in the COFF (Common Object File Format) format. To assemble to this format use the `-f coff` switch with `nasm` (as shown in the comments of the above code). The extension of the resulting object file will be `o`.

The Linux C compiler is a GNU compiler also. To convert the code above to run under Linux, simply remove the underscore prefixes in lines 38 and 39. Linux uses the ELF (Executable and Linkable Format) format for

²GNU is a project of the Free Software Foundation (<http://www.fsf.org>)

³<http://www.delorie.com/djgpp>

object files. Use the `-f elf` switch for Linux. It also produces an object with an `o` extension.

Borland C/C++ is another popular compiler. It uses the Microsoft OMF format for object files. Use the `-f obj` switch for Borland compilers. The extension of the object file will be `obj`. The OMF format uses different `segment` directives than the other object formats. The data segment (line 13) must be changed to:

```
segment _DATA public align=4 class=DATA use32
```

The bss segment (line 26) must be changed to:

```
segment _BSS public align=4 class=BSS use32
```

The text segment (line 36) must be changed to:

```
segment _TEXT public align=1 class=CODE use32
```

In addition a new line should be added before line 36:

```
group DGROUP _BSS _DATA
```

The Microsoft C/C++ can use either the OMF format or the Win32 format for object files. (If given a OMF format, it converts the information to Win32 format internally.) Win32 format allows segments to be defined just as for DJGPP and Linux. Use the `-f win32` switch to output in this mode. The extension of the object file will be `obj`.

1.4.3 Assembling the code

The first step is to assembly the code. From the command line, type:

```
nasm -f object-format first.asm
```

where *object-format* is either *coff*, *elf*, *obj* or *win32* depending on what C compiler will be used. (Remember that the source file must be changed for both Linux and Borland as well.)

1.4.4 Compiling the C code

Compile the `driver.c` file using a C compiler. For DJGPP, use:

```
gcc -c driver.c
```

The `-c` switch means to just compile, do not attempt to link yet. This same switch works on Linux, Borland and Microsoft compilers as well.

1.4.5 Linking the object files

Linking is the process of combining the machine code and data in object files and library files together to create an executable file. As will be shown below, this process is complicated.

C code requires the standard C library and special *startup code* to run. It is *much* easier to let the C compiler call the linker with the correct parameters, than to try to call the linker directly. For example, to link the code for the first program using DJGPP, use:

```
gcc -o first driver.o first.o asm_io.o
```

This creates an executable called `first.exe` (or just `first` under Linux).

With Borland, one would use:

```
bcc32 first.obj driver.obj asm_io.obj
```

Borland uses the name of the first file listed to determine the executable name. So in the above case, the program would be named `first.exe`.

It is possible to combine the compiling and linking step. For example,

```
gcc -o first driver.c first.o asm_io.o
```

Now `gcc` will compile `driver.c` and then link.

1.4.6 Understanding an assembly listing file

The `-l listing-file` switch can be used to tell `nasm` to create a listing file of a given name. This file shows how the code was assembled. Here is how lines 17 and 18 (in the data segment) appear in the listing file. (The line numbers are in the listing file; however notice that the line numbers in the source file may not be the same as the line numbers in the listing file.)

```
48 00000000 456E7465722061206E-   prompt1 db   "Enter a number: ", 0
49 00000009 756D6265723A2000
50 00000011 456E74657220616E6F-   prompt2 db   "Enter another number: ", 0
51 0000001A 74686572206E756D62-
52 00000023 65723A2000
```

The first column in each line is the line number and the second is the offset (in hex) of the data in the segment. The third column shows the raw hex values that will be stored. In this case the hex data correspond to ASCII codes. Finally, the text from the source file is displayed on the line. The offsets listed in the second column are very likely *not* the true offsets that the data will be placed at in the complete program. Each module may define its own labels in the data segment (and the other segments, too). In the link

step (see section 1.4.5), all these data segment label definitions are combined to form one data segment. The new final offsets are then computed by the linker.

Here is a small section (lines 54 to 56 of the source file) of the text segment in the listing file:

```
94 0000002C A1[00000000]      mov     eax, [input1]
95 00000031 0305[04000000]      add     eax, [input2]
96 00000037 89C3                mov     ebx, eax
```

The third column shows the machine code generated by the assembly. Often the complete code for an instruction can not be computed yet. For example, in line 94 the offset (or address) of `input1` is not known until the code is linked. The assembler can compute the op-code for the `mov` instruction (which from the listing is `A1`), but it writes the offset in square brackets because the exact value can not be computed yet. In this case, a temporary offset of 0 is used because `input1` is at the beginning of the part of the bss segment defined in this file. Remember this does *not* mean that it will be at the beginning of the final bss segment of the program. When the code is linked, the linker will insert the correct offset into the position. Other instructions, like line 96, do not reference any labels. Here the assembler can compute the complete machine code.

If one looks closely at line 95, something seems very strange about the offset in the square brackets of the machine code. The `input2` label is at offset 4 (as defined in this file); however, the offset that appears is not 00000004, but 04000000. Why? Different processors store multibyte integers in different orders in memory. There are two popular methods of storing integers: *big endian* and *little endian*. Big endian is the method that seems the most natural. The biggest (*i.e.*, most significant) byte is stored first, then the next biggest, *etc.* For example, the dword 00000004 would be stored as the four bytes 00 00 00 04. IBM mainframes, most RISC processors and Motorola processors all use this big endian method. However, Intel-based processors use the little endian method! Here the least significant byte is stored first. So, 00000004 is stored in memory as 04 00 00 00. This format is hardwired into the CPU and can not be changed (actually, Intel is working on a new 64-bit processor for which the format can be specified.) Normally, the programmer does not need to worry about which format is used. However, there are circumstances where it is important.

1. When binary data is transferred between different computers (either from files or through a network).
2. When binary data is written out to memory as a multibyte integer and then read back as individual bytes or *vis versa*.

```

1  _____ skel.asm _____
2  %include "asm_io.inc"
3  segment .data
4  ;
5  ; initialized data is put in the data segment here
6  ;
7  segment .bss
8  ;
9  ; uninitialized data is put in the bss segment
10 ;
11
12 segment .text
13     global  _asm_main
14 _asm_main:
15     enter  0,0           ; setup routine
16     pusha
17
18 ;
19 ; code is put in the text segment. Do not modify the code before
20 ; or after this comment.
21 ;
22
23     popa
24     mov   eax, 0         ; return back to C
25     leave
26     ret
27  _____ skel.asm _____
```

Figure 1.7: Skeleton Program

1.5 Skeleton File

Figure 1.7 a skeleton file that can be used as a starting point for writing assembly programs.

Chapter 2

Basic Assembly Language

2.1 Working with Integers

2.1.1 Integer representation

Integers come in two flavors: unsigned and signed. Unsigned integers (which are non-negative) are represented in a very straightforward binary manner. The number 200 as an one byte unsigned integer would be represented as by 11001000 (or C8 in hex).

Signed integers (which may be positive or negative) are represented in a more complicated ways. For example, consider -56 . $+56$ as a byte would be represented by 00111000. On paper, one could represent -56 as -111000 , but how would this be represented in a byte in the computer's memory. How would the minus sign be stored?

There are three general techniques that have been used to represent signed integers in computer memory. All of these methods use the most significant bit of the integer as a *sign bit*. This bit is 0 if the number is positive and 1 if negative.

Signed magnitude

The first method is the simplest and is called *signed magnitude*. It represents the integer as two parts. The first part is the sign bit and the second is the magnitude of the integer. So 56 would be represented as the byte 00111000 (the sign bit is underlined) and -56 would be 10111000. The largest byte value would be 01111111 or $+127$ and the smallest byte value would be 11111111 or -127 . To negate a value, the sign bit is reversed. This method is straightforward, but it does have its drawbacks. First, there are two possible values of zero, $+0$ (00000000) and -0 (10000000). Since zero is neither positive nor negative, both of these representations should act the same. This complicates the logic of arithmetic for the CPU. Secondly,

general arithmetic is also complicated. If 10 is added to -56 , this must be recast as 10 subtracted by 56. Again, this complicates the logic of the CPU.

One's complement

The second method is known as *one's complement* representation. The one's complement of a number is found by reversing each bit in the number. (Another way to look at it is that the new bit value is $1 - \text{oldbitvalue}$.) For example, the one's complement of 00111000 ($+56$) is 11000111 . In one's complement notation, computing the one's complement is equivalent to negation. Thus, 11000111 is the representation for -56 . Note that the sign bit was automatically changed by one's complement and that as one would expect taking the one's complement twice yields the original number. As for the first method, there are two representations of zero: 00000000 ($+0$) and 11111111 (-0). Arithmetic with one's complement numbers is complicated.

There is a handy trick to finding the one's complement of a number in hexadecimal without converting it to binary. The trick is to subtract the hex digit from F (or 15 in decimal). This method assumes that the number of bits in the number is a multiple of 4. Here is an example: $+56$ is represented by 38 in hex. To find the one's complement, subtract each digit from F to get C7 in hex. This agrees with the result above.

Two's complement

The first two methods described were used on early computers. Modern computers use a third method called *two's complement* representation. The two's complement of a number is found by the following two steps:

1. Find the one's complement of the number
2. Add one to the result of step 1

Here's an example using 00111000 (56). First the one's complement is computed: 11000111 . Then one is added:

$$\begin{array}{r} 11000111 \\ + \quad \quad 1 \\ \hline 11001000 \end{array}$$

In two complement's notation, computing the two's complement is equivalent to negating a number. Thus, 11001000 is the two's complement representation of -56 . Two negations should reproduce the original number. Surprising two's complement does meet this requirement. Take the two's

Number	Hex Representation
0	00
1	01
127	7F
-128	80
-127	81
-2	FE
-1	FF

Table 2.1: Two's Complement Representation

complement of 11001000 by adding one to the one's complement.

$$\begin{array}{r}
 \underline{00110111} \\
 + \quad \quad \quad 1 \\
 \hline
 \underline{00111000}
 \end{array}$$

When performing the addition in the two's complement operation, the addition of the leftmost bit may produce a carry. This carry is *not* used. Remember that all data on the computer is of some fixed size (in terms of number of bits). Adding two bytes always produces a byte as a result (just as adding two words produces a word, *etc.*) This property is important for two's complement notation. For example, consider zero as a one byte two's complement number (00000000). Computing its two complement produces the sum:

$$\begin{array}{r}
 \underline{11111111} \\
 + \quad \quad \quad 1 \\
 \hline
 c \quad \underline{00000000}
 \end{array}$$

where *c* represents a carry. (Later it will be shown how to detect this carry, but it is not stored in the result.) Thus, in two's complement notation there is only one zero. This makes two's complement arithmetic simpler than the previous methods.

Using two's complement notation, a signed byte can be used to represent the numbers -128 to $+127$. Table 2.1 shows some selected values. If 16 bits are used, the signed numbers $-32,768$ to $+32,767$ can be represented. $+32,767$ is represented by 7FFF, $-32,768$ by 8000, -128 as FF80 and -1 as FFFF. 32 bit two's complement numbers range from -2 billion to $+2$ billion approximately.

The CPU has no idea what a particular byte (or word or double word) is supposed to represent. Assembly does not have the idea of types that a high level language has. How data is interpreted depends on what instruction is used on the data. Whether the hex value FF is considered to represent a signed -1 or a unsigned $+255$ depends on the programmer. The C language

defines signed and unsigned integer types. This allows a C compiler to determine the correct instructions to use with the data.

2.1.2 Sign extension

In assembly, all data has a specified size. It is not uncommon to need to change the size of data to use it with other data. Decreasing size is the easiest.

Decreasing size of data

To decrease the size of data, simply remove the more significant bits of the data. Here's a trivial example:

```
mov    ax, 0034h    ; ax = 52 (stored in 16 bits)
mov    cl, al       ; cl = lower 8-bits of ax
```

Of course, if the number can not be represented correctly in the smaller size, decreasing the size does not work. For example, if `AX` were `0134h` (or 308 in decimal) then the above code would still set `CL` to `34h`. This method works with both signed and unsigned numbers. Consider signed numbers, if `AX` was `FFFFh` (-1 as a word), then `CL` would be `FFh` (-1 as a byte). However, note that this is not correct if the value in `AX` was unsigned!

The rule for unsigned numbers is that all the bits being removed must be 0 for the conversion to be correct. The rule for signed numbers is that the bits being removed must be either all 1's or all 0's. In addition, the first bit not being removed must have the same value as the removed bits. This bit will be the new sign bit of the smaller value. It is important that it be same as the original sign bit!

Increasing size of data

Increasing the size of data is more complicated than decreasing. Consider the hex byte `FF`. If it is extended to a word, what value should the word have? It depends on how `FF` is interpreted. If `FF` is a unsigned byte (255 in decimal), then the word should be `00FF`; however, if it is a signed byte (-1 in decimal), then the word should be `FFFF`.

In general, to extend an unsigned number, one makes all the new bits of the expanded number 0. Thus, `FF` becomes `00FF`. However, to extend a signed number, one must *extend* the sign bit. This means that the new bits become copies of the sign bit. Since the sign bit of `FF` is 1, the new bits must also be all ones, to produce `FFFF`. If the signed number `5A` (90 in decimal) was extended, the result would be `005A`.

There are several instructions that the 80386 provides for extension of numbers. Remember that the computer does not know whether a number is signed or unsigned. It is up to the programmer to use the correct instruction.

For unsigned numbers, one can simply put zeros in the upper bits using a MOV instruction. For example, to extend the byte in AL to an unsigned word in AX:

```
mov    ah, 0    ; zero out upper 8-bits
```

However, it is not possible to use a MOV instruction to convert the unsigned word in AX to an unsigned double word in EAX. Why not? There is no way to specify the upper 16 bits of EAX in a MOV. The 80386 solves this problem by providing a new instruction MOVZX. This instruction has two operands. The destination (first operand) must be a 16 or 32 bit register. The source (second operand) may be an 8 or 16 bit register or a byte or word of memory. The other restriction is that the destination must be larger than the source. (Most instructions require the source and destination to be the same size.) Here are some examples:

```
movzx  eax, ax      ; extends ax into eax
movzx  eax, al      ; extends al into eax
movzx  ax, al       ; extends al into ax
movzx  ebx, ax      ; extends ax into ebx
```

For signed numbers, there is no easy way to use the MOV instruction for any case. The 8086 provided several instructions to extend signed numbers. The CBW (Convert Byte to Word) instruction sign extends the AL register into AX. The operands are implicit. The CWD (Convert Word to Double word) instruction sign extends AX into DX:AX. The notation DX:AX means to think of the DX and AX registers as one 32 bit register with the upper 16 bits in DX and the lower bits in AX. (Remember that the 8086 did not have any 32 bit registers!) The 80386 added several new instructions. The CWDE (Convert Word to Double word Extended) instruction sign extends AX into EAX. The CDQ (Convert Double word to Quad word) instruction sign extends EAX into EDX:EAX (64 bits!). Finally, the MOVSX instruction works like MOVZX except it uses the rules for signed numbers.

Application to C programming

Extending of unsigned and signed integers also occurs in C. Variables in C may be declared as either signed or unsigned (`int` is signed). Consider the code in Figure 2.1. In line 3, the variable `a` is extended using the rules for unsigned values (using MOVZX), but in line 4, the signed rules are used for `b` (using MOVSX).

ANSI C does not define whether the char type is signed or not, it is up to each individual compiler to decide this. That is why the type is explicitly defined in Figure 2.1.

```

1 unsigned char uchar = 0xFF;
2 signed char  schar = 0xFF;
3 int a = (int) uchar;    /* a = 255 (0x000000FF) */
4 int b = (int) schar;    /* a = -1 (0xFFFFFFFF) */

```

Figure 2.1:

```

char ch;
while( (ch = fgetc(fp)) != EOF ) {
    /* do something with ch */
}

```

Figure 2.2:

There is a common C programming bug that directly relates to this subject. Consider the code in Figure 2.2. The prototype of `fgetc()` is:

```
int fgetc( FILE * );
```

One might question why does the function return back an `int` since it reads characters? The reason is that it normally does return back a `char` (extended to an `int` value using zero extension). However, there is one value that it may return that is not a character, `EOF`. This is a macro that is usually defined as `-1`. Thus, `fgetc()` either returns back a `char` extended to an `int` value (which looks like `000000xx` in hex) or `EOF` (which looks like `FFFFFFFF` in hex).

The basic problem with the program in Figure 2.2 is that `fgetc()` returns an `int`, but this value is stored in a `char`. C will truncate the higher order bits to fit the `int` value into the `char`. The only problem is that the numbers (in hex) `000000FF` and `FFFFFFFF` both will be truncated to the byte `FF`. Thus, the while loop can not distinguish between reading the byte `FF` from the file and end of file.

Exactly what the code does in this case, depends on whether `char` is signed or unsigned. Why? Because in line 2, `ch` is compared with `EOF`. Since `EOF` is an `int` value¹, `ch` will be extended to an `int` so that two values being compared are of the same size². As Figure 2.1 showed, where the variable is signed or unsigned is very important.

If `char` is unsigned, `FF` is extended to be `000000FF`. This is compared to `EOF` (`FFFFFFFF`) and found to be not equal. Thus, the loop never ends!

¹It is a common misconception that files have an EOF character at their end. This is *not* true!

²The reason for this requirement will be shown later.

If `char` is signed, `FF` is extended to `FFFFFFFF`. This does compare as equal and the loop ends. However, since the byte `FF` may have been read from the file, the loop could be ending prematurely.

The solution to this problem is to define the `ch` variable as an `int`, not a `char`. When this is done, no truncating or extension is done in line 2. Inside the loop, it is safe to truncate the value since `ch` *must* actually be a simple byte there.

2.1.3 Two's complement arithmetic

As was seen earlier, the `add` instruction performs addition and the `sub` instruction performs subtraction. Two of the bits in the `FLAGS` register that these instructions set are the *overflow* and *carry flag*. The overflow flag is set if the true result of the operation is too big to fit into the destination for signed arithmetic. The carry flag is set if there is a carry in the msb of an addition or a borrow in the msb of a subtraction. Thus, it can be used to detect overflow for unsigned arithmetic. The uses of the carry flag for signed arithmetic will be seen shortly. One of the great advantages of 2's complement is that the rules for addition and subtraction are exactly the same as for unsigned integers. Thus, `add` and `sub` may be used on signed or unsigned integers.

$$\begin{array}{r} 002C \\ + \text{FFFF} \\ \hline 002B \end{array} \quad \begin{array}{r} 44 \\ + (-1) \\ \hline 43 \end{array}$$

There is a carry generated, but it is not part of the answer.

There are two different multiply and divide instructions. First, to multiply use either the `MUL` or `IMUL` instruction. The `mul` instruction is used to multiply unsigned numbers and `imul` is used to multiply signed integers. Why are two different instructions needed? The rules for multiplication are different for unsigned and 2's complement signed numbers. How so? Consider the multiplication of the byte `FF` with itself yielding a word result. Using unsigned multiplication this is 255 times 255 or 65025 (or `FE01` in hex). Using signed multiplication this is -1 times -1 or 1 (or `0001` in hex).

There are several forms of the multiplication instructions. The oldest form looks like:

```
mul    source
```

The *source* is either a register or a memory reference. It can not be an immediate value. Exactly what multiplication is performed depends on the size of the source operand. If the operand is byte sized, it is multiplied by the byte in the `AL` register and the result is stored in the 16 bits of `AX`. If the source is 16-bit, it is multiplied by the word in `AX` and the 32-bit result

dest	source1	source2	Action
	reg/mem8		AX = AL*source1
	reg/mem16		DX:AX = AX*source1
	reg/mem32		EDX:EAX = EAX*source1
reg16	reg/mem16		dest *= source1
reg32	reg/mem32		dest *= source1
reg16	immed8		dest *= immed8
reg32	immed8		dest *= immed8
reg16	immed16		dest *= immed16
reg32	immed32		dest *= immed32
reg16	reg/mem16	immed8	dest = source1*source2
reg32	reg/mem32	immed8	dest = source1*source2
reg16	reg/mem16	immed16	dest = source1*source2
reg32	reg/mem32	immed32	dest = source1*source2

Table 2.2: `imul` Instructions

is stored in DX:AX. If the source is 32-bit, it is multiplied by EAX and the 64-bit result is stored into EDX:EAX.

The `imul` instruction has the same formats as `mul`, but also adds some other instruction formats. There are two and three operand formats:

```
imul  dest, source1
imul  dest, source1, source2
```

Table 2.2 shows the possible combinations.

The two division operators are `DIV` and `IDIV`. They perform unsigned and signed integer division respectively. The general format is:

```
div  source
```

If the source is 8-bit, then AX is divided by the operand. The quotient is stored in AL and the remainder in AH. If the source is 16-bit, then DX:AX is divided by the operand. The quotient is stored into AX and remainder into DX. If the source is 32-bit, then EDX:EAX is divided by the operand and the quotient is stored into EAX and the remainder into EDX. The `IDIV` instruction works the same way. There are no special `IDIV` instructions like the special `IMUL` ones. If the quotient is too big to fit into its register or the divisor is zero, the program is interrupted and terminates. A very common error is to forget to initialize DX or EDX before division.

The `NEG` instruction negates its single operand by computing its two's complement. Its operand may be any 8-bit, 16-bit, or 32-bit register or memory location.

2.1.4 Example program

```

1  _____ math.asm _____
2  %include "asm_io.inc"
3  segment .data          ; Output strings
4  prompt                db   "Enter a number: ", 0
5  square_msg            db   "Square of input is ", 0
6  cube_msg              db   "Cube of input is ", 0
7  cube25_msg           db   "Cube of input times 25 is ", 0
8  quot_msg              db   "Quotient of cube/100 is ", 0
9  rem_msg               db   "Remainder of cube/100 is ", 0
10 neg_msg               db   "The negation of the remainder is ", 0
11
12 segment .bss
13 input                 resd 1
14
15 segment .text
16     global _asm_main
17 _asm_main:
18     enter 0,0          ; setup routine
19     pusha
20     mov  eax, prompt
21     call print_string
22
23     call read_int
24     mov  [input], eax
25
26     imul eax          ; edx:eax = eax * eax
27     mov  ebx, eax     ; save answer in ebx
28     mov  eax, square_msg
29     call print_string
30     mov  eax, ebx
31     call print_int
32     call print_nl
33
34     mov  ebx, eax
35     imul ebx, [input] ; ebx *= [input]
36     mov  eax, cube_msg
37     call print_string
38     mov  eax, ebx
39     call print_int
40     call print_nl

```

```
41
42     imul    ecx, ebx, 25      ; ecx = ebx*25
43     mov     eax, cube25_msg
44     call    print_string
45     mov     eax, ecx
46     call    print_int
47     call    print_nl
48
49     mov     eax, ebx
50     cdq                    ; initialize edx by sign extension
51     mov     ecx, 100         ; can't divide by immediate value
52     idiv   ecx              ; edx:eax / ecx
53     mov     ecx, eax         ; save quotient into ecx
54     mov     eax, quot_msg
55     call    print_string
56     mov     eax, ecx
57     call    print_int
58     call    print_nl
59     mov     eax, rem_msg
60     call    print_string
61     mov     eax, edx
62     call    print_int
63     call    print_nl
64
65     neg     edx              ; negate the remainder
66     mov     eax, neg_msg
67     call    print_string
68     mov     eax, edx
69     call    print_int
70     call    print_nl
71
72     popa
73     mov     eax, 0          ; return back to C
74     leave
75     ret
```

math.asm

2.1.5 Extended precision arithmetic

Assembly language also provides instructions that allow one to perform addition and subtraction of numbers larger than double words. These instructions use the carry flag. As stated above, both the ADD and SUB instructions modify the carry flag if a carry or borrow are generated, respectively.

This information stored in the carry flag can be used to add or subtract large numbers by breaking up the operation into smaller double word (or smaller) pieces.

The ADC and SBB instructions use this information in the carry flag. The ADC instruction performs the following operation:

$$\textit{operand1} = \textit{operand1} + \textit{carry flag} + \textit{operand2}$$

The SBB instruction performs:

$$\textit{operand1} = \textit{operand1} - \textit{carry flag} - \textit{operand2}$$

How are these used? Consider the sum of 64-bit integers in EDX:EAX and EBX:ECX. The following code would store the sum in EDX:EAX:

```

1      add    eax, ecx      ; add lower 32-bits
2      adc    edx, ebx      ; add upper 32-bits and carry from previous sum
```

Subtraction is very similar. The following code subtracts EBX:ECX from EDX:EAX:

```

1      sub    eax, ecx      ; subtract lower 32-bits
2      sbb    edx, ebx      ; subtract upper 32-bits and borrow
```

For *really* large numbers, a loop could be used (see Section 2.2). For a sum loop, it would be convenient to use ADC instruction for every iteration (instead of all but the first iteration). This can be done by using the CLC (CLear Carry) instruction right before the loop starts to initialize the carry flag to 0. If the carry flag is 0, there is no difference between the ADD and ADC instructions. The same idea can be used for subtraction, too.

2.2 Control Structures

High level languages provide high level control structures (*e.g.*, the *if* and *while* statements) that control the thread of execution. Assembly language does not provide such complex control structures. It instead uses the infamous *goto* and used inappropriately can result in spaghetti code! However, it *is* possible to write structured assembly language programs. The basic procedure is to design the program logic using the familiar high level control structures and translate the design into the appropriate assembly language (much like a compiler would do).

2.2.1 Comparisons

Control structures decide what to do based on comparisons of data. In assembly, the result of a comparison is stored in the FLAGS register to be used later. The 80x86 provides the `CMP` instruction to perform comparisons. The FLAGS register is set based on the difference of the two operands of the `CMP` instruction. The operands are subtracted and the FLAGS are set based on the result, but the result is *not* stored anywhere. If you need the result use the `SUB` instead of the `CMP` instruction.

For unsigned integers, there are two flags (bits in the FLAGS register) that are important: the zero (ZF) and carry (CF) flags. The zero flag is set (1) if the resulting difference would be zero. The carry flag is used as a borrow flag for subtraction. Consider a comparison like:

```
cmp    vleft, vright
```

The difference of `vleft - vright` is computed and the flags are set accordingly. If the difference of the of `CMP` is zero, `vleft = vright`, then ZF is set (*i.e.*, 1) and the CF is unset (*i.e.*, 0). If `vleft > vright`, then ZF is unset and CF is unset (no borrow). If `vleft < vright`, then ZF is unset and CF is set (borrow).

Why does $SF = OF$ if $vleft > vright$? If there is no overflow, then the difference will have the correct value and must be non-negative. Thus, $SF = OF = 0$. However, if there is an overflow, the difference will not have the correct value (and in fact will be negative). Thus, $SF = OF = 1$.

For signed integers, there are three flags that are important: the zero (ZF) flag, the overflow (OF) flag and the sign (SF) flag. The overflow flag is set if the result of an operation overflows (or underflows). The sign flag is set if the result of an operation is negative. If `vleft = vright`, the ZF is set (just as for unsigned integers). If `vleft > vright`, ZF is unset and $SF = OF$. If `vleft < vright`, ZF is unset and $SF \neq OF$.

Do not forget that other instructions can also change the FLAGS register, not just `CMP`.

2.2.2 Branch instructions

Branch instructions can transfer execution to arbitrary points of a program. In other words, they act like a *goto*. There are two types of branches: unconditional and conditional. An unconditional branch is just like a *goto*, it always makes the branch. A conditional branch may or may not make the branch depending on the flags in the FLAGS register. If a conditional branch does not make the branch, control passes to the next instruction.

The `JMP` (short for *jump*) instruction makes unconditional branches. Its single argument is usually a *code label* to the instruction to branch to. The assembler or linker will replace the label with correct address of the instruction. This is another one of the tedious operations that the assembler does to make the programmer's life easier. It is important to realize that

JZ	branches only if ZF is set
JNZ	branches only if ZF is unset
JO	branches only if OF is set
JNO	branches only if OF is unset
JS	branches only if SF is set
JNS	branches only if SF is unset
JC	branches only if CF is set
JNC	branches only if CF is unset
JP	branches only if PF is set
JNP	branches only if PF is unset

Table 2.3: Simple Conditional Branches

the statement immediately after the `JMP` instruction will never be executed unless another instruction branches to it!

There are several variations of the jump instruction:

SHORT This jump is very limited in range. It can only move up or down 128 bytes in memory. The advantage of this type is that it uses less memory than the others. It uses a single signed byte to store the *displacement* of the jump. The displacement is how bytes to move ahead or behind. (The displacement is added to EIP). To specify a short jump, use the `SHORT` keyword immediately before the label in the `JMP` instruction.

NEAR This jump is the default type for both unconditional and conditional branches, it can be used to jump to any location in a segment. Actually, the 80386 supports two types of near jumps. One uses two bytes for the displacement. This allows one to move up or down roughly 32,000 bytes. The other type uses four bytes for the displacement, which of course allows one to move to any location in the code segment. The four byte type is the default in 386 protected mode. The two byte type can be specified by putting the `WORD` keyword before the label in the `JMP` instruction.

FAR This jump allows control to move to another code segment. This is a very rare thing to do in 386 protected mode.

Valid code labels follow the same rules as data labels. Code labels are defined by placing them in the code segment in front of the statement they label. A colon is placed at the end of the label at its point of definition. The colon is *not* part of the name.

There are many different conditional branch instructions. They also take a code label as their single operand. The simplest ones just look at a

single flag in the FLAGS register to determine whether to branch or not. See Table 2.3 for a list of these instructions. (PF is the *parity flag* which indicates the odd or evenness of a result.)

The following pseudo-code:

```
if ( EAX == 0 )
    EBX = 1;
else
    EBX = 2;
```

could be written in assembly as:

```
1      cmp    eax, 0          ; set flags (ZF set if eax - 0 = 0)
2      jz     thenblock      ; if ZF is set branch to thenblock
3      mov    ebx, 2         ; ELSE part of IF
4      jmp    next          ; jump over THEN part of IF
5 thenblock:
6      mov    ebx, 1         ; THEN part of IF
7 next:
```

Other comparisons are not so easy using the conditional branches in Table 2.3. To illustrate, consider the following pseudo-code:

```
if ( EAX >= 5 )
    EBX = 1;
else
    EBX = 2;
```

If EAX is greater than or equal to five, the ZF may be set or unset and SF will equal OF. Here is assembly code that tests for these conditions (assuming that EAX is signed):

```
1      cmp    eax, 5
2      js     signon        ; goto signon if SF = 1
3      jo     elseblock     ; goto elseblock if OF = 1 and SF = 0
4      jmp    thenblock     ; goto thenblock if SF = 0 and OF = 0
5 signon:
6      jo     thenblock     ; goto thenblock if SF = 1 and OF = 1
7 elseblock:
8      mov    ebx, 2
9      jmp    next
10 thenblock:
11     mov    ebx, 1
12 next:
```

Signed		Unsigned	
JE	branches if <code>vleft = vright</code>	JE	branches if <code>vleft = vright</code>
JNE	branches if <code>vleft ≠ vright</code>	JNE	branches if <code>vleft ≠ vright</code>
JL, JNGE	branches if <code>vleft < vright</code>	JB, JNAE	branches if <code>vleft < vright</code>
JLE, JNG	branches if <code>vleft ≤ vright</code>	JBE, JNA	branches if <code>vleft ≤ vright</code>
JG, JNLE	branches if <code>vleft > vright</code>	JA, JNBE	branches if <code>vleft > vright</code>
JGE, JNL	branches if <code>vleft ≥ vright</code>	JAE, JNA	branches if <code>vleft ≥ vright</code>

Table 2.4: Signed and Unsigned Comparison Instructions

The above code is very awkward. Fortunately, the 80x86 provides additional branch instructions to make these type of tests *much* easier. There are signed and unsigned versions of each. Table 2.4 shows these instructions. The equal and not equal branches (JE and JNE) are the same for both signed and unsigned integers. (In fact, JE and JNE are really identical to JZ and JNZ, respectively.) Each of the other branch instructions have two synonyms. For example, look at JL (jump less than) and JNGE (jump not greater than or equal to). These are the same instruction because:

$$x < y \implies \mathbf{not}(x \geq y)$$

The unsigned branches use A for *above* and B for *below* instead of L and G.

Using these new branch instructions, the pseudo-code above can be translated to assembly much easier.

```

1      cmp    eax, 5
2      jge    thenblock
3      mov    ebx, 2
4      jmp    next
5 thenblock:
6      mov    ebx, 1
7 next:
```

2.2.3 The loop instructions

The 80x86 provides several instructions designed to implement *for*-like loops. Each of these instructions takes a code label as its single operand.

LOOP Decrements ECX, if ECX ≠ 0, branches to label

LOOPE, LOOPZ Decrements ECX (FLAGS register is not modified), if ECX ≠ 0 and ZF = 1, branches

LOOPNE, LOOPNZ Decrements ECX (FLAGS unchanged), if ECX ≠ 0 and ZF = 0, branches

The last two loop instructions are useful for sequential search loops. The following pseudo-code:

```
sum = 0;
for( i=10; i >0; i-- )
    sum += i;
```

could be translated into assembly as:

```
1     mov    eax, 0           ; eax is sum
2     mov    ecx, 10         ; ecx is i
3 loop_start:
4     add    eax, ecx
5     loop  loop_start
```

2.3 Translating Standard Control Structures

This section looks at how the standard control structures of high level languages can be implemented in assembly language.

2.3.1 If statements

The following pseudo-code:

```
if ( condition )
    then_block;
else
    else_block ;
```

could be implemented as:

```
1     ; code to set FLAGS
2     jxx   else_block      ; select xx so that branches if condition false
3     ; code for then block
4     jmp   endif
5 else_block:
6     ; code for else block
7 endif:
```

If there is no else, then the `else_block` branch can be replaced by a branch to `endif`.

```
1     ; code to set FLAGS
2     jxx   endif          ; select xx so that branches if condition false
3     ; code for then block
4 endif:
```


2.3.2 While loops

The *while* loop is a top tested loop:

```
while( condition ) {
    body of loop;
}
```

This could be translated into:

```
1 while:
2     ; code to set FLAGS based on condition
3     jxx    endwhile    ; select xx so that branches if false
4     ; body of loop
5     jmp    while
6 endwhile:
```

2.3.3 Do while loops

The *do while* loop is a bottom tested loop:

```
do {
    body of loop;
} while( condition );
```

This could be translated into:

```
1 do:
2     ; body of loop
3     ; code to set FLAGS based on condition
4     jxx    do           ; select xx so that branches if true
```

2.4 Example: Finding Prime Numbers

This section looks at a program that finds prime numbers. Recall that prime numbers are evenly divisible by only 1 and themselves. There is no formula for doing this. The basic method this program uses is to find the factors of all odd numbers³ below a given limit. If no factor can be found for an odd number, it is prime. Figure 2.3 shows the basic algorithm written in C.

Here's the assembly version:

```
1 prime.asm
2 %include "asm_io.inc"
3 segment .data
4 Message db "Find primes up to: ", 0
```

³2 is the only even prime number.

```

1  unsigned guess;  /* current guess for prime */
2  unsigned factor; /* possible factor of guess */
3  unsigned limit;  /* find primes up to this value */
4
5  printf("Find primes up to: ");
6  scanf("%u", &limit);
7  printf("2\n");  /* treat first two primes as */
8  printf("3\n");  /* special case */
9  guess = 5;      /* initial guess */
10 while ( guess <= limit ) {
11     /* look for a factor of guess */
12     factor = 3;
13     while ( factor*factor < guess &&
14             guess % factor != 0 )
15         factor += 2;
16     if ( guess % factor != 0 )
17         printf("%d\n", guess);
18     guess += 2;  /* only look at odd numbers */
19 }

```

Figure 2.3:

```

4
5 segment .bss
6 Limit      resd    1          ; find primes up to this limit
7 Guess      resd    1          ; the current guess for prime
8
9 segment .text
10         global _asm_main
11 _asm_main:
12         enter 0,0          ; setup routine
13         pusha
14
15         mov    eax, Message
16         call   print_string
17         call   read_int      ; scanf("%u", & limit );
18         mov    [Limit], eax
19
20         mov    eax, 2          ; printf("2\n");
21         call   print_int
22         call   print_nl

```

```

23         mov     eax, 3                ; printf("3\n");
24         call    print_int
25         call    print_nl
26
27         mov     dword [Guess], 5      ; Guess = 5;
28 while_limit:                          ; while ( Guess <= Limit )
29         mov     eax, [Guess]
30         cmp     eax, [Limit]
31         jnbe   end_while_limit      ; use jnbe since numbers are unsigned
32
33         mov     ebx, 3                ; ebx is factor = 3;
34 while_factor:
35         mov     eax, ebx
36         mul     eax                    ; edx:eax = eax*eax
37         jo     end_while_factor      ; if answer won't fit in eax alone
38         cmp     eax, [Guess]
39         jnb    end_while_factor      ; if !(factor*factor < guess)
40         mov     eax, [Guess]
41         mov     edx, 0
42         div    ebx                    ; edx = edx:eax % ebx
43         cmp     edx, 0
44         je     end_while_factor      ; if !(guess % factor != 0)
45
46         add     ebx, 2                ; factor += 2;
47         jmp     while_factor
48 end_while_factor:
49         je     end_if                ; if !(guess % factor != 0)
50         mov     eax, [Guess]          ; printf("%u\n")
51         call    print_int
52         call    print_nl
53 end_if:
54         mov     eax, [Guess]
55         add     eax, 2
56         mov     [Guess], eax         ; guess += 2
57         jmp     while_limit
58 end_while_limit:
59
60         popa
61         mov     eax, 0                ; return back to C
62         leave
63         ret

```

prime.asm

Chapter 3

Bit Operations

3.1 Shift Operations

Assembly language allows the programmer to manipulate the individual bits of data. One common bit operation is called a *shift*. A shift operation moves the position of the bits of some data. Shifts can be either toward the left (*i.e.*, toward the most significant bits) or toward the right (the least significant bits).

3.1.1 Logical shifts

A logical shift is the simplest type of shift. It shifts in a very straightforward manner. Figure 3.1 shows an example of shifted a byte number.

Original	1	1	1	0	1	0	1	0
Left shifted	1	1	0	1	0	1	0	0
Right shifted	0	1	1	1	0	1	0	1

Figure 3.1: Logical shifts

Note that new, incoming bits are always zero. The **SHL** and **SHR** instructions are used to perform logical left and right shifts respectively. These instructions allow one to shift by any number of positions. The number of positions to shift can either be a constant or can be stored in the **CL** register. The last bit shifted out of the data is stored in the carry flag. Here are some code examples:

```
1      mov     ax, 0C123H
2      shl     ax, 1           ; shift 1 bit to left,   ax = 8246H, CF = 1
3      shr     ax, 1           ; shift 1 bit to right,  ax = 4123H, CF = 0
4      shr     ax, 1           ; shift 1 bit to right,  ax = 2091H, CF = 1
5      mov     ax, 0C123H
```

```

6      shl    ax, 2          ; shift 2 bits to left,  ax = 048CH, CF = 1
7      mov    cl, 3
8      shr    ax, cl        ; shift 3 bits to right, ax = 0091H, CF = 1

```

3.1.2 Use of shifts

Fast multiplication and division are the most common uses of a shift operations. Recall that in the decimal system, multiplication and division by a power of ten are simple, just shift digits. The same is true for powers of two in binary. For example, to double the binary number 1011_2 (or 11 in decimal), shift once to the left to get 10110_2 (or 22). The quotient of a division by a power of two is the result of a right shift. To divide by just 2, use a single right shift; to divide by 4 (2^2), shift right 2 places; to divide by 8 (2^3), shift 3 places to the right, *etc.* Shift instructions are very basic and are *much* faster than the corresponding MUL and DIV instructions!

Actually, logical shifts can be used multiply and divide unsigned values. They do not work in general for signed values. Consider the 2-byte value FFFF (signed -1). If it is logically right shifted once, the result is 7FFF which is $+32,767$! Another type of shift can be used for signed values.

3.1.3 Arithmetic shifts

These shifts are designed to be allow signed numbers to be quickly multiplied and divided by powers of 2. They insure that the sign bit is treated correctly.

SAL Shift Arithmetic Left - This instruction is just a synonym for SHL. It is assembled into the exactly the same machine code as SHL. As long as the sign bit is not changed by the shift, the result will be correct.

SAR Shift Arithmetic Right - This is a new instruction that does not shift the sign bit (*i.e.*, the msb) of its operand. The other bits are shifted as normal except that the new bits that enter from the left are copies of the sign bit (that is, if the sign bit is 1, the new bits are also 1). Thus, if a byte is shifted with this instruction, only the lower 7 bits are shifted. As for the other shifts, the last bit shifted out is stored in the carry flag.

```

1      mov    ax, 0C123H
2      sal    ax, 1          ; ax = 8246H, CF = 1
3      sal    ax, 1          ; ax = 048CH, CF = 1
4      sar    ax, 2          ; ax = 0123H, CF = 0

```

3.1.4 Rotate shifts

The rotate shift instructions work like logical shifts except that bits lost off one end of the data are shifted in on the other side. Thus, the data is treated as if it is a circular structure. The two simplest rotate instructions are ROL and ROR which make left and right rotations, respectively. Just as for the other shifts, these shifts leave the a copy of the last bit shifted around in the carry flag.

```

1      mov    ax, 0C123H
2      rol   ax, 1           ; ax = 8247H, CF = 1
3      rol   ax, 1           ; ax = 048FH, CF = 1
4      rol   ax, 1           ; ax = 091EH, CF = 0
5      ror   ax, 2           ; ax = 8247H, CF = 1
6      ror   ax, 1           ; ax = C123H, CF = 1

```

There are two additional rotate instructions that shift the bits in the data and the carry flag named RCL and RCR. For example, if the AX register is rotated with these instructions, the 17-bits made up of AX and the carry flag are rotated.

```

1      mov    ax, 0C123H
2      cld                    ; clear the carry flag (CF = 0)
3      rcl   ax, 1           ; ax = 8246H, CF = 1
4      rcl   ax, 1           ; ax = 048DH, CF = 1
5      rcl   ax, 1           ; ax = 091BH, CF = 0
6      rcr   ax, 2           ; ax = 8246H, CF = 1
7      rcr   ax, 1           ; ax = C123H, CF = 0

```

3.1.5 Simple application

Here is a code snippet that counts the number of bits that are “on” (*i.e.*, 1) in the EAX register.

```

1      mov    bl, 0           ; bl will contain the count of ON bits
2      mov    ecx, 32        ; ecx is the loop counter
3  count_loop:
4      shl   eax, 1          ; shift bit into carry flag
5      jnc   skip_inc       ; if CF == 0, goto skip_inc
6      inc   bl
7  skip_inc:
8      loop  count_loop

```

X	Y	X AND Y
0	0	0
0	1	0
1	0	0
1	1	1

Table 3.1: The AND operation

	1	0	1	0	1	0	1	0
AND	1	1	0	0	1	0	0	1
	1	0	0	0	1	0	0	0

Figure 3.2: ANDing a byte

The above code destroys the original value of `EAX` (`EAX` is zero at the end of the loop). If one wished to retain the value of `EAX`, line 4 could be replaced with `rol eax, 1`.

3.2 Boolean Bitwise Operations

There are four common boolean operators: *AND*, *OR*, *XOR* and *NOT*. A *truth table* shows the result of each operation for each possible value of its operands.

3.2.1 The *AND* operation

The result of the *AND* of two bits is only 1 if both bits are 1, else the result is 0 as the truth table in Table 3.1 shows.

Processors support these operations as instructions that act independently on all the bits of data in parallel. For example, if the contents of `AL` and `BL` are *AND*ed together, the basic *AND* operation is applied to each of the 8 pairs of corresponding bits in the two registers as Figure 3.2 shows. Below is a code example:

```

1      mov    ax, 0C123H
2      and    ax, 82F6H          ; ax = 8022H

```

3.2.2 The *OR* operation

The inclusive *OR* of 2 bits is 0 only if both bits are 0, else the result is 1 as the truth table in Table 3.2 shows. Below is a code example:

```

1      mov    ax, 0C123H
2      or     ax, 0E831H        ; ax = E933H

```


<i>X</i>	<i>Y</i>	<i>X OR Y</i>
0	0	0
0	1	1
1	0	1
1	1	1

Table 3.2: The OR operation

<i>X</i>	<i>Y</i>	<i>X XOR Y</i>
0	0	0
0	1	1
1	0	1
1	1	0

Table 3.3: The XOR operation

3.2.3 The *XOR* operation

The exclusive *OR* of 2 bits is 0 only if and only if both bits are equal, else the result is 1 as the truth table in Table 3.3 shows. Below is a code example:

```

1      mov    ax, 0C123H
2      xor    ax, 0E831H          ; ax = 2912H

```

3.2.4 The *NOT* operation

The *NOT* operation is a *unary* operation (*i.e.*, it acts on one operand, not two like *binary* operations such as *AND*). The *NOT* of a bit is the opposite value of the bit as the truth table in Table 3.4 shows. Below is a code example:

```

1      mov    ax, 0C123H
2      not   ax                ; ax = 3EDCH

```

Note that the *NOT* finds the one's complement. Unlike the other bitwise operations, the *NOT* instruction does not change any of the bits in the *FLAGS* register.

3.2.5 The *TEST* instruction

The *TEST* instruction performs an *AND* operation, but does not store the result. It only sets the *FLAGS* register based on what the result would be (much like how the *CMP* instruction performs a subtraction but only sets *FLAGS*). For example, if the result would be zero, *ZF* would be set.

X	NOT X
0	1
1	0

Table 3.4: The NOT operation

Turn on bit i	<i>OR</i> the number with 2^i (which is the binary number with just bit i on)
Turn off bit i	<i>AND</i> the number with the binary number with only bit i off. This operand is often called a <i>mask</i>
Complement bit i	<i>XOR</i> the number with 2^i

Table 3.5: Uses of boolean operations

3.2.6 Uses of boolean operations

Boolean operations are very useful for manipulating individual bits of data without modifying the other bits. Table 3.5 shows three common uses of these operations. Below is some example code, implementing these ideas.

```

1  mov    ax, 0C123H
2  or     ax, 8           ; turn on bit 3,   ax = C12BH
3  and   ax, 0FFDFH     ; turn off bit 5,  ax = C10BH
4  xor   ax, 8000H     ; invert bit 31,  ax = 410BH
5  or    ax, 0F00H     ; turn on nibble, ax = 4F0BH
6  and   ax, 0FFF0H    ; turn off nibble, ax = 4F00H
7  xor   ax, 0F00FH    ; invert nibbles, ax = BF0FH
8  xor   ax, 0FFFFH    ; 1's complement, ax = 40F0H

```

The *AND* operation can also be used to find the remainder of a division by a power of two. To find the remainder of a division by 2^i , *AND* the number with a mask equal to $2^i - 1$. This mask will contain ones from bit 0 up to bit $i - 1$. It is just these bits that contain the remainder. The result of the *AND* will keep these bits and zero out the others. Next is a snippet of code that finds the quotient and remainder of the division of 100 by 16.

```

1  mov    eax, 100      ; 100 = 64H
2  mov    ebx, 000000FH ; mask = 16 - 1 = 15 or F
3  and   ebx, eax      ; ebx = remainder = 4
4  shr   eax, 4        ; eax = quotient of eax/2^4 = 6

```

Using the CL register it is possible to modify arbitrary bits of data. Next is an example that sets (turns on) an arbitrary bit in EAX. The number of the bit to set is stored in BH.

```

1      mov    cl, bh          ; first build the number to OR with
2      mov    ebx, 1
3      shl   ebx, cl         ; shift left cl times
4      or    eax, ebx        ; turn on bit

```

Turning a bit off is just a little harder.

```

1      mov    cl, bh          ; first build the number to AND with
2      mov    ebx, 1
3      shl   ebx, cl         ; shift left cl times
4      not   ebx             ; invert bits
5      and   eax, ebx        ; turn off bit

```

Code to complement an arbitrary bit is left as an exercise for the reader.

It is not uncommon to see the following puzzling instruction in a 80x86 program:

```

xor    eax, eax            ; eax = 0

```

A number *XOR*'ed with itself always results in zero. This instruction is used because its machine code is smaller than the corresponding *MOV* instruction.

3.3 Manipulating bits in C

3.3.1 The bitwise operators of C

Unlike some high-level languages, C does provide operators for bitwise operations. The *AND* operation is represented by the binary `&` operator¹. The *OR* operation is represented by the binary `|` operator. The *XOR* operation is represented by the binary `^` operator. And the *NOT* operation is represented by the unary `~` operator.

The shift operations are performed by C's `<<` and `>>` binary operators. The `<<` operator performs left shifts and the `>>` operator performs right shifts. These operators take two operands. The left operand is the value to shift and the right operand is the number of bits to shift by. If the value to shift is an unsigned type, a logical shift is made. If the value is a signed type (like `int`), then an arithmetic shift is used. Below is some example C code using these operators:

```

1  short int s;          /* assume that short int is 16-bit */
2  short unsigned u;
3  s = -1;               /* s = 0xFFFF (2's complement) */
4  u = 100;              /* u = 0x0064 */
5  u = u | 0x0100;      /* u = 0x0164 */

```

¹This operator is different from the binary `&&` and unary `&` operators!

Macro	Meaning
S_IRUSR	user can read
S_IWUSR	user can write
S_IXUSR	user can execute
S_IRGRP	group can read
S_IWGRP	group can write
S_IXGRP	group can execute
S_IROTH	others can read
S_IWOTH	others can write
S_IXOTH	others can execute

Table 3.6: POSIX File Permission Macros

```

6 s = s & 0xFFF0;      /* s = 0xFFF0 */
7 s = s ^ u;          /* s = 0xFE94 */
8 u = u << 3;         /* u = 0x0B20 (logical shift) */
9 s = s >> 2;         /* s = 0xFFA5 (arithmetic shift) */

```

3.3.2 Using bitwise operators in C

The bitwise operators are used in C for the same purposes as they are used in assembly language. They allow one to manipulate individual bits of data and can be used for fast multiplication and division. In fact, a smart C compiler will use a shift for a multiplication like, `x *= 2`, automatically.

Many operating system API²'s (such as *POSIX*³ and Win32) contain functions which use operands that have data encoded as bits. For example, POSIX systems maintain file permissions for three different types of users: *user* (a better name would be *owner*), *group* and *others*. Each type of user can be granted permission to read, write and/or execute a file. To change the permissions of a file requires the C programmer to manipulate individual bits. POSIX defines several macros to help (see Table 3.6). The `chmod` function can be used to set the permissions of file. This function takes two parameters, a string with the name of the file to act on and an integer⁴ with the appropriate bits set for the desired permissions. For example, the code below sets the permissions to allow the owner of the file to read and write to it, users in the group to read the file and others have no access.

```
chmod("foo", S_IRUSR | S_IWUSR | S_IRGRP );
```

The POSIX `stat` function can be used to find out the current permission

²Application Programming Interface

³stands for Portable Operating System Interface for Computer Environments. A standard developed by the IEEE based on UNIX.

⁴Actually a parameter of type `mode_t` which is a typedef to an integral type.

bits for the file. Used with the `chmod` function, it is possible to modify some of the permissions without changing others. Here is an example that removes write access to others and adds read access to the owner of the file. The other permissions are not altered.

```

1 struct stat file_stats ; /* struct used by stat() */
2 stat("foo", & file_stats ); /* read file info.
3                               file_stats .st_mode holds permission bits */
4 chmod("foo", ( file_stats .st_mode & ~S_IWOTH) | S_IRUSR);

```

3.4 Counting Bits

Earlier a straightforward technique was given for counting the number of bits that are “on” in a double word. This section looks at other less direct methods of doing this as an exercise using the bit operations discussed in this chapter.

3.4.1 Method one

The first method is very simple, but not obvious. Here is the code for the function:

```

1 int count_bits ( unsigned int data )
2 {
3     int cnt = 0;
4
5     while( data != 0 ) {
6         data = data & (data - 1);
7         cnt++;
8     }
9     return cnt;
10 }

```

How does this method work? In every iteration of the loop, one bit is turned off in `data`. When all the bits are off (*i.e.*, when `data` is zero), the loop stops. The number of iterations required to make `data` zero is equal to the number of bits in the original value of `data`.

Line 6 is where a bit of `data` is turned off. How does this work? Consider the general form of the binary representation of `data` and the rightmost 1 in this representation. By definition, every bit after this 1 must be zero. Now, what will be the binary representation of `data - 1`? The bits to the left of the rightmost 1 will be the same as for `data`, but at the point of the rightmost 1 the bits will be the complement of the original bits of `data`. For example:

```

data      = xxxxx10000
data - 1  = xxxxx01111

```

```

1  static unsigned char byte_bit_count [256]; /* lookup table */
2
3  void initialize_count_bits ()
4  {
5      int cnt, i, data;
6
7      for( i = 0; i < 256; i++ ) {
8          cnt = 0;
9          data = i;
10         while( data != 0 ) {          /* method one */
11             data = data & (data - 1);
12             cnt++;
13         }
14         byte_bit_count [i] = cnt;
15     }
16 }
17
18 int count_bits ( unsigned int data )
19 {
20     const unsigned char * byte = ( unsigned char *) & data;
21
22     return byte_bit_count [byte [0]] + byte_bit_count [byte [1]] +
23         byte_bit_count [byte [2]] + byte_bit_count [byte [3]];
24 }

```

Figure 3.3: Method Two

where the *x*'s are the same for both numbers. When `data` is *AND*'ed with `data - 1`, the result will zero the rightmost 1 in `data` and leave all the other bits unchanged.

3.4.2 Method two

A lookup table can also be used to count the bits of an arbitrary double word. The straightforward approach would be to precompute the number of bits for each double word and store this in an array. However, there are two related problems with this approach. There are roughly *4 billion* double word values! This means that the array will be very big and that initializing it will also be very time consuming. (In fact, unless one is going to actually use the array more than 4 billion times, more time will be taken to initialize the array than it would require to just compute the bit counts using method one!)

A more realistic method would precompute the bit counts for all possible byte values and store these into an array. Then the double word can be split up into four byte values. The bit counts of these four byte values are looked up from the array and summed to find the bit count of the original double word. Figure 3.3 shows the code to implement this approach.

The `initialize_count_bits` function must be called before the first call to the `count_bits` function. This function initializes the global `byte_bit_count` array. The `count_bits` function looks at the `data` variable not as a double word, but as an array of four bytes. The `dword` pointer acts as a pointer to this four byte array. Thus, `dword[0]` is one of the bytes in `data` (either the least significant or the most significant byte depending on if the hardware is little or big endian, respectively.) Of course, one could use a construction like:

```
(data >> 24) & 0x000000FF
```

to find the most significant byte value and similar ones for the other bytes; however, these constructions will be slower than an array reference.

One last point, a `for` loop could easily be used to compute the sum on lines 22 and 23. But, a `for` loop would include the overhead of initializing a loop index, comparing the index after each iteration and incrementing the index. Computing the sum as the explicit sum of four values will be faster. In fact, a smart compiler would convert the `for` loop version to the explicit sum. This process of reducing or eliminating loop iterations is a compiler optimization technique known as *loop unrolling*.

3.4.3 Method Three

There is yet another clever method of counting the bits that are on in `data`. This method literally adds the one's and zero's of the `data` together. This sum must equal the number of one's in the `data`. For example, consider counting the one's in a byte stored in a variable named `data`. The first step is to perform the following operation:

```
data = (data & 0x55) + ((data >> 1) & 0x55);
```

What does this do? The hex constant `0x55` is `01010101` in binary. In the first operand of the addition, `data` is *AND*'ed with this, bits at the odd bit positions are pulled out. The second operand `((data >> 1) & 0x55)` first moves all the bits at the even positions to an odd position and uses the same mask to pull out these same bits. Now, the first operand contains the odd bits and the second operand contains the even bits of `data`. When these two operands are added together, the even and odd bits of `data` are added together. For example, if `data` is `101100112`, then:

$$\begin{array}{r} \text{data} \& \text{01010101}_2 \\ + (\text{data} \gg 1) \& \text{01010101}_2 \quad \text{or} \quad + \end{array} \begin{array}{|c|c|c|c|} \hline 00 & 01 & 00 & 01 \\ \hline 01 & 01 & 00 & 01 \\ \hline 01 & 10 & 00 & 10 \\ \hline \end{array}$$

```

1 int count_bits(unsigned int x )
2 {
3   static unsigned int mask[] = { 0x55555555,
4                                   0x33333333,
5                                   0x0F0F0F0F,
6                                   0x00FF00FF,
7                                   0x0000FFFF };
8   int i;
9   int shift ; /* number of positions to shift to right */
10
11  for( i=0, shift=1; i < 5; i++, shift *= 2 )
12    x = (x & mask[i]) + ( (x >> shift) & mask[i] );
13  return x;
14 }

```

Figure 3.4: Method 3

The addition on the right shows the actual bits added together. The bits of the byte are divided into four 2-bit fields to show that actually there are four independent additions being performed. Since the most these sums can be is two, there is no possibility that the sum will overflow its field and corrupt one of the other fields' sums.

Of course, the total number of bits have not been computed yet. However, the same technique that was used above can be used to compute the total in a series of similar steps. The next step would be:
`data = (data & 0x33) + ((data >> 2) & 0x33);`

Continuing the above example (remember that `data` now is 01100010_2):

$$\begin{array}{r}
 \text{data} \& 00110011_2 \\
 + (\text{data} \gg 2) \& 00110011_2 \\
 \hline
 \end{array}
 \quad \text{or} \quad
 \begin{array}{r}
 + \begin{array}{|c|c|} \hline 0010 & 0010 \\ \hline 0001 & 0000 \\ \hline 0011 & 0010 \\ \hline \end{array}
 \end{array}$$

Now there are two 4-bit fields to that are independently added.

The next step is to add these two bit sums together to form the final result:

`data = (data & 0x0F) + ((data >> 4) & 0x0F);`

Using the example above (with `data` equal to 00110010_2):

$$\begin{array}{r}
 \text{data} \& 00001111_2 \\
 + (\text{data} \gg 4) \& 00001111_2 \\
 \hline
 \end{array}
 \quad \text{or} \quad
 \begin{array}{r}
 + \begin{array}{|c|} \hline 00000010 \\ \hline 00000011 \\ \hline 00000101 \\ \hline \end{array}
 \end{array}$$

Now `data` is 5 which is the correct result. Figure 3.4 shows an implementation of this method that counts the bits in a double word. It uses a `for` loop to compute the sum. It would be faster to unroll the loop; however, the

loop makes it clearer how the method generalizes to different sizes of data.

Chapter 4

Subprograms

This chapter looks at using subprograms to make modular programs and to interface with high level languages (like C). Functions and procedures are high level language examples of subprograms.

The code that calls a subprogram and the subprogram itself must agree on how data will be passed between them. These rules on how data will be passed are called *calling conventions*. A large part of this chapter will deal with the standard C calling conventions that can be used to interface assembly subprograms with C programs. This (and other conventions) often pass the addresses of data (*i.e.*, pointers) to allow the subprogram to access the data in memory.

4.1 Indirect Addressing

Indirect addressing allows registers to act like pointer variables. To indicate that a register is to be used indirectly as a pointer, it is enclosed in square brackets (`[]`). For example:

```
1      mov    ax, [Data]      ; normal direct memory addressing of a word
2      mov    ebx, Data      ; ebx = & Data
3      mov    ax, [ebx]      ; ax = *ebx
```

Because AX holds a word, line 3 reads a word starting at the address stored in EBX. If AX was replaced with AL, only a single byte would be read. It is important to realize that registers do not have types like variables do in C. What EBX is assumed to point to is completely determined to what instructions are used. Furthermore, even the fact that EBX is a pointer is completely determined by the what instructions are used. If EBX is used incorrectly, often there will be no assembler error; however, the program will not work correctly. This is one of the many reasons that assembly programming is more error prone than high level programming.

All the 32-bit general purpose (EAX, EBX, ECX, EDX) and index (ESI, EDI) registers can be used for indirect addressing. In general, the 16-bit and 8-bit registers can not be.

4.2 Simple Subprogram Example

A subprogram is an independent unit of code that can be used from different parts of a program. In other words, a subprogram is like a function in C. A jump can be used to invoke the subprogram, but returning presents a problem. If the subprogram is to be used by different parts of the program, it must return back to the section of code that invoked it. Thus, the jump back from the subprogram can not be hard coded to a label. The code below shows how this could be done using the indirect form of the JMP instruction. This form of the instruction uses the value of a register to determine where to jump to (thus, the register acts much like a *function pointer* in C.) Here is the first program from chapter 1 rewritten to use a subprogram.

```

_____ sub1.asm _____
1 ; file: sub1.asm
2 ; Subprogram example program
3 %include "asm_io.inc"
4
5 segment .data
6 prompt1 db "Enter a number: ", 0 ; don't forget nul terminator
7 prompt2 db "Enter another number: ", 0
8 outmsg1 db "You entered ", 0
9 outmsg2 db " and ", 0
10 outmsg3 db ", the sum of these is ", 0
11
12 segment .bss
13 input1 resd 1
14 input2 resd 1
15
16 segment .text
17     global _asm_main
18 _asm_main:
19     enter 0,0 ; setup routine
20     pusha
21
22     mov eax, prompt1 ; print out prompt
23     call print_string
24
25     mov ebx, input1 ; store address of input1 into ebx

```

```

26         mov     ecx, ret1         ; store return address into ecx
27         jmp     short get_int     ; read integer
28 ret1:
29         mov     eax, prompt2      ; print out prompt
30         call    print_string
31
32         mov     ebx, input2
33         mov     ecx, $ + 7        ; ecx = this address + 7
34         jmp     short get_int
35
36         mov     eax, [input1]     ; eax = dword at input1
37         add     eax, [input2]     ; eax += dword at input2
38         mov     ebx, eax          ; ebx = eax
39
40         mov     eax, outmsg1
41         call    print_string      ; print out first message
42         mov     eax, [input1]
43         call    print_int         ; print out input1
44         mov     eax, outmsg2
45         call    print_string      ; print out second message
46         mov     eax, [input2]
47         call    print_int         ; print out input2
48         mov     eax, outmsg3
49         call    print_string      ; print out third message
50         mov     eax, ebx
51         call    print_int         ; print out sum (ebx)
52         call    print_nl         ; print new-line
53
54         popa
55         mov     eax, 0             ; return back to C
56         leave
57         ret
58 ; subprogram get_int
59 ; Parameters:
60 ;   ebx - address of dword to store integer into
61 ;   ecx - address of instruction to return to
62 ; Notes:
63 ;   value of eax is destroyed
64 get_int:
65         call    read_int
66         mov     [ebx], eax        ; store input into memory
67         jmp     ecx              ; jump back to caller

```

The `get_int` subprogram uses a simple, register-based calling convention. It expects the `EBX` register to hold the address of the `DWORD` to store the number input into and the `ECX` register to hold the code address of the instruction to jump back to. In lines 25 to 28, the `ret1` label is used to compute this return address. In lines 32 to 34, the `$` operator is used to compute the return address. The `$` operator returns the current address for the line it appears on. The expression `$ + 7` computes the address of the `MOV` instruction on line 36.

Both of these return address computations are awkward. The first method requires a label to be defined for each subprogram call. The second method does not require a label, but does require careful thought. If a near jump was used instead of a short jump, the number to add to `$` would not be 7! Fortunately, there is a much simpler way to invoke subprograms. This method uses the *stack*.

4.3 The Stack

Many CPU's have built in support of a stack. A stack is a Last-In First-Out (*LIFO*) list. The stack is an area of memory that is organized in this fashion. The `PUSH` instruction adds data to the stack and the `POP` instruction removes data. The data removed is always the last data added (that is why it is called a last-in first-out list).

The `SS` segment register specifies the segment that contains the stack (usually this is the same segment data is stored into). The `ESP` register contains the address of the data that would be removed from the stack. This data is said to be at the *top* of the stack. Data can only be added in double word units. That is, one can not push a single byte on the stack.

The `PUSH` instruction inserts a double word¹ on the stack by subtracting 4 from `ESP` and then stores the double word at `[ESP]`. The `POP` instruction reads the double word at `[ESP]` and then adds 4 to `ESP`. The code below demonstrates how these instructions work and assumes that `ESP` is initially 1000H.

```

1      push    dword 1      ; 1 stored at 0FFCh, ESP = 0FFCh
2      push    dword 2      ; 2 stored at 0FF8h, ESP = 0FF8h
3      push    dword 3      ; 3 stored at 0FF4h, ESP = 0FF4h
4      pop     eax          ; EAX = 3, ESP = 0FF8h
5      pop     ebx          ; EBX = 2, ESP = 0FFCh
6      pop     ecx          ; ECX = 1, ESP = 1000h

```

¹Actually words can be pushed too, but in 32-bit protected mode, it is better to work with only double words on the stack.

The stack can be used as a convenient place to store data temporarily. It is also used for making subprogram calls, passing parameters and local variables.

The 80x86 also provides a `PUSHA` instruction that pushes the values of `EAX`, `EBX`, `ECX`, `EDX`, `ESI`, `EDI` and `EBP` registers (not in this order). The `POPA` instruction can be used to pop them all back off.

4.4 The CALL and RET Instructions

The 80x86 provides two instructions that use the stack to make calling subprograms quick and easy. The `CALL` instruction makes an unconditional jump to a subprogram and *pushes* the address of the next instruction on the stack. The `RET` instruction *pops off* an address and jumps to that address. When using these instructions, it is very important that one manage the stack correctly so that the right number is popped off by the `RET` instruction!

The previous program can be rewritten to use these new instructions by changing lines 25 to 34 to be:

```

mov    ebx, input1
call   get_int

mov    ebx, input2
call   get_int

```

and change the subprogram `get_int` to:

```

get_int:
    call read_int
    mov  [ebx], eax
    ret

```

There are several advantages to using `CALL` and `RET`:

- It is simpler!
- It allows subprogram calls to be nested easily. Notice that `get_int` calls `read_int`. This call pushes another address on the stack. At the end of `read_int`'s code is a `RET` that pops off the return address and jumps back to `get_int`'s code. Then when `get_int`'s `RET` is executed, it pops off the return address that jumps back to `asm_main`. This works correctly because of the LIFO property of the stack.

Remember it is *very* important to pop off all data that is pushed on the stack. For example, consider the following:

```

1  get_int:
2      call    read_int
3      mov     [ebx], eax
4      push   eax
5      ret                    ; pops off EAX value, not return address!!

```

This code would not return correctly!

4.5 Calling Conventions

When a subprogram is invoked, the calling code and the subprogram (the *callee*) must agree on how to pass data between them. High-level languages have standard ways to pass data known as *calling conventions*. For high-level code to interface with assembly language, the assembly language code must use the same conventions as the high-level language. The calling conventions can differ from compiler to compiler or may vary depending on how the code is compiled (*e.g.*, if optimizations are on or not). One universal convention is that the code will be invoked with a `CALL` instruction and return via a `RET`.

All PC C compilers support one calling convention that will be described in the rest of this chapter in stages. One property of these conventions are that subprograms are *reentrant*. A reentrant subprogram may be called at any point of a program safely (even inside the subprogram itself).

4.5.1 Passing parameters on the stack

Parameters to a subprogram may be passed on the stack. They are pushed onto the stack before the `CALL` instruction. Just as in C, if the parameter is to be changed by the subprogram, the *address* of the data must be passed, not the *value*. If the parameter's size is less than a double word, it must be converted to a double word before being pushed.

The parameters on the stack are not popped off by the subprogram, instead they are access in the stack itself. Why?

- Since they have to pushed on the stack before the `CALL` instruction, the return address would have to be popped off first (and then pushed back on again).
- Often the parameters will have to be used in several places in the subprogram. Usually, they can not be kept in a register for the entire subprogram and would have to be stored in memory. Leaving them

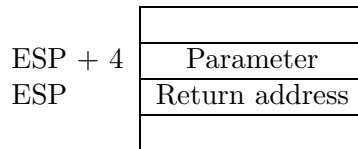


Figure 4.1:

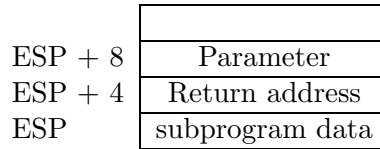


Figure 4.2:

on the stack keeps a copy of the data in memory that can be accessed at any point of the subprogram.

Consider a subprogram that is passed a single parameter on the stack. When the subprogram is invoked, the stack looks like Figure 4.1. The parameter can be accessed using indirect addressing ($[\text{ESP}+4]$ ²).

If the stack is also used inside the subprogram to store data, the number needed to be added to ESP will change. For example, Figure 4.2 shows what the stack looks like if a DWORD is pushed the stack. Now the parameter is at $\text{ESP} + 8$ not $\text{ESP} + 4$. Thus, it can be very error prone to use ESP when referencing parameters. To solve this problem, the 80386 supplies another register to use: EBP. This register's only purpose is to reference data on the stack. The C calling convention mandates that a subprogram first save the value of EBP on the stack and then set EBP to be equal to ESP. This allows ESP to change as data is pushed or popped off the stack without modifying EBP. At the end of the subprogram, the original value of EBP must be restored (this is why it is saved at the start of the subprogram.) Figure 4.3 shows the general form of a subprogram that follows these conventions.

Lines 2 and 3 in Figure 4.3 make up the general *prologue* of a subprogram. Lines 5 and 6 make up the *epilogue*. Figure 4.4 shows what the stack looks like immediately after the prologue. Now the parameter can be access with $[\text{EBP} + 8]$ at any place in the subprogram without worrying about what else has been pushed onto the stack by the subprogram.

After the subprogram is over, the parameters that were pushed on the stack must be removed. The C calling convention specifies that the caller code must do this. Other conventions are different. For example, the Pascal calling convention specifies that the subprogram must remove the parame-

When using indirect addressing, the 80x86 processor accesses different segments depending on what registers are used in the indirect addressing expression. ESP (and EBP) use the stack segment while EAX, EBX, ECX and EDX use the data segment. However, this is usually unimportant for most protected mode programs, because for them the data and stack segments are the same.

²It is legal to add a constant to a register when using indirect addressing. More complicated expressions are possible too. This is covered in the next chapter

```

1 subprogram_label:
2     push    ebp           ; save original EBP value on stack
3     mov     ebp, esp      ; new EBP = ESP
4 ; subprogram code
5     pop     ebp           ; restore original EBP value
6     ret

```

Figure 4.3: General subprogram form

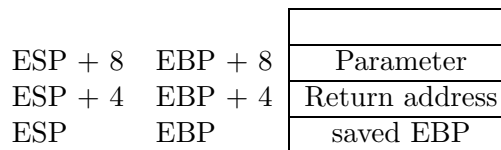


Figure 4.4:

ters. (There is another form of the RET instruction that makes this easy to do.) Some C compilers support this convention too. The `pascal` keyword is used in the prototype and definition of the function to tell the compiler to use this convention. In fact, MS Windows API C functions use the Pascal convention. Why? It is a little more efficient than the C convention. Why do all C functions not use this convention, then? In general, C allows a function to have varying number of arguments (*e.g.*, the `printf` and `scanf` functions). For these types of functions, the operation to remove the parameters from the stack will vary from one call of the function to the next. The C convention allows the instructions to perform this operation to be easily varied from one call to the next. The Pascal convention makes this operation very difficult. Thus, the Pascal convention (like the Pascal language) does not allow this type of function. MS Windows can use this convention since none of its API functions take varying numbers of arguments.

Figure 4.5 shows how a subprogram using the C calling convention would be called. Line 3 removes the parameter from the stack by directly manipulating the stack pointer. A POP instruction could be used to do this also, but would require the useless result to be stored in a register. Actually, for this particular case, many compilers would use a POP ECX instruction to remove the parameter. The compiler would use a POP instead of an ADD because the ADD requires more bytes for the instruction. However, the POP also changes ECX's value! Next is another example program with two subprograms that use the C calling conventions discussed above. Line 54 (and other lines) shows that multiple data and text segments may be declared in a single source file. They will be combined into single data and text segments in

1	push	dword 1	; pass 1 as parameter
2	call	fun	
3	add	esp, 4	; remove parameter from stack

Figure 4.5: Sample subprogram call

the linking process. Splitting up the data and code into separate segments allow the data that a subprogram uses to be defined close by the code of the subprogram.

```

sub3.asm
1  %include "asm_io.inc"
2
3  segment .data
4  sum    dd    0
5
6  segment .bss
7  input  resd 1
8
9  ;
10 ; psuedo-code algorithm
11 ; i = 1;
12 ; sum = 0;
13 ; while( get_int(i, &input), input != 0 ) {
14 ;   sum += input;
15 ;   i++;
16 ; }
17 ; print_sum(num);
18 segment .text
19     global  _asm_main
20 _asm_main:
21     enter  0,0          ; setup routine
22     pusha
23
24     mov    edx, 1      ; edx is 'i' in pseudo-code
25 while_loop:
26     push  edx          ; save i on stack
27     push  dword input  ; push address on input on stack
28     call  get_int
29     add   esp, 8       ; remove i and &input from stack
30

```

```

31     mov     eax, [input]
32     cmp     eax, 0
33     je      end_while
34
35     add     [sum], eax      ; sum += input
36
37     inc     edx
38     jmp     short while_loop
39
40 end_while:
41     push   dword [sum]      ; push value of sum onto stack
42     call   print_sum
43     pop    ecx              ; remove [sum] from stack
44
45     popa
46     leave
47     ret
48
49 ; subprogram get_int
50 ; Parameters (in order pushed on stack)
51 ;   number of input (at [ebp + 12])
52 ;   address of word to store input into (at [ebp + 8])
53 ; Notes:
54 ;   values of eax and ebx are destroyed
55 segment .data
56 prompt db      ") Enter an integer number (0 to quit): ", 0
57
58 segment .text
59 get_int:
60     push   ebp
61     mov    ebp, esp
62
63     mov    eax, [ebp + 12]
64     call   print_int
65
66     mov    eax, prompt
67     call   print_string
68
69     call   read_int
70     mov    ebx, [ebp + 8]
71     mov    [ebx], eax      ; store input into memory
72

```

```

73         pop     ebp
74         ret                ; jump back to caller
75
76 ; subprogram print_sum
77 ; prints out the sum
78 ; Parameter:
79 ;   sum to print out (at [ebp+8])
80 ; Note: destroys value of eax
81 ;
82 segment .data
83 result db     "The sum is ", 0
84
85 segment .text
86 print_sum:
87         push   ebp
88         mov    ebp, esp
89
90         mov    eax, result
91         call   print_string
92
93         mov    eax, [ebp+8]
94         call   print_int
95         call   print_nl
96
97         pop    ebp
98         ret

```

sub3.asm

4.5.2 Local variables on the stack

The stack can be used as a convenient location for local variables. This is exactly where C stores normal (or *automatic* in C lingo) variables. Using the stack for variables is important if one wishes subprograms to be reentrant. A reentrant subprogram will work if it is invoked at any place, including the subprogram itself. In other words, reentrant subprograms can be invoked *recursively*. Using the stack for variables also saves memory. Data not stored on the stack is using memory from the beginning of the program until the end of the program (C calls these types of variables *global* or *static*). Data stored on the stack only use memory when the subprogram they are defined for is active.

Local variables are stored right after the saved EBP value in the stack. They are allocated by subtracting the number of bytes required from ESP in the prologue of the subprogram. Figure 4.6 shows the new subprogram

```

1 subprogram_label:
2     push    ebp                ; save original EBP value on stack
3     mov     ebp, esp          ; new EBP = ESP
4     sub     esp, LOCAL_BYTES  ; = # bytes needed by locals
5 ; subprogram code
6     mov     esp, ebp          ; deallocate locals
7     pop     ebp                ; restore original EBP value
8     ret

```

Figure 4.6: General subprogram form with local variables

```

1 void calc_sum( int n, int * sump )
2 {
3     int i, sum = 0;
4
5     for( i=1; i <= n; i++ )
6         sum += i;
7     *sump = sum;
8 }

```

Figure 4.7: C version of sum

skeleton. The EBP register is used to access local variables. Consider the C function in Figure 4.7. Figure 4.8 shows how the equivalent subprogram could be written in assembly.

Figure 4.9 shows what the stack looks like after the prologue of the program in Figure 4.8. This combination of the parameters return information and local variables used by a single subprogram call is called a *stack frame*. Every invocation of a C function creates a new stack frame on the stack.

The prologue and epilogue of a subprogram can be simplified by using two special instructions that are designed specifically for this purpose. The `ENTER` instruction performs the prologue code and the `LEAVE` performs the epilogue. The `ENTER` instruction takes two immediate operands. For the C calling convention, the second operand is always 0. The first operand is the number bytes needed by local variables. The `LEAVE` instruction has no operands. Figure 4.10 shows how this instructions are used. Note that the program skeleton (Figure 1.7) also uses `ENTER` and `LEAVE`.

```

1 cal_sum:
2     push    ebp
3     mov     ebp, esp
4     sub     esp, 4           ; make room for local sum
5
6     mov     dword [ebp - 4], 0 ; sum = 0
7     mov     ebx, 1           ; ebx (i) = 1
8 for_loop:
9     cmp     ebx, [ebp+12]    ; is i >= n?
10    jnle    end_for
11
12    add     [ebp-4], ebx      ; sum += i
13    inc     ebx
14    jmp     short for_loop
15
16 end_for:
17    mov     ebx, [ebp+8]     ; ebx = sump
18    mov     eax, [ebp-4]     ; eax = sum
19    mov     [ebx], eax       ; *sump = sum;
20
21    mov     esp, ebp
22    pop     ebp
23    ret

```

Figure 4.8: Assembly version of sum

4.6 Multi-Module Programs

A *multi-module program* is one composed of more than one object file. All the programs presented here have been multi-module programs. They consisted of the C driver object file and the assembly object file (plus the C library object files). Recall that the linker combines the object files into a single executable program. The linker must match up references made to each label in one module (*i.e.*, object file) to its definition in another module. In order for module A to use a label defined in module B, the **extern** directive must be used. After the **extern** directive comes a comma delimited list of labels. The directive tells the assembler to treat these labels as *external* to the module. That is, these are labels that can be used in this module, but are defined in another. The `asm_io.inc` file defines the `read_int`, *etc.* routines as external.

In assembly, labels can not be accessed externally by default. If a label

ESP + 16	EBP + 12	n
ESP + 12	EBP + 8	sump
ESP + 8	EBP + 4	Return address
ESP + 4	EBP	saved EBP
ESP	EBP - 4	sum

Figure 4.9:

```

1 subprogram_label:
2     enter  LOCAL_BYTES, 0      ; = # bytes needed by locals
3 ; subprogram code
4     leave
5     ret

```

Figure 4.10: General subprogram form with local variables using ENTER and LEAVE

can be accessed from other modules than the one it is defined in, it must be declared *global* in its module. The `global` directive does this. Line 13 of the skeleton program listing in Figure 1.7 shows the `_asm_main` label being defined as global. Without this declaration, there would be a linker error. Why? Because the C code would not be able to refer to the *internal* `_asm_main` label.

Next is the code for the previous example, rewritten to use two modules. The two subprograms (`get_int` and `print_sum`) are in a separate source file than the `_asm_main` routine.

```

----- main4.asm -----
1 %include "asm_io.inc"
2
3 segment .data
4 sum     dd  0
5
6 segment .bss
7 input   resd 1
8
9 segment .text
10        global  _asm_main
11        extern  get_int, print_sum
12 _asm_main:
13        enter   0,0           ; setup routine
14        pusha

```



```

15
16     mov     edx, 1           ; edx is 'i' in pseudo-code
17 while_loop:
18     push   edx             ; save i on stack
19     push   dword input     ; push address on input on stack
20     call   get_int
21     add    esp, 8          ; remove i and &input from stack
22
23     mov    eax, [input]
24     cmp    eax, 0
25     je     end_while
26
27     add    [sum], eax      ; sum += input
28
29     inc    edx
30     jmp   short while_loop
31
32 end_while:
33     push   dword [sum]     ; push value of sum onto stack
34     call   print_sum
35     pop    ecx            ; remove [sum] from stack
36
37     popa
38     leave
39     ret

```

main4.asm

sub4.asm

```

1  %include "asm_io.inc"
2
3  segment .data
4  prompt db      ") Enter an integer number (0 to quit): ", 0
5
6  segment .text
7      global  get_int, print_sum
8  get_int:
9      enter  0,0
10
11     mov    eax, [ebp + 12]
12     call   print_int
13
14     mov    eax, prompt
15     call   print_string
16

```

```

17         call    read_int
18         mov     ebx, [ebp + 8]
19         mov     [ebx], eax           ; store input into memory
20
21         leave
22         ret                          ; jump back to caller
23
24 segment .data
25 result db    "The sum is ", 0
26
27 segment .text
28 print_sum:
29         enter  0,0
30
31         mov     eax, result
32         call   print_string
33
34         mov     eax, [ebp+8]
35         call   print_int
36         call   print_nl
37
38         leave
39         ret

```

sub4.asm

The previous example only has global code labels; however, global data labels work exactly the same way.

4.7 Interfacing Assembly with C

Today, very few programs are written completely in assembly. Compilers are very good at converting high level code into efficient machine code. Since it is much easier to write code in a high level language, it is more popular. In addition, high level code is *much* more portable than assembly!

When assembly is used, it is often only used for small parts of the code. This can be done in two ways: calling assembly subroutines from C or inline assembly. Inline assembly allows the programmer to place assembly statements directly into C code. This can be very convenient; however, there are disadvantages to inline assembly. The assembly code must be written in the format the compiler uses. No compiler at the moment supports NASM's format. Different compilers require different formats. Borland and Microsoft require MASM format. DJGPP and Linux's gcc require GAS³ format. The

³GAS is the assembler that all GNU compiler's use. It uses the AT&T syntax which

```

1 segment .data
2 x          dd      0
3 format     db      "x = %d\n", 0
4
5 segment .text
6 ...
7     push   dword [x]      ; push x's value
8     push   dword format   ; push address of format string
9     call   _printf       ; note underscore!
10    add    esp, 8         ; remove parameters from stack

```

Figure 4.11: Call to printf

technique of calling an assembly subroutine is much more standardized on the PC.

Assembly routines are usually used with C for the following reasons:

- Direct access is needed to hardware features of the computer that are difficult or impossible to access from C.
- The routine must be as fast as possible and the programmer can hand optimize the code better than the compiler can.

The last reason is not as valid as it once was. Compiler technology has improved over the years and compilers can often generate very efficient code (especially if compiler optimizations are turned on). The disadvantages of assembly routines are: reduced portability and readability.

Most of the C calling conventions have already been specified. However, there are a few additional features that need to be described.

4.7.1 Saving registers

First, C assumes that a subroutine maintains the values of the following registers: EBX, ESI, EDI, EBP, CS, DS, SS, ES. This does not mean that the subroutine can not change them internally. Instead, it means that if it does change their values, it must restore their original values before the subroutine returns. The EBX, ESI and EDI values must be unmodified because C uses these registers for *register variables*. Usually the stack is used to save the original values of these registers.

is very different from the relatively similar syntaxes of MASM, TASM and NASM.

*The **register** keyword can be used in a C variable declaration to suggest to the compiler that it use a register for this variable instead of a memory location. These are known as register variables. Modern compilers do this automatically without requiring any suggestions.*

EBP + 12	value of <code>x</code>
EBP + 8	address of format string
EBP + 4	Return address
EBP	saved EBP

Figure 4.12: Stack inside `printf`

4.7.2 Labels of functions

Most C compilers prepend a single underscore(`_`) character at the beginning of the names of functions and global/static variables. For example, a function named `f` will be assigned the label `_f`. Thus, if this is to be an assembly routine, it *must* be labelled `_f`, not `f`. The Linux gcc compiler does *not* prepend any character. Under Linux ELF executables, one simply would use the label `f` for the C function `f`. However, DJGPP's gcc does prepend an underscore. Note that in the assembly skeleton program (Figure 1.7), the label for the main routine is `_asm_main`.

4.7.3 Passing parameters

Under the C calling convention, the arguments of a function are pushed on the stack in the *reverse* order that they appear in the function call.

Consider the following C statement: `printf("x = %d\n", x)`; Figure 4.11 shows how this would be compiled (shown in the equivalent NASM format). Figure 4.12 shows what the stack looks like after the prologue inside the `printf` function. The `printf` function is one of the C library functions that can take any number of arguments. The rules of the C calling conventions were specifically written to allow these types of functions. Since the address of the format string is pushed last, it's location on the stack will *always* be at `EBP + 8` not matter how many parameters are passed to the function. The `printf` code can then look at the format string to determine how many parameters should have been passed and look for them on the stack.

Of course, if a mistake is made, `printf("x = %d\n")`, the `printf` code will still print out the double word value at `[EBP + 12]`. However, this will not be `x`'s value!

4.7.4 Calculating addresses of local variables

Finding the address of a label defined in the `data` or `bss` segments is simple. Basically, the linker does this. However, calculating the address of a local variable (or parameter) on the stack is not as straightforward. However, this is a very common need when calling subroutines. Consider the case of passing the address of a variable (let's call it `x`) to a function

It is not necessary to use assembly to process an arbitrary number of arguments in C. The `stdarg.h` header file defines macros that can be used to process them portably. See any good C book for details.

(let's call it `foo`). If `x` is located at `EBP - 8` on the stack, one cannot just use:

```
mov    eax, ebp - 8
```

Why? The value that `MOV` stores into `EAX` must be computed by the assembler (that is, it must in the end be a constant). However, there is an instruction that does the desired calculation. It is called `LEA` (for *Load Effective Address*). The following would calculate the address of `x` and store it into `EAX`:

```
lea    eax, [ebp - 8]
```

Now `EAX` holds the address of `x` and could be pushed on the stack when calling function `foo`. Do not be confused, it looks like this instruction is reading the data at `[EBP-8]`; however, this is *not* true. The `LEA` instruction *never* reads memory! It only computes the address that would be read by another instruction and stores this address in its first register operand. Since it does not actually read any memory, no memory size designation (*e.g.* `dword`) is needed or allowed.

4.7.5 Returning values

Non-void C functions return back a value. The C calling conventions specify how this is done. Return values are passed via registers. All integral types (`char`, `int`, `enum`, *etc.*) are returned in the `EAX` register. If they are smaller than 32-bits, they are extended to 32-bits when stored in `EAX`. (How they are extended depends on if they are signed or unsigned types.) Pointer values are also stored in `EAX`. Floating point values are stored in the `ST0` register of the math coprocessor. (This register is discussed in the floating point chapter.)

4.7.6 Other calling conventions

The rules described above describe the standard C calling convention that is supported by all 80x86 C compilers. Often compilers support other calling conventions as well. When interfacing with assembly language it is *very* important to know what calling convention the compiler is using when it calls your function. Usually, the default is to use the standard calling convention; however, this is not always the case⁴. Compilers that use multiple conventions often have command line switches that can be used to change the default convention. They also provide extensions to the C syntax

⁴The Watcom C compiler is an example of one that does *not* use the standard convention by default.

to explicitly assign calling conventions to individual functions. However, these extensions are not standardized and may vary from one compiler to another.

The GCC compiler allows different calling conventions. The convention of a function can be explicitly declared by using the `__attribute__` extension. For example, to declare a void function that uses the standard calling convention named `f` that takes a single `int` parameter, use the following syntax for its prototype:

```
void f( int ) __attribute__((cdecl));
```

GCC also supports the *standard call* calling convention. The function above could be declared to use this convention by replacing the `cdecl` with `stdcall`. The difference in `stdcall` and `cdecl` is that `stdcall` requires the subroutine to remove the parameters from the stack (as the Pascal calling convention does). Thus, the `stdcall` convention can only be used with functions that take a fixed number of arguments (*i.e.*, ones not like `printf` and `scanf`).

GCC also supports an additional attribute called `regparm` that tells the compiler to use registers to pass up to 3 integer arguments to a function instead of using the stack. This is a common type of optimization that many compilers support.

Borland and Microsoft use a common syntax to declare calling conventions. They add the `__cdecl` and `__stdcall` keywords to C. These keywords act as function modifiers and appear immediately before the function name in a prototype. For example, the function `f` above would be defined as follows for Borland and Microsoft:

```
void __cdecl f( int );
```

There are advantages and disadvantages to each of the calling conventions. The main advantages of the `cdecl` convention is that it is simple and very flexible. It can be used for any type of C function and C compiler. Using other conventions can limit the portability of the subroutine. Its main disadvantage is that it can be slower than some of the others and use more memory (since every invocation of the function requires code to remove the parameters on the stack).

The advantages of the `stdcall` convention is that it uses less memory than `cdecl`. No stack cleanup is required after the `CALL` instruction. Its main disadvantage is that it can not be used with functions that have variable numbers of arguments.

The advantage of using a convention that uses registers to pass integer parameters is speed. The main disadvantage is that the convention is more complex. Some parameters may be in registers and others on the stack.

4.7.7 Examples

Next is an example that shows how an assembly routine can be interfaced to a C program. (Note that this program does not use the assembly skeleton program (Figure 1.7) or the driver.c module.)

```

_____ main5.c _____
1 #include <stdio.h>
2 /* prototype for assembly routine */
3 void calc_sum( int , int * ) __attribute__((cdecl));
4
5 int main( void )
6 {
7     int n, sum;
8
9     printf("Sum integers up to: ");
10    scanf("%d", &n);
11    calc_sum(n, &sum);
12    printf("Sum is %d\n", sum);
13    return 0;
14 }

_____ main5.c _____

_____ sub5.asm _____
1 ; subroutine _calc_sum
2 ; finds the sum of the integers 1 through n
3 ; Parameters:
4 ;   n    - what to sum up to (at [ebp + 8])
5 ;   sump - pointer to int to store sum into (at [ebp + 12])
6 ; pseudo C code:
7 ; void calc_sum( int n, int * sump )
8 ; {
9 ;   int i, sum = 0;
10 ;   for( i=1; i <= n; i++ )
11 ;       sum += i;
12 ;   *sump = sum;
13 ; }
14
15 segment .text
16     global _calc_sum
17 ;
18 ; local variable:

```

```

Sum integers up to: 10
Stack Dump # 1
EBP = BFFFFB70 ESP = BFFFFB68
+16 BFFFFB80 080499EC
+12 BFFFFB7C BFFFFB80
+8  BFFFFB78 0000000A
+4  BFFFFB74 08048501
+0  BFFFFB70 BFFFFB88
-4  BFFFFB6C 00000000
-8  BFFFFB68 4010648C
Sum is 55

```

Figure 4.13: Sample run of sub5 program

```

19 ; sum at [ebp-4]
20 _calc_sum:
21     enter    4,0           ; make room for sum on stack
22     push    ebx           ; IMPORTANT!
23
24     mov     dword [ebp-4],0 ; sum = 0
25     dump_stack 1, 2, 4     ; print out stack from ebp-8 to ebp+16
26     mov     ecx, 1         ; ecx is i in pseudocode
27 for_loop:
28     cmp     ecx, [ebp+8]   ; cmp i and n
29     jnle   end_for        ; if not i <= n, quit
30
31     add    [ebp-4], ecx    ; sum += i
32     inc    ecx
33     jmp    short for_loop
34
35 end_for:
36     mov    ebx, [ebp+12]   ; ebx = sump
37     mov    eax, [ebp-4]    ; eax = sum
38     mov    [ebx], eax
39
40     pop    ebx             ; restore ebx
41     leave
42     ret

```

sub5.asm

Why is line 22 of `sub5.asm` so important? Because the C calling convention requires the value of `EBX` to be unmodified by the function call. If

this is not done, it is very likely that the program will not work correctly.

Line 25 demonstrates how the `dump_stack` macro works. Recall that the first parameter is just a numeric label, and the second and third parameters determine how many double words to display below and above EBP respectively. Figure 4.13 shows an example run of the program. For this dump, one can see that the address of the dword to store the sum is `BFFFFB80` (at `EBP + 12`); the number to sum up to is `0000000A` (at `EBP + 8`); the return address for the routine is `08048501` (at `EBP + 4`); the saved EBP value is `BFFFFB88` (at `EBP`); the value of the local variable is `0` at (`EBP - 4`); and finally the saved EBX value is `4010648C` (at `EBP - 8`).

The `calc_sum` function could be rewritten to return the sum as its return value instead of using a pointer parameter. Since the sum is an integral value, the sum would be left in the EAX register. Line 11 of the `main5.c` file would need to be changed to:

```
sum = calc_sum(n);
```

Also, the prototype of `calc_sum` would need to be altered. Below is the modified assembly code:

```

_____ sub6.asm _____
1 ; subroutine _calc_sum
2 ; finds the sum of the integers 1 through n
3 ; Parameters:
4 ;   n    - what to sum up to (at [ebp + 8])
5 ; Return value:
6 ;   value of sum
7 ; pseudo C code:
8 ; int calc_sum( int n )
9 ; {
10 ;   int i, sum = 0;
11 ;   for( i=1; i <= n; i++ )
12 ;     sum += i;
13 ;   return sum;
14 ; }
15 segment .text
16     global  _calc_sum
17 ;
18 ; local variable:
19 ;   sum at [ebp-4]
20 _calc_sum:
21     enter   4,0           ; make room for sum on stack
22
23     mov     dword [ebp-4],0 ; sum = 0
24     mov     ecx, 1        ; ecx is i in pseudocode

```

```

1  segment .data
2  format      db "%d", 0
3
4  segment .text
5  ...
6      lea     eax, [ebp-16]
7      push   eax
8      push   dword format
9      call   _scanf
10     add    esp, 8
11     ...

```

Figure 4.14: Calling `scanf` from assembly

```

25  for_loop:
26      cmp     ecx, [ebp+8]      ; cmp i and n
27      jnle   end_for          ; if not i <= n, quit
28
29      add    [ebp-4], ecx      ; sum += i
30      inc    ecx
31      jmp    short for_loop
32
33  end_for:
34      mov    eax, [ebp-4]      ; eax = sum
35
36      leave
37      ret

```

sub6.asm

4.7.8 Calling C functions from assembly

One great advantage of interfacing C and assembly is that allows assembly code to access the large C library and user written functions. For example, what if one wanted to call the `scanf` function to read in an integer from the keyboard. Figure 4.14 shows code to do this. One very important point to remember is that `scanf` follows the C calling standard to the letter. This means that it preserves the values of the EBX, ESI and EDI registers; however, the EAX, ECX and EDX registers may be modified! In fact, EAX will definitely be changed, as it will contain the return value of the `scanf` call. For other examples of using interfacing with C, look at the code in `asm_io.asm` which was used to create `asm_io.obj`.

4.8 Reentrant and Recursive Subprograms

A reentrant subprogram must satisfy the following properties:

- It must not modify any code instructions. In a high level language this would be difficult, but in assembly it is not hard for a program to try to modify its own code. For example:

```
mov    word [cs:$+7], 5      ; copy 5 into the word 7 bytes ahead
add    ax, 2                 ; previous statement changes 2 to 5!
```

This code would work in real mode, but in protected mode operating systems the code segment is marked as read only. When the first line above executes the program will be aborted on these systems. This type of programming is bad for many reasons. It is confusing, hard to maintain and does not allow code sharing (see below).

- It must not modify global data (such as data in the `data` and the `bss` segments). All variables are stored on the stack.

There are several advantages to writing reentrant code.

- A reentrant subprogram can be called recursively.
- A reentrant program can be shared by multiple processes. On many multi-tasking operating systems, if there are multiple instances of a program running, only *one* copy of the code is in memory. Shared libraries and DLL's (*Dynamic Link Libraries*) use this idea as well.
- Reentrant subprograms work much better in *multi-threaded*⁵ programs. Windows 9x/NT and most UNIX-like operating systems (Solaris, Linux, *etc.*) support multi-threaded programs.

4.8.1 Recursive subprograms

These types of subprograms call themselves. The recursion can be either *direct* or *indirect*. Direct recursion occurs when a subprogram, say `foo`, calls itself inside `foo`'s body. Indirect recursion occurs when a subprogram is not called by itself directly, but by another subprogram it calls. For example, subprogram `foo` could call `bar` and `bar` could call `foo`.

Recursive subprograms must have a *termination condition*. When this condition is true, no more recursive calls are made. If a recursive routine does not have a termination condition or the condition never becomes true, the recursion will never end (much like an infinite loop).

⁵A multi-threaded program has multiple threads of execution. That is, the program itself is multi-tasked.

```

1 ; finds n!
2 segment .text
3     global _fact
4 _fact:
5     enter 0,0
6
7     mov     eax, [ebp+8]    ; eax = n
8     cmp     eax, 1
9     jbe     term_cond     ; if n <= 1, terminate
10    dec     eax
11    push    eax
12    call    _fact         ; call fact(n-1) recursively
13    pop     ecx           ; answer in eax
14    mul     dword [ebp+8] ; edx:eax = eax * [ebp+8]
15    jmp     short end_fact
16 term_cond:
17     mov     eax, 1
18 end_fact:
19     leave
20     ret

```

Figure 4.15: Recursive factorial function

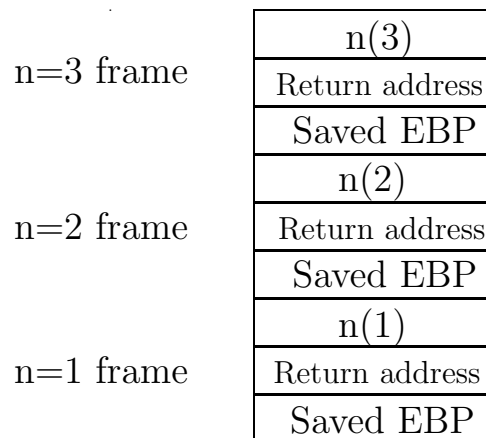


Figure 4.16: Stack frames for factorial function

```

1 void f( int x )
2 {
3     int i;
4     for( i=0; i < x; i++ ) {
5         printf( "%d\n", i);
6         f(i);
7     }
8 }

```

Figure 4.17: Another example (C version)

Figure 4.15 shows a function that calculates factorials recursively. It could be called from C with:

```
x = fact(3);          /* find 3! */
```

Figure 4.16 shows what the stack looks like at its deepest point for the above function call.

Figures 4.17 and 4.18 show another more complicated recursive example in C and assembly, respectively. What is the output is for `f(3)`? Note that the `ENTER` instruction creates a new `i` on the stack for each recursive call. Thus, each recursive instance of `f` has its own independent variable `i`. Defining `i` as a double word in the `data` segment would not work the same.

4.8.2 Review of C variable storage types

C provides several types of variable storage.

global These variables are defined outside of any function and are stored at fixed memory locations (in the `data` or `bss` segments) and exist from the beginning of the program until the end. By default, they can be accessed from any function in the program; however, if they are declared as `static`, only the functions in the same module can access them (*i.e.*, in assembly terms, the label is internal, not external).

static These are *local* variables of a function that are declared `static`. (Unfortunately, C uses the keyword `static` for two different purposes!) These variables are also stored at fixed memory locations (in `data` or `bss`), but can only be directly accessed in the functions they are defined in.

automatic This is the default type for a C variable defined inside a function. These variables are allocated on the stack when the function they are defined in is invoked and are deallocated when the function returns. Thus, they do not have fixed memory locations.

```
1 %define i ebp-4
2 %define x ebp+8          ; useful macros
3 segment .data
4 format      db "%d", 10, 0    ; 10 = '\n'
5 segment .text
6     global _f
7     extern _printf
8 _f:
9     enter 4,0                ; allocate room on stack for i
10
11    mov     dword [i], 0      ; i = 0
12 lp:
13    mov     eax, [i]          ; is i < x?
14    cmp     eax, [x]
15    jnl    quit
16
17    push   eax                ; call printf
18    push   format
19    call   _printf
20    add    esp, 8
21
22    push   dword [i]          ; call f
23    call   _f
24    pop    eax
25
26    inc    dword [i]          ; i++
27    jmp    short lp
28 quit:
29    leave
30    ret
```

Figure 4.18: Another example (assembly version)

register This keyword asks the compiler to use a register for the data in this variable. This is just a *request*. The compiler does *not* have to honor it. If the address of the variable is used anywhere in the program it will not be honored (since registers do not have addresses). Also, only simple integral types can be register values. Structured types can not be; they would not fit in a register! C compilers will often automatically make normal automatic variables into register variables without any hint from the programmer.

volatile This keyword tells the compiler that the value of the variable may change any moment. This means that the compiler can not make any assumptions about when the variable is modified. Often a compiler might store the value of a variable in a register temporarily and use the register in place of the variable in a section of code. It can not do these types of optimizations with **volatile** variables. A common example of a volatile variable would be one could be altered by two threads of a multi-threaded program. Consider the following code:

```
1 x = 10;  
2 y = 20;  
3 z = x;
```

If **x** could be altered by another thread, it is possible that the other thread changes **x** between lines 1 and 3 so that **z** would not be 10. However, if the **x** was not declared **volatile**, the compiler might assume that **x** is unchanged and set **z** to 10.

Another use of **volatile** is to keep the compiler from using a register for a variable.

Chapter 5

Arrays

5.1 Introduction

An *array* is a contiguous block of list of data in memory. Each element of the list must be the same type and use exactly the same number of bytes of memory for storage. Because of these properties, arrays allow efficient access of the data by its position (or index) in the array. The address of any element can be computed by knowing three facts:

- The address of the first element of the array.
- The number of bytes in each element
- The index of the element

It is convenient to consider the index of the first element of the array to be zero (just as in C). It is possible to use other values for the first index, but it complicates the computations.

5.1.1 Defining arrays

Defining arrays in the data and bss segments

To define an initialized array in the **data** segment, use the normal **db**, **dw**, *etc.* directives. NASM also provides a useful directive named **TIMES** that can be used to repeat a statement many times without having to duplicate the statements by hand. Figure 5.1 shows several examples of these.

To define an uninitialized array in the **bss** segment, use the **resb**, **resw**, *etc.* directives. Remember that these directives have an operand that specifies how many units of memory to reserve. Figure 5.1 also shows examples of these types of definitions.

```

1 segment .data
2 ; define array of 10 double words initialized to 1,2,..,10
3 a1          dd  1, 2, 3, 4, 5, 6, 7, 8, 9, 10
4 ; define array of 10 words initialized to 0
5 a2          dw  0, 0, 0, 0, 0, 0, 0, 0, 0, 0
6 ; same as before using TIMES
7 a3          times 10 dw 0
8 ; define array of bytes with 200 0's and then a 100 1's
9 a4          times 200 db 0
10           times 100 db 1
11
12 segment .bss
13 ; define an array of 10 uninitialized double words
14 a5          resd  10
15 ; define an array of 100 uninitialized words
16 a6          resw  100

```

Figure 5.1: Defining arrays

Defining arrays as local variables on the stack

There is no direct way to define a local array variable on the stack. As before, one computes the total bytes required by *all* local variables, including arrays, and subtracts this from ESP (either directly or using the ENTER instruction). For example, if a function needed a character variable, two double word integers and a 50 element word array, one would need $1 + 2 \times 4 + 50 \times 2 = 109$ bytes. However, the number subtracted from ESP should be a multiple of four (112 in this case) to keep ESP on a double word boundary. One could arrange the variables inside this 109 bytes in several ways. Figure 5.2 shows two possible ways. The unused part of the first ordering is there to keep the double words on double word boundaries to speed up memory accesses.

5.1.2 Accessing elements of arrays

There is no [] operator in assembly language as in C. To access an element of an array, its address must be computed. Consider the following two array definitions:

```

array1      db    5, 4, 3, 2, 1      ; array of bytes
array2      dw    5, 4, 3, 2, 1      ; array of words

```

Here are some examples using this arrays:

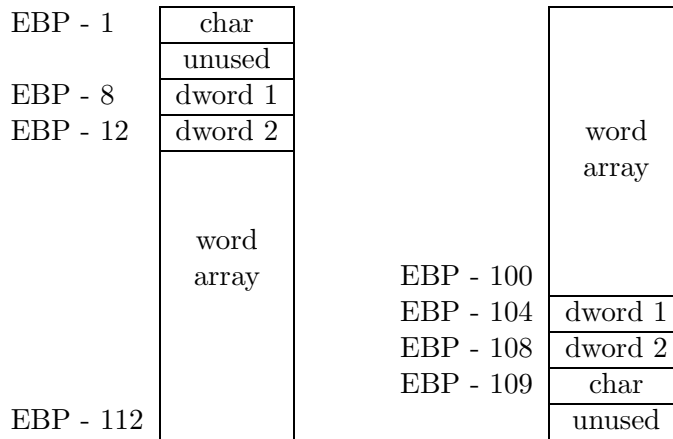


Figure 5.2: Arrangments of the stack

```

1      mov     al, [array1]           ; al = array1[0]
2      mov     al, [array1 + 1]      ; al = array1[1]
3      mov     [array1 + 3], al      ; array1[3] = al
4      mov     ax, [array2]          ; ax = array2[0]
5      mov     ax, [array2 + 2]      ; ax = array2[1] (NOT array2[2]!)
6      mov     [array2 + 6], ax      ; array2[3] = ax
7      mov     ax, [array2 + 1]      ; ax = ??

```

In line 5, element 1 of the word array is referenced, not element 2. Why? Words are two byte units, so to move to the next element of a word array, one must move two bytes ahead, not one. Line 7 will read one byte from the first element and one from the second. In C, the compiler looks at the type of a pointer in determining how many bytes to move in an expression that uses pointer arithmetic so that the programmer does not have to. However, in assembly, it is up to the programmer to take the size of array elements in account when moving from element to element.

Figure 5.3 shows a code snippet that adds all the elements of `array1` in the previous example code. In line 7, AX is added to DX. Why not AL? First, the two operands of the ADD instruction must be the same size. Secondly, it would be easy to add up bytes and get a sum that was too big to fit into a byte. By using DX, sums up to 65,535 are allowed. However, it is important to realize that AH is being added also. This is why AH is set to zero¹ in line 3.

Figures 5.4 and 5.5 show two alternative ways to calculate the sum. The lines in italics replace lines 6 and 7 of Figure 5.3.

¹Setting AH to zero is implicitly assuming that AL is an unsigned number. If it is signed, the appropriate action would be to insert a CBW instruction between lines 6 and 7

```

1      mov     ebx, array1      ; ebx = address of array1
2      mov     dx, 0           ; dx will hold sum
3      mov     ah, 0           ; ?
4      mov     ecx, 5
5  lp:
6      mov     al, [ebx]       ; al = *ebx
7      add     dx, ax          ; dx += ax (not al!)
8      inc     ebx            ; bx++
9      loop   lp

```

Figure 5.3: Summing elements of an array (Version 1)

```

1      mov     ebx, array1      ; ebx = address of array1
2      mov     dx, 0           ; dx will hold sum
3      mov     ecx, 5
4  lp:
5      add     dl, [ebx]       ; dl += *ebx
6      jnc     next           ; if no carry goto next
7      inc     dh              ; inc dh
8  next:
9      inc     ebx            ; bx++
10     loop   lp

```

Figure 5.4: Summing elements of an array (Version 2)

5.1.3 More advanced indirect addressing

Not surprisingly, indirect addressing is often used with arrays. The most general form of an indirect memory reference is:

$$[\textit{base reg} + \textit{factor} * \textit{index reg} + \textit{constant}]$$

where:

base reg is one of the registers EAX, EBX, ECX, EDX, EBP, ESP, ESI or EDI.

factor is either 1, 2, 4 or 8. (If 1, factor is omitted.)

index reg is one of the registers EAX, EBX, ECX, EDX, EBP, ESI, EDI. (Note that ESP is not in list.)

```

1      mov     ebx, array1      ; ebx = address of array1
2      mov     dx, 0           ; dx will hold sum
3      mov     ecx, 5
4  lp:
5      add     dl, [ebx]       ; dl += *ebx
6      adc     dh, 0           ; dh += carry flag + 0
7      inc     ebx             ; bx++
8      loop   lp

```

Figure 5.5: Summing elements of an array (Version 3)

constant is a 32-bit constant. The constant can be a label (or a label expression).

5.1.4 Example

Here is an example that uses an array and passes it to a function. It uses the `array1.c` program (listed below) as a driver, not the `driver.c` program.

```

----- array1.asm -----
1  %define ARRAY_SIZE 100
2  %define NEW_LINE 10
3
4  segment .data
5  FirstMsg      db  "First 10 elements of array", 0
6  Prompt        db  "Enter index of element to display: ", 0
7  SecondMsg     db  "Element %d is %d", NEW_LINE, 0
8  ThirdMsg      db  "Elements 20 through 29 of array", 0
9  InputFormat   db  "%d", 0
10
11 segment .bss
12 array        resd ARRAY_SIZE
13
14 segment .text
15     extern  _puts, _printf, _scanf, _dump_line
16     global  _asm_main
17 _asm_main:
18     enter  4,0           ; local dword variable at EBP - 4
19     push   ebx
20     push   esi
21

```

```

22 ; initialize array to 100, 99, 98, 97, ...
23
24     mov     ecx, ARRAY_SIZE
25     mov     ebx, array
26 init_loop:
27     mov     [ebx], ecx
28     add     ebx, 4
29     loop   init_loop
30
31     push   dword FirstMsg           ; print out FirstMsg
32     call   _puts
33     pop    ecx
34
35     push   dword 10
36     push   dword array
37     call   _print_array           ; print first 10 elements of array
38     add   esp, 8
39
40 ; prompt user for element index
41 Prompt_loop:
42     push   dword Prompt
43     call   _printf
44     pop    ecx
45
46     lea   eax, [ebp-4]           ; eax = address of local dword
47     push   eax
48     push   dword InputFormat
49     call   _scanf
50     add   esp, 8
51     cmp   eax, 1                 ; eax = return value of scanf
52     je    InputOK
53
54     call   _dump_line           ; dump rest of line and start over
55     jmp   Prompt_loop           ; if input invalid
56
57 InputOK:
58     mov   esi, [ebp-4]
59     push  dword [array + 4*esi]
60     push  esi
61     push  dword SecondMsg       ; print out value of element
62     call  _printf
63     add  esp, 12

```

```

64
65     push    dword ThirdMsg      ; print out elements 20-29
66     call   _puts
67     pop    ecx
68
69     push    dword 10
70     push    dword array + 20*4   ; address of array[20]
71     call   _print_array
72     add    esp, 8
73
74     pop    esi
75     pop    ebx
76     mov    eax, 0                ; return back to C
77     leave
78     ret
79
80 ;
81 ; routine _print_array
82 ; C-callable routine that prints out elements of a double word array as
83 ; signed integers.
84 ; C prototype:
85 ; void print_array( const int * a, int n);
86 ; Parameters:
87 ;   a - pointer to array to print out (at ebp+8 on stack)
88 ;   n - number of integers to print out (at ebp+12 on stack)
89
90 segment .data
91 OutputFormat    db    "%-5d %5d", NEW_LINE, 0
92
93 segment .text
94     global _print_array
95 _print_array:
96     enter    0,0
97     push    esi
98     push    ebx
99
100    xor     esi, esi                ; esi = 0
101    mov     ecx, [ebp+12]           ; ecx = n
102    mov     ebx, [ebp+8]           ; ebx = address of array
103 print_loop:
104    push    ecx                    ; printf might change ecx!
105

```

```

106     push    dword [ebx + 4*esi]      ; push array[esi]
107     push    esi
108     push    dword OutputFormat
109     call    _printf
110     add     esp, 12                 ; remove parameters (leave ecx!)
111
112     inc     esi
113     pop     ecx
114     loop   print_loop
115
116     pop     ebx
117     pop     esi
118     leave
119     ret

```

array1.asm

```

_____ array1c.c _____
1  #include <stdio.h>
2
3  int asm_main( void );
4  void dump_line( void );
5
6  int main()
7  {
8      int ret_status ;
9      ret_status = asm_main();
10     return ret_status ;
11 }
12
13 /*
14  * function dump_line
15  * dumps all chars left in current line from input buffer
16  */
17 void dump_line()
18 {
19     int ch;
20
21     while( (ch = getchar()) != EOF && ch != '\n')
22         /* null body*/;
23 }

```

array1c.c

LODSB	AL = [DS:ESI] ESI = ESI ± 1	STOSB	[ES:EDI] = AL EDI = EDI ± 1
LODSW	AX = [DS:ESI] ESI = ESI ± 2	STOSW	[ES:EDI] = AX EDI = EDI ± 2
LODSD	EAX = [DS:ESI] ESI = ESI ± 4	STOSD	[ES:EDI] = EAX EDI = EDI ± 4

Figure 5.6: Reading and writing string instructions

5.2 Array/String Instructions

The 80x86 family of processors provide several instructions that are designed to work with arrays. These instructions are called *string instructions*. They use the index registers (ESI and EDI) to perform an operation and then to automatically increment or decrement one or both of the index registers. The *direction flag* in the FLAGS register determines where the index registers are incremented or decremented. There are two instructions that modify the direction flag:

CLD clears the direction flag. In this state, the index registers are incremented.

STD sets the direction flag. In this state, the index registers are decremented.

A *very* common mistake in 80x86 programming is to forget to explicitly put the direction flag in the correct state. This often leads to code that works most of the time (when the direction flag happens to be in the desired state), but does not work *all* the time.

5.2.1 Reading and writing memory

The simplest string instructions either read or write memory or both. They may read or write a byte, word or double word at a time. Figure 5.6 shows these instructions with a short psuedo-code description of what they do. There are several points to notice here. First, ESI is used for reading and EDI for writing. It is easy to remember this if one remembers that SI stands for *Source Index* and DI stands for *Destination Index*. Next, notice that the register that holds the data is fixed (either AL, AX or EAX). Finally, note that the storing instructions use ES to determine the segment to write to, not DS. In protected mode programming this is not usually a problem, since there is only one data segment and ES should be automatically initialized to reference it (just as DS is). However, in real mode programming, it is *very* important for the programmer to initialize ES to the correct segment

```

1  segment .data
2  array1 dd 1, 2, 3, 4, 5, 6, 7, 8, 9, 10
3
4  segment .bss
5  array2 resd 10
6
7  segment .text
8      cld                                ; don't forget this!
9      mov     esi, array1
10     mov     edi, array2
11     mov     ecx, 10
12 lp:
13     lodsd
14     stosd
15     loop   lp

```

Figure 5.7: Load and store example

selector value². Figure 5.7 shows an example use of these instructions that copies an array into another.

The combination of a `LODSx` and `STOSx` instruction (as in lines 13 and 14 of Figure 5.7) is very common. In fact, this combination can be performed by a single `MOVSD` string instruction. Figure 5.8 describes the operations that these instructions perform. Lines 13 and 14 of Figure 5.7 could be replaced with a single `MOVSD` instruction with the same effect. The only difference would be that the `EAX` register would not be used at all in the loop.

5.2.2 The `REP` instruction prefix

The 80x86 family provides a special instruction prefix³ called `REP` that can be used with the above string instructions. This prefix tells the CPU to repeat the next string instruction a specified number of times. The `ECX` register is used to count the iterations (just as for the `LOOP` instruction). Using the `REP` prefix, the loop in Figure 5.7 (lines 12 to 15) could be replaced with a single line:

²Another complication is that one can not copy the value of the `DS` register into the `ES` register directly using a single `MOV` instruction. Instead, the value of `DS` must be copied to a general purpose register (like `AX`) and then copied from that register to `ES` using two `MOV` instructions.

³A instruction prefix is not an instruction, it is a special byte that is placed before a string instruction that modifies the instructions behavior. Other prefixes are also used to override segment defaults of memory accesses

MOVSB	byte [ES:EDI] = byte [DS:ESI] ESI = ESI ± 1 EDI = EDI ± 1
MOVSW	word [ES:EDI] = word [DS:ESI] ESI = ESI ± 2 EDI = EDI ± 2
MOVSD	dword [ES:EDI] = dword [DS:ESI] ESI = ESI ± 4 EDI = EDI ± 4

Figure 5.8: Memory move string instructions

```

1 segment .bss
2 array resd 10
3
4 segment .text
5     cld                ; don't forget this!
6     mov     edi, array
7     mov     ecx, 10
8     xor     eax, eax
9     rep stosd

```

Figure 5.9: Zero array example

```
rep movsd
```

Figure 5.9 shows another example that zeroes out the contents of an array.

5.2.3 Comparison string instructions

Figure 5.10 shows several new string instructions that can be used to compare memory with other memory or a register. They are useful for comparing or searching arrays. They set the FLAGS register just like the `CMP` instruction. The `CMPSx` instructions compare corresponding memory locations and the `SCASx` scan memory locations for a specific value.

Figure 5.11 shows a short code snippet that searches for the number 12 in a double word array. The `SCASD` instruction on line 10 always adds 4 to EDI, even if the value searched for is found. Thus, if one wishes to find the address of the 12 found in the array, it is necessary to subtract 4 from EDI (as line 16 does).

CMPSB	compares byte [DS:ESI] and byte [ES:EDI] ESI = ESI ± 1 EDI = EDI ± 1
CMPSW	compares word [DS:ESI] and word [ES:EDI] ESI = ESI ± 2 EDI = EDI ± 2
CMPSD	compares dword [DS:ESI] and dword [ES:EDI] ESI = ESI ± 4 EDI = EDI ± 4
SCASB	compares AL and [ES:EDI] EDI ± 1
SCASW	compares AX and [ES:EDI] EDI ± 2
SCASD	compares EAX and [ES:EDI] EDI ± 4

Figure 5.10: Comparison string instructions

5.2.4 The REPx instruction prefixes

There are several other REP-like instruction prefixes that can be used with the comparison string instructions. Figure 5.12 shows the two new prefixes and describes their operation. REPE and REPZ are just synonyms for the same prefix (as are REPNE and REPNZ). If the repeated comparison string instruction stops because of the result of the comparison, the index register or registers are still incremented and ECX decremented; however, the FLAGS register still holds the state that terminated the repetition. Thus, it is possible to use the Z flag to determine if the repeated comparisons stopped because of a comparison or ECX becoming zero.

Why can one not just look to see if ECX is zero after the repeated comparison?

Figure 5.13 shows an example code snippet that determines if two blocks of memory are equal. The JE on line 7 of the example checks to see the result of the previous instruction. If the repeated comparison stopped because it found two unequal bytes, the Z flag will still be cleared and no branch is made; however, if the comparisons stopped because ECX became zero, the Z flag will still be set and the code branches to the `equal` label.

5.2.5 Example

This section contains an assembly source file with several functions that implement array operations using string instructions. Many of the functions duplicate familiar C library functions.

```

1 segment .bss
2 array      resd 100
3
4 segment .text
5     cld
6     mov     edi, array      ; pointer to start of array
7     mov     ecx, 100       ; number of elements
8     mov     eax, 12        ; number to scan for
9 lp:
10    scasd
11    je      found
12    loop   lp
13    ; code to perform if not found
14    jmp    onward
15 found:
16    sub     edi, 4          ; edi now points to 12 in array
17    ; code to perform if found
18 onward:

```

Figure 5.11: Search example

REPE, REPZ	repeats instruction while Z flag is set or at most ECX times
REPNE, REPNZ	repeats instruction while Z flag is cleared or at most ECX times

Figure 5.12: REPx instruction prefixes

```

1 global _asm_copy, _asm_find, _asm_strlen, _asm_strcpy
2
3 segment .text
4 ; function _asm_copy
5 ; copies blocks of memory
6 ; C prototype
7 ; void asm_copy( void * dest, const void * src, unsigned sz);
8 ; parameters:
9 ; dest - pointer to buffer to copy to
10 ; src  - pointer to buffer to copy from
11 ; sz   - number of bytes to copy
12
13 ; next, some helpful symbols are defined
14

```

```

1 segment .text
2     cld
3     mov     esi, block1      ; address of first block
4     mov     edi, block2      ; address of second block
5     mov     ecx, size        ; size of blocks in bytes
6     repe   cmpsb            ; repeat while Z flag is set
7     je     equal            ; if Z set, blocks equal
8     ; code to perform if blocks are not equal
9     jmp    onward
10 equal:
11     ; code to perform if equal
12 onward:

```

Figure 5.13: Comparing memory blocks

```

15 %define dest [ebp+8]
16 %define src  [ebp+12]
17 %define sz   [ebp+16]
18 _asm_copy:
19     enter   0, 0
20     push   esi
21     push   edi
22
23     mov    esi, src          ; esi = address of buffer to copy from
24     mov    edi, dest         ; edi = address of buffer to copy to
25     mov    ecx, sz           ; ecx = number of bytes to copy
26
27     cld                      ; clear direction flag
28     rep   movsb              ; execute movsb ECX times
29
30     pop    edi
31     pop    esi
32     leave
33     ret
34
35
36 ; function _asm_find
37 ; searches memory for a given byte
38 ; void * asm_find( const void * src, char target, unsigned sz);
39 ; parameters:

```

```
40 ; src    - pointer to buffer to search
41 ; target - byte value to search for
42 ; sz     - number of bytes in buffer
43 ; return value:
44 ; if target is found, pointer to first occurrence of target in buffer
45 ; is returned
46 ; else
47 ;     NULL is returned
48 ; NOTE: target is a byte value, but is pushed on stack as a dword value.
49 ;     The byte value is stored in the lower 8-bits.
50 ;
51 %define src    [ebp+8]
52 %define target [ebp+12]
53 %define sz     [ebp+16]
54
55 _asm_find:
56     enter    0,0
57     push    edi
58
59     mov     eax, target    ; al has value to search for
60     mov     edi, src
61     mov     ecx, sz
62     cld
63
64     repne  scasb          ; scan until ECX == 0 or [ES:EDI] == AL
65
66     je     found_it      ; if zero flag set, then found value
67     mov     eax, 0        ; if not found, return NULL pointer
68     jmp    short quit
69 found_it:
70     mov     eax, edi
71     dec     eax          ; if found return (DI - 1)
72 quit:
73     pop     edi
74     leave
75     ret
76
77
78 ; function _asm_strlen
79 ; returns the size of a string
80 ; unsigned asm_strlen( const char * );
81 ; parameter:
```

```

82 ; src - pointer to string
83 ; return value:
84 ; number of chars in string (not counting, ending 0) (in EAX)
85
86 %define src [ebp + 8]
87 _asm_strlen:
88     enter    0,0
89     push    edi
90
91     mov     edi, src        ; edi = pointer to string
92     mov     ecx, 0FFFFFFFh ; use largest possible ECX
93     xor     al,al          ; al = 0
94     cld
95
96     repnz   scasb          ; scan for terminating 0
97
98 ;
99 ; repnz will go one step too far, so length is 0FFFFFFE - ECX,
100 ; not 0FFFFFFF - ECX
101 ;
102     mov     eax,0FFFFFFEh
103     sub     eax, ecx        ; length = 0FFFFFFEh - ecx
104
105     pop     edi
106     leave
107     ret
108
109 ; function _asm_strcpy
110 ; copies a string
111 ; void asm_strcpy( char * dest, const char * src);
112 ; parameters:
113 ; dest - pointer to string to copy to
114 ; src - pointer to string to copy from
115 ;
116 %define dest [ebp + 8]
117 %define src [ebp + 12]
118 _asm_strcpy:
119     enter    0,0
120     push    esi
121     push    edi
122
123     mov     edi, dest

```



```

124     mov     esi, src
125     cld
126 cpy_loop:
127     lodsb                ; load AL & inc si
128     stosb                ; store AL & inc di
129     or      al, al        ; set condition flags
130     jnz     cpy_loop      ; if not past terminating 0, continue
131
132     pop     edi
133     pop     esi
134     leave
135     ret

```

memory.asm

memex.c

```

1  #include <stdio.h>
2
3  #define STR_SIZE 30
4  /* prototypes */
5
6  void asm_copy( void *, const void *, unsigned ) __attribute__((cdecl));
7  void * asm_find( const void *,
8                  char target, unsigned ) __attribute__((cdecl));
9  unsigned asm_strlen( const char * ) __attribute__((cdecl));
10 void asm_strcpy( char *, const char * ) __attribute__((cdecl));
11
12 int main()
13 {
14     char st1[STR_SIZE] = "test string";
15     char st2[STR_SIZE];
16     char * st;
17     char ch;
18
19     asm_copy(st2, st1, STR_SIZE); /* copy all 30 chars of string */
20     printf("%s\n", st2);
21
22     printf("Enter a char: "); /* look for byte in string */
23     scanf("%c%*[^\\n]", &ch);
24     st = asm_find(st2, ch, STR_SIZE);
25     if ( st )
26         printf("Found it: %s\n", st);
27     else
28         printf("Not found\n");

```

```
29
30  st1 [0] = 0;
31  printf ("Enter string :");
32  scanf ("%s", st1);
33  printf (" len = %u\n", asm_strlen(st1));
34
35  asm_strcpy( st2, st1);    /* copy meaningful data in string */
36  printf ("%s\n", st2 );
37
38  return 0;
39 }
```

memex.c

Chapter 6

Floating Point

6.1 Floating Point Representation

6.1.1 Non-integral binary numbers

When number systems were discussed in the first chapter, only integer values were discussed. Obviously, it must be possible to represent non-integral numbers in other bases as well as decimal. In decimal, digits to the right of the decimal point have associated negative powers of ten:

$$0.123 = 1 \times 10^{-1} + 2 \times 10^{-2} + 3 \times 10^{-3}$$

Not surprisingly, binary numbers work similarly:

$$0.101_2 = 1 \times 2^{-1} + 0 \times 2^{-2} + 1 \times 2^{-3} = 0.625$$

This idea can be combined with the integer methods of Chapter 1 to convert a general number:

$$110.011_2 = 4 + 2 + 0.25 + 0.125 = 6.375$$

Converting from decimal to binary is not very difficult either. In general, divide the decimal number into two parts: integer and fraction. Convert the integer part to binary using the methods from Chapter 1. The fractional part is converted using the method described below.

Consider a binary fraction with the bits labeled a, b, c, \dots . The number in binary then looks like:

$$0.abcdef\dots$$

Multiply the number by two. The binary representation of the new number will be:

$$a.bcd\epsilon f\dots$$

$0.5625 \times 2 = 1.125$	first bit = 1
$0.125 \times 2 = 0.25$	second bit = 0
$0.25 \times 2 = 0.5$	third bit = 0
$0.5 \times 2 = 1.0$	fourth bit = 1

Figure 6.1: Converting 0.5625 to binary

$0.85 \times 2 = 1.7$
$0.7 \times 2 = 1.4$
$0.4 \times 2 = 0.8$
$0.8 \times 2 = 1.6$
$0.6 \times 2 = 1.2$
$0.2 \times 2 = 0.4$
$0.4 \times 2 = 0.8$
$0.8 \times 2 = 1.6$

Figure 6.2: Converting 0.85 to binary

Note that the first bit is now in the one's place. Replace the a with 0 to get:

$$0.bcdf\dots$$

and multiply by two again to get:

$$b.cdf\dots$$

Now the second bit (b) is in the one's position. This procedure can be repeated until as many bits are needed are found. Figure 6.1 shows a real example that converts 0.5625 to binary. The method stops when a fractional part of zero is reached.

As another example, consider converting 23.85 to binary. It is easy to convert the integral part ($23 = 10111_2$), but what about the fractional part (0.85)? Figure 6.2 shows the beginning of this calculation. If one looks at

the numbers carefully, an infinite loop is found! This means that 0.85 is a repeating binary (as opposed to a repeating decimal in base 10)¹ There is a pattern to the numbers in the calculation. Looking at the pattern, one can see that $0.85 = 0.11\overline{0110}_2$. Thus, $23.85 = 10111.11\overline{0110}_2$.

One important consequence of the above calculation is that 23.85 can not be represented *exactly* in binary using a finite number of bits. (Just as $\frac{1}{3}$ can not be represented in decimal with a finite number of digits.) As this chapter shows, `float` and `double` variables in C are stored in binary. Thus, values like 23.85 can not be stored exactly into these variables. Only an approximation of 23.85 can be stored.

To simplify the hardware, floating point numbers are stored in a consistent format. This format uses scientific notation (but in binary, using powers of two, not ten). For example, 23.85 or $10111.11011001100110\dots_2$ would be stored as:

$$1.011111011001100110\dots \times 2^{100}$$

(where the exponent (100) is in binary). A *normalized* floating point number has the form:

$$1.sssssssssssss \times 2^{eeeeeee}$$

where *1.sssssssssssss* is the *significand* and *eeeeeee* is the *exponent*.

6.1.2 IEEE floating point representation

The IEEE (Institute of Electrical and Electronic Engineers) is an international organization that has designed specific binary formats for storing floating point numbers. This format is used on most (but not all!) computers made today. Often it is supported by the hardware of the computer itself. For example, Intel's numeric (or math) coprocessors (which are built into all its CPU's since the Pentium) use it. The IEEE defines two different formats with different precisions: single and double precision. Single precision is used by `float` variables in C and double precision is used by `double` variables.

Intel's math coprocessor also uses a third, higher precision called *extended precision*. In fact, all data in the coprocessor itself is in this precision. When it is stored in memory from the coprocessor it is converted to either single or double precision automatically.² Extended precision uses a slightly different general format than the IEEE float and double formats and so will not be discussed here.

¹It should not be so surprising that a number might repeat in one base, but not another. Think about $\frac{1}{3}$, it repeats in decimal, but in ternary (base 3) it would be 0.1_3 .

² Some compilers (such as Borland's) `long double` type uses this extended precision. However, other compilers use double precision for both `double` and `long double`. (This is allowed by ANSI C.)

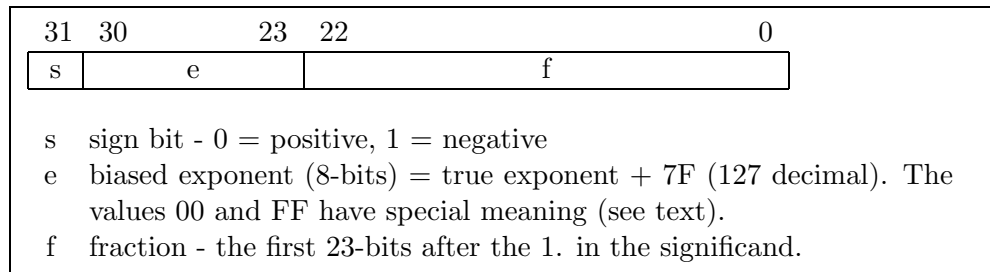


Figure 6.3: IEEE single precision

IEEE single precision

Single precision floating point uses 32 bits to encode the number. It is usually accurate to 7 significant decimal digits. Floating point numbers are stored in a much more complicated format than integers. Figure 6.3 shows the basic format of a IEEE single precision number. There are several quirks to the format. Floating point numbers do not use the two's complement representation for negative numbers. They use a signed magnitude representation. Bit 31 determines the sign of the number as shown.

The binary exponent is not stored directly. Instead, the sum of the exponent and 7F is stored from bit 23 to 30. This *biased exponent* is always non-negative.

The fraction part assumes a normalized significand (in the form $1.ssssssss$). Since the first bit is always an one, the leading one is *not stored!* This allows the storage of an additional bit at the end and so increases the precision slightly. This idea is known as the *hidden one representation*.

One should always keep in mind that the bytes 41 BE CC CD can be interpreted different ways depending on what a program does with them! As a single precision floating point number, they represent 23.850000381, but as a double word integer, they represent 1,103,023,309! The CPU does not know which is the correct interpretation!

How would 23.85 be stored? First, it is positive so the sign bit is 0. Next the true exponent is 4, so the biased exponent is $7F + 4 = 83_{16}$. Finally, the fraction is 01111101100110011001100 (remember the leading one is hidden). Putting this all together (to help clarify the different sections of the floating point format, the sign bit and the fraction have been underlined and the bits have been grouped into 4-bit nibbles):

$$\underline{0} \underline{100\ 0001\ 1011\ 1110\ 1100\ 1100\ 1100\ 1100}_2 = 41BECCCC_{16}$$

This is not exactly 23.85 (since it is a repeating binary). If one converts the above back to decimal, one finds that it is approximately 23.849998474. This number is very close to 23.85, but it is not exact. Actually, in C, 23.85 would not be represented exactly as above. Since the left-most bit that was truncated from the exact representation is 1, the last bit is rounded up to 1. So 23.85 would be represented as 41 BE CC CD in hex using single precision. Converting this to decimal results in 23.850000381 which is a slightly better approximation of 23.85.

$e = 0$ and $f = 0$	denotes the number zero (which can not be normalized) Note that there is a +0 and -0.
$e = 0$ and $f \neq 0$	denotes a <i>denormalized number</i> . These are discussed in the next section.
$e = FF$ and $f = 0$	denotes infinity (∞). There are both positive and negative infinities.
$e = FF$ and $f \neq 0$	denotes an undefined result, known as <i>NaN</i> (Not a Number).

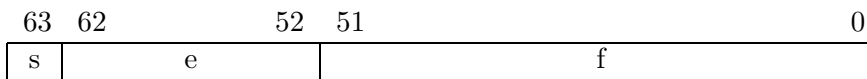
Table 6.1: Special values of f and e 

Figure 6.4: IEEE double precision

How would -23.85 be represented? Just change the sign bit: C1 BE CC CD. Do *not* take the two's complement!

Certain combinations of e and f have special meanings for IEEE floats. Table 6.1 describes these special values. An infinity is produced by an overflow or by division by zero. An undefined result is produced by an invalid operation such as trying to find the square root of a negative number, adding two infinities, *etc.*

Normalized single precision numbers can range in magnitude from 1.0×2^{-126} ($\approx 1.1755 \times 10^{-35}$) to $1.11111 \dots \times 2^{127}$ ($\approx 3.4028 \times 10^{35}$).

Denormalized numbers

Denormalized numbers can be used to represent numbers with magnitudes too small to normalize (*i.e.*, below 1.0×2^{-126}). For example, consider the number $1.001_2 \times 2^{-129}$ ($\approx 1.6530 \times 10^{-39}$). In the given normalized form, the exponent is too small. However, it can be represented in the unnormalized form: $0.01001_2 \times 2^{-127}$. To store this number, the biased exponent is set to 0 (see Table 6.1) and the fraction is the complete significant of the number written as a product with 2^{-127} (*i.e.*, all bits are stored including the one to the left of the decimal point). The representation of 1.001×2^{-129} is then:

0 000 0000 0 001 0010 0000 0000 0000 0000

IEEE double precision

IEEE double precision uses 64 bits to represent numbers and is usually accurate to about 15 significant decimal digits. As Figure 6.4 shows, the

basic format is very similar to single precision. More bits are used for the biased exponent (11) and the fraction (52) than for single precision.

The larger range for the biased exponent has two consequences. The first is that it is calculated as the sum of the true exponent and 3FF (1023) (not 7F as for single precision). Secondly, a large range of true exponents (and thus a larger range of magnitudes) is allowed. Double precision magnitudes can range from approximately 10^{-308} to 10^{308} .

It is the larger field of the fraction that is responsible for the increase in the number of significant digits for double values.

As an example, consider 23.85 again. The biased exponent will be $4 + 3FF = 403$ in hex. Thus, the double representation would be:

0 100 0000 0011 0111 1101 1001 1001 1001 1001 1001 1001 1001 1001 1001 1010

or 40 37 D9 99 99 99 99 9A in hex. If one converts this back to decimal, one finds 23.850000000000014 (there are 12 zeros!) which is a much better approximation of 23.85.

The double precision has the same special values as single precision³. Denormalized numbers are also very similar. The only main difference is that double denormalized numbers use 2^{-1023} instead of 2^{-127} .

6.2 Floating Point Arithmetic

Floating point arithmetic on a computer is different than in continuous mathematics. In mathematics, all numbers can be considered exact. As shown in the previous section, on a computer many numbers can not be represented exactly with a finite number of bits. All calculations are performed with limited precision. In the examples of this section, numbers with a 8-bit significands will be used for simplicity.

6.2.1 Addition

To add two floating point numbers, the exponents must be equal. If they are not already equal, then they must be made equal by shifting the significand of the number with the smaller exponent. For example, consider $10.375 + 6.34375 = 16.71875$ or in binary:

$$\begin{array}{r} 1.0100110 \times 2^3 \\ + 1.1001011 \times 2^2 \\ \hline \end{array}$$

³The only difference is that for the infinity and undefined values, the biased exponent is 7FF not FF.

These two numbers do not have the same exponent so shift the significant to make the exponents the same and then add:

$$\begin{array}{r} 1.0100110 \times 2^3 \\ + 0.1100110 \times 2^3 \\ \hline 10.0001100 \times 2^3 \end{array}$$

Note that the shifting of 1.001011×2^2 drops off the trailing one and after rounding results in 0.1100110×2^3 . The result of the addition, 10.0001100×2^3 (or 1.00001100×2^4) is equal to 10000.110_2 or 16.75. This is *not* equal to the exact answer (16.71875)! It is only an approximation due to the round off errors of the addition process.

It is important to realize that floating point arithmetic on a computer (or calculator) is always an approximation. The laws of mathematics do not always work with floating point numbers on a computer. Mathematics assumes infinite precision which no computer can match. For example, mathematics teaches that $(a + b) - b = a$; however, this may not hold true exactly on a computer!

6.2.2 Subtraction

Subtraction works very similarly and has the same problems as addition. As an example, consider $16.75 - 15.9375 = 0.8125$:

$$\begin{array}{r} 1.0000110 \times 2^4 \\ - 1.1111111 \times 2^3 \\ \hline \end{array}$$

Shifting 1.1111111×2^3 gives (rounding up) 1.0000000×2^4

$$\begin{array}{r} 1.0000110 \times 2^4 \\ - 1.0000000 \times 2^4 \\ \hline 0.0000110 \times 2^4 \end{array}$$

$0.0000110 \times 2^4 = 0.11_2 = 0.75$ which is not exactly correct.

6.2.3 Multiplication and division

For multiplication, the significantands are multiplied and the exponents are added. Consider $10.375 \times 2.5 = 25.9375$:

$$\begin{array}{r} 1.0100110 \times 2^3 \\ \times 1.0100000 \times 2^1 \\ \hline 10100110 \\ + 10100110 \\ \hline 1.10011111000000 \times 2^4 \end{array}$$

Of course, the real result would be rounded to 8-bits to give:

$$1.1010000 \times 2^4 = 11010.000_2 = 26$$

Division is more complicated, but has similar problems with round off errors.

6.2.4 Ramifications for programming

The main point of this section is that floating point calculations are not exact. The programmer needs to be aware of this. A common mistake that programmers make with floating point numbers is to compare them assuming that a calculation is exact. For example, consider a function named $f(x)$ that makes a complex calculation and a program is trying to find the function's roots⁴. One might be tempted to use the following statement to check to see if x is a root:

```
if ( f(x) == 0.0 )
```

But, what if $f(x)$ returns 1×10^{-30} ? This very likely means that x is a *very* good approximation of a true root; however, the equality will be false. There may not be any IEEE floating point value of x that returns exactly zero, due to round off errors in $f(x)$.

A much better method would be to use:

```
if ( fabs(f(x)) < EPS )
```

where `EPS` is a macro defined to be a very small positive value (like 1×10^{-10}). This is true whenever $f(x)$ is very close to zero. In general, to compare a floating point value (say x) to another (y) use:

```
if ( fabs(x - y)/fabs(y) < EPS )
```

6.3 The Numeric Coprocessor

6.3.1 Hardware

The earliest Intel processors had no hardware support for floating point operations. This does not mean that they could not perform float operations. It just means that they had to be performed by procedures composed of many non-floating point instructions. For these early systems, Intel did provide an additional chip called a *math coprocessor*. A math coprocessor has machine instructions that perform many floating point operations much faster than using a software procedure (on early processors, at least 10 times faster!). The coprocessor for the 8086/8088 was called the 8087. For the 80286, there was a 80287 and for the 80386, a 80387. The 80486DX processor

⁴A root of a function is a value x such that $f(x) = 0$

integrated the math coprocessor into the 80486 itself.⁵ Since the Pentium, all generations of 80x86 processors have a builtin math coprocessor; however, it is still programmed as if it was a separate unit. Even earlier systems without a coprocessor can install software that emulates a math coprocessor. These emulator packages are automatically activated when a program executes a coprocessor instruction and runs a software procedure that produces the same result as the coprocessor would have (though much slower, of course).

The numeric coprocessor has eight floating point registers. Each register holds 80-bits of data. Floating point numbers are *always* stored as 80-bit extended precision numbers in these registers. The registers are named **ST0**, **ST1**, **ST2**, . . . **ST7**. The floating point registers are used differently than the integer registers of the main CPU. The floating point registers are organized as a *stack*. Recall that a stack is a *Last-In First-Out* (LIFO) list. **ST0** always refers to the value at the top of the stack. All new numbers are added to the top of the stack. Existing numbers are pushed down on the stack to make room for the new number.

There is also a status register in the numeric coprocessor. It has several flags. Only the 4 flags used for comparisons will be covered: **C₀**, **C₁**, **C₂** and **C₃**. The use of these is discussed later.

6.3.2 Instructions

To make it easy to distinguish the normal CPU instructions from coprocessor ones, all the coprocessor mnemonics start with a **F**.

Loading and storing

There are several instructions that load data onto the top of the coprocessor register stack:

- FLD *source*** loads a floating point number from memory onto the top of the stack. The *source* may be a single, double or extended precision number or a coprocessor register.
- FILD *source*** reads a *integer* from memory, converts it to floating point and stores the result on top of the stack. The *source* may be either a word, double word or quad word.
- FLD1** stores a one on the top of the stack.
- FLDZ** stores a zero on the top of the stack.

There are also several instructions that store data from the stack into memory. Some of these instructions also *pop* (*i.e.*, remove) the number from the stack as it stores it.

⁵However, the 80486SX did *not* have an integrated coprocessor. There was a separate 80487SX chip for these machines.

FST <i>dest</i>	stores the top of the stack (ST0) into memory. The <i>destination</i> may either a single or double precision number or a coprocessor register.
FSTP <i>dest</i>	stores the top of the stack into memory just as FST; however, after the number is stored, its value is popped from the stack. The <i>destination</i> may either a single, double or extended precision number or a coprocessor register.
FIST <i>dest</i>	stores the value of the top of the stack converted to an integer into memory. The <i>destination</i> may either a word or a double word. The stack itself is unchanged. How the floating point number is converted to an integer depends on some bits in the coprocessor's <i>control word</i> . This is a special (non-floating point) word register that controls how the coprocessor works. By default, the control word is initialized so that it rounds to the nearest integer when it converts to integer. However, the FSTCW (Store Control Word) and FLDCW (Load Control Word) instructions can be used to change this behavior.
FISTP <i>dest</i>	Same as FIST except for two things. The top of the stack is popped and the <i>destination</i> may also be a quad word.

There are two other instructions that can be move or remove data on the stack itself.

FXCH ST <i>n</i>	exchanges the values in ST0 and ST <i>n</i> on the stack (where <i>n</i> is register number from 1 to 7).
FFREE ST <i>n</i>	frees up a register on the stack by marking the register as unused or empty.

Addition and subtraction

Each of the addition instructions compute the sum of ST0 and another operand. The result is always stored in a coprocessor register.

FADD <i>src</i>	ST0 += <i>src</i> . The <i>src</i> may be any coprocessor register or a single or double precision number in memory.
FADD <i>dest</i> , ST0	<i>dest</i> += ST0. The <i>dest</i> may be any coprocessor register.
FADDP <i>dest</i> or FADDP <i>dest</i> , ST0	<i>dest</i> += ST0 then pop stack. The <i>dest</i> may be any coprocessor register.
FIADD <i>src</i>	ST0 += (float) <i>src</i> . Adds an integer to ST0. The <i>src</i> must be a word or double word in memory.

There are twice as many subtraction instructions than addition because the order of the operands is important for subtraction (*i.e.*, $a + b = b + a$, but $a - b \neq b - a$!). For each instruction is an alternate one that subtracts in the reverse order. These reverse instructions all end in either R or RP. Figure 6.5 shows a short code snippet that adds up the elements of an array

```

1 segment .bss
2 array      resq SIZE
3 sum        resq 1
4
5 segment .text
6     mov     ecx, SIZE
7     mov     esi, array
8     fldz                    ; ST0 = 0
9 lp:
10    fadd    qword [esi]     ; ST0 += *(esi)
11    add     esi, 8          ; move to next double
12    loop   lp
13    fstp   qword sum       ; store result into sum

```

Figure 6.5: Array sum example

of doubles. On lines 10 and 13, one must specify the size of the memory operand. Otherwise the assembler would not know whether the memory operand was a float (dword) or a double (qword).

FSUB <i>src</i>	ST0 -= <i>src</i> . The <i>src</i> may be any coprocessor register or a single or double precision number in memory.
FSUBR <i>src</i>	ST0 = <i>src</i> - ST0. The <i>src</i> may be any coprocessor register or a single or double precision number in memory.
FSUB <i>dest</i> , ST0	<i>dest</i> -= ST0. The <i>dest</i> may be any coprocessor register.
FSUBR <i>dest</i> , ST0	<i>dest</i> = ST0 - <i>dest</i> . The <i>dest</i> may be any coprocessor register.
FSUBP <i>dest</i> or FSUBP <i>dest</i> , ST0	<i>dest</i> -= ST0 then pop stack. The <i>dest</i> may be any coprocessor register.
FSUBRP <i>dest</i> or FSUBRP <i>dest</i> , ST0	<i>dest</i> = ST0 - <i>dest</i> then pop stack. The <i>dest</i> may be any coprocessor register.
FISUB <i>src</i>	ST0 -= (float) <i>src</i> . Subtracts an integer from ST0. The <i>src</i> must be a word or double word in memory.
FISUBR <i>src</i>	ST0 = (float) <i>src</i> - ST0. Subtracts ST0 from an integer. The <i>src</i> must be a word or double word in memory.

Multiplication and division

The multiplication instructions are completely analogous to the addition instructions.

FMUL <i>src</i>	ST0 *= <i>src</i> . The <i>src</i> may be any coprocessor register or a single or double precision number in memory.
FMUL <i>dest</i> , ST0	<i>dest</i> *= ST0. The <i>dest</i> may be any coprocessor register.
FMULP <i>dest</i> or FMULP <i>dest</i> , ST0	<i>dest</i> *= ST0 then pop stack. The <i>dest</i> may be any coprocessor register.
FIMUL <i>src</i>	ST0 *= (float) <i>src</i> . Multiplies an integer to ST0. The <i>src</i> must be a word or double word in memory.

Not surprisingly, the division instructions are analogous to the subtraction instructions. Division by zero results in an infinity.

FDIV <i>src</i>	ST0 /= <i>src</i> . The <i>src</i> may be any coprocessor register or a single or double precision number in memory.
FDIVR <i>src</i>	ST0 = <i>src</i> / ST0. The <i>src</i> may be any coprocessor register or a single or double precision number in memory.
FDIV <i>dest</i> , ST0	<i>dest</i> /= ST0. The <i>dest</i> may be any coprocessor register.
FDIVR <i>dest</i> , ST0	<i>dest</i> = ST0 / <i>dest</i> . The <i>dest</i> may be any coprocessor register.
FDIVP <i>dest</i> or FDIVP <i>dest</i> , ST0	<i>dest</i> /= ST0 then pop stack. The <i>dest</i> may be any coprocessor register.
FDIVRP <i>dest</i> or FDIVRP <i>dest</i> , ST0	<i>dest</i> = ST0 / <i>dest</i> then pop stack. The <i>dest</i> may be any coprocessor register.
FIDIV <i>src</i>	ST0 /= (float) <i>src</i> . Divides ST0 by an integer. The <i>src</i> must be a word or double word in memory.
FIDIVR <i>src</i>	ST0 = (float) <i>src</i> / ST0. Divides an integer by ST0. The <i>src</i> must be a word or double word in memory.

Comparisons

The coprocessor also performs comparisons of floating point numbers. The FCOM family of instructions does this operation.

```

1 ;   if ( x > y )
2 ;
3     fld    qword [x]      ; ST0 = x
4     fcomp  qword [y]      ; compare ST0 and y
5     fstsw  ax             ; move C bits into FLAGS
6     sahf
7     jna    else_part      ; if x not above y, goto else_part
8 then_part:
9     ; code for then part
10    jmp    end_if
11 else_part:
12    ; code for else part
13 end_if:

```

Figure 6.6: Comparison example

<code>FCOM <i>src</i></code>	compares <code>ST0</code> and <code>src</code> . The <code>src</code> can be a coprocessor register or a float or double in memory.
<code>FCOMP <i>src</i></code>	compares <code>ST0</code> and <code>src</code> , then pops stack. The <code>src</code> can be a coprocessor register or a float or double in memory.
<code>FCOMPP</code>	compares <code>ST0</code> and <code>ST1</code> , then pops stack twice.
<code>FICOM <i>src</i></code>	compares <code>ST0</code> and (float) <code>src</code> . The <code>src</code> can be a word or dword integer in memory.
<code>FICOMP <i>src</i></code>	compares <code>ST0</code> and (float) <code>src</code> , then pops stack. The <code>src</code> a word or dword integer in memory.
<code>FTST</code>	compares <code>ST0</code> and 0.

These instructions change the `C0`, `C1`, `C2` and `C3` bits of the coprocessor status register. Unfortunately, it is not possible for the CPU to access these bits directly. The conditional branch instructions use the `FLAGS` register, not the coprocessor status register. However, it is relatively simple to transfer the bits of the status word into the corresponding bits of the `FLAGS` register using some new instructions:

<code>FSTSW <i>dest</i></code>	Stores the coprocessor status word into either a word in memory or the <code>AX</code> register.
<code>SAHF</code>	Stores the <code>AH</code> register into the <code>FLAGS</code> register.
<code>LAHF</code>	Loads the <code>AH</code> register with the bits of the <code>FLAGS</code> register.

Figure 6.6 shows a short example code snippet. Lines 5 and 6 transfer the `C0`, `C1`, `C2` and `C3` bits of the coprocessor status word into the `FLAGS` register. The bits are transferred so that they are analogous to the result of a comparison of two *unsigned* integers. This is why line 7 uses a `JNA` instruction.

The Pentium Pro (and later processors (Pentium II and III)) support two new comparison operators that directly modify the CPU's FLAGS register.

FCOMI *src* compares ST0 and *src*. The *src* must be a coprocessor register.

FCOMIP *src* compares ST0 and *src*, then pops stack. The *src* must be a coprocessor register.

Figure 6.7 shows an example subroutine that finds the maximum of two doubles using the FCOMIP instruction. Do not confuse these instructions with the integer comparison functions (FICOM and FICOMP).

Miscellaneous instructions

This section covers some other miscellaneous instructions that the coprocessor provides.

FCHS ST0 = - ST0 Changes the sign of ST0

FABS ST0 = |ST0| Takes the absolute value of ST0

FSQRT ST0 = $\sqrt{\text{ST0}}$ Takes the square root of ST0

FSCALE ST0 = ST0 $\times 2^{\text{ST1}}$ multiplies ST0 by a power of 2 quickly. ST1 is not removed from the coprocessor stack. Figure 6.8 shows an example of how to use this instruction.

6.3.3 Examples

6.3.4 Quadratic formula

The first example shows how the quadratic formula can be encoded in assembly. Recall that the quadratic formula computes the solutions to the quadratic equation:

$$ax^2 + bx + c = 0$$

The formula itself gives two solutions for x : x_1 and x_2 .

$$x_1, x_2 = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

The expression inside the square root ($b^2 - 4ac$) is called the *discriminant*. Its value is useful in determining which of the following three possibilities are true for the solutions.

1. There is only one real degenerate solution. $b^2 - 4ac = 0$
2. There are two real solutions. $b^2 - 4ac > 0$
3. There are two complex solutions. $b^2 - 4ac < 0$

Here is a small C program that uses the assembly subroutine:

```

                                quad.c
1  #include <stdio.h>
2
3  int quadratic( double, double, double, double *, double *);
4
5  int main()
6  {
7      double a,b,c, root1, root2;
8
9      printf("Enter a, b, c: ");
10     scanf("%lf %lf %lf", &a, &b, &c);
11     if (quadratic( a, b, c, &root1, &root2 )
12         printf(" roots: %.10g %.10g\n", root1, root2);
13     else
14         printf("No real roots\n");
15     return 0;
16 }

```

quad.c

Here is the assembly routine:

```

                                quad.asm
1  ; function quadratic
2  ; finds solutions to the quadratic equation:
3  ;      a*x^2 + b*x + c = 0
4  ; C prototype:
5  ;   int quadratic( double a, double b, double c,
6  ;                  double * root1, double *root2 )
7  ; Parameters:
8  ;   a, b, c - coefficients of powers of quadratic equation (see above)
9  ;   root1  - pointer to double to store first root in
10 ;   root2  - pointer to double to store second root in
11 ; Return value:
12 ;   returns 1 if real roots found, else 0
13
14 %define a          qword [ebp+8]
15 %define b          qword [ebp+16]
16 %define c          qword [ebp+24]
17 %define root1     dword [ebp+32]
18 %define root2     dword [ebp+36]
19 %define disc      qword [ebp-8]
20 %define one_over_2a qword [ebp-16]

```

```

21
22 segment .data
23 MinusFour      dw      -4
24
25 segment .text
26     global _quadratic
27 _quadratic:
28     push     ebp
29     mov     ebp, esp
30     sub     esp, 16      ; allocate 2 doubles (disc & one_over_2a)
31     push     ebx        ; must save original ebx
32
33     fld     word [MinusFour]; stack -4
34     fld     a           ; stack: a, -4
35     fld     c           ; stack: c, a, -4
36     fmulp  st1         ; stack: a*c, -4
37     fmulp  st1         ; stack: -4*a*c
38     fld     b
39     fld     b           ; stack: b, b, -4*a*c
40     fmulp  st1         ; stack: b*b, -4*a*c
41     faddp  st1         ; stack: b*b - 4*a*c
42     ftst
43     fstsw  ax          ; test with 0
44     sahf
45     jb     no_real_solutions ; if disc < 0, no real solutions
46     fsqrt
47     fstp   disc        ; stack: sqrt(b*b - 4*a*c)
48     fstp   disc        ; store and pop stack
49     fld1
50     fld     a           ; stack: 1.0
51     fscale
52     fdivp  st1         ; stack: a * 2^(1.0) = 2*a, 1
53     fst    one_over_2a ; stack: 1/(2*a)
54     fld     b           ; stack: b, 1/(2*a)
55     fld     disc        ; stack: disc, b, 1/(2*a)
56     fsubrp st1         ; stack: disc - b, 1/(2*a)
57     fmulp  st1         ; stack: (-b + disc)/(2*a)
58     mov     ebx, root1
59     fstp   qword [ebx] ; store in *root1
60     fld     b           ; stack: b
61     fld     disc        ; stack: disc, b
62     fchs
63     fsubrp st1         ; stack: -disc, b
64     fsubrp st1         ; stack: -disc - b

```

```

63      fmul   one_over_2a      ; stack: (-b - disc)/(2*a)
64      mov    ebx, root2
65      fstp   qword [ebx]     ; store in *root2
66      mov    eax, 1          ; return value is 1
67      jmp    short quit
68
69 no_real_solutions:
70      mov    eax, 0          ; return value is 0
71
72 quit:
73      pop    ebx
74      mov    esp, ebp
75      pop    ebp
76      ret

```

quad.asm

6.3.5 Reading array from file

In this example, an assembly routine reads doubles from a file. Here is a short C test program:

readt.c

```

1  /*
2  * This program tests the 32-bit read_doubles() assembly procedure.
3  * It reads the doubles from stdin. (Use redirection to read from file.)
4  */
5  #include <stdio.h>
6  extern int read_doubles( FILE *, double *, int );
7  #define MAX 100
8
9  int main()
10 {
11     int i,n;
12     double a[MAX];
13
14     n = read_doubles(stdin , a , MAX);
15
16     for( i=0; i < n; i++ )
17         printf ("%3d %g\n", i, a[i]);
18     return 0;
19 }

```

readt.c

Here is the assembly routine

```

_____ read.asm _____
1 segment .data
2 format db      "%lf", 0      ; format for fscanf()
3
4 segment .text
5     global  _read_doubles
6     extern  _fscanf
7
8     %define SIZEOF_DOUBLE  8
9     %define FP              dword [ebp + 8]
10    %define ARRAYP         dword [ebp + 12]
11    %define ARRAY_SIZE    dword [ebp + 16]
12    %define TEMP_DOUBLE   [ebp - 8]
13
14    ;
15    ; function _read_doubles
16    ; C prototype:
17    ; int read_doubles( FILE * fp, double * arrayp, int array_size );
18    ; This function reads doubles from a text file into an array, until
19    ; EOF or array is full.
20    ; Parameters:
21    ; fp          - FILE pointer to read from (must be open for input)
22    ; arrayp      - pointer to double array to read into
23    ; array_size - number of elements in array
24    ; Return value:
25    ; number of doubles stored into array (in EAX)
26
27    _read_doubles:
28        push    ebp
29        mov     ebp,esp
30        sub     esp, SIZEOF_DOUBLE      ; define one double on stack
31
32        push    esi                    ; save esi
33        mov     esi, ARRAYP            ; esi = ARRAYP
34        xor     edx, edx                ; edx = array index (initially 0)
35
36    while_loop:
37        cmp     edx, ARRAY_SIZE        ; is edx < ARRAY_SIZE?
38        jnl    short quit              ; if not, quit loop
39    ;
40    ; call fscanf() to read a double into TEMP_DOUBLE

```

```

41 ; fscanf() might change edx so save it
42 ;
43     push    edx                ; save edx
44     lea    eax, TEMP_DOUBLE
45     push    eax                ; push &TEMP_DOUBLE
46     push    dword format      ; push &format
47     push    FP                ; push file pointer
48     call   _fscanf
49     add    esp, 12
50     pop    edx                ; restore edx
51     cmp    eax, 1             ; did fscanf return 1?
52     jne    short quit        ; if not, quit loop
53
54 ;
55 ; copy TEMP_DOUBLE into ARRAYP[edx]
56 ; (The 8-bytes of the double are copied by two 4-byte copies)
57 ;
58     mov    eax, [ebp - 8]
59     mov    [esi + 8*edx], eax  ; first copy lowest 4 bytes
60     mov    eax, [ebp - 4]
61     mov    [esi + 8*edx + 4], eax ; next copy highest 4 bytes
62
63     inc    edx
64     jmp    while_loop
65
66 quit:
67     pop    esi                ; restore esi
68
69     mov    eax, edx          ; store return value into eax
70
71     mov    esp, ebp
72     pop    ebp
73     ret

```

6.3.6 Finding primes

This final example looks at finding prime numbers again. This implementation is more efficient than the previous one. It stores the primes it has found in an array and only divides by the previous primes it has found instead of every odd number to find new primes.

One other difference is that it computes the square root of the guess for the next prime to determine at what point it can stop searching for factors.

It alters the coprocessor control word so that it that when it stores the square root as an integer, it truncates instead of rounding. This is controlled by bits 10 and 11 of the control word. This bits are called the RC (Rounding Control) bits. If they are both 0 (the default), the coprocessor rounds when converting to integer. If they are both 1, the coprocessor truncates integer conversions. Notice that the routine is careful to save the original control word and restore it before it returns.

Here is the C driver program:

```

_____ fprime.c _____
1  #include <stdio.h>
2  #include <stdlib.h>
3  /*
4   * function find_primes
5   * finds the indicated number of primes
6   * Parameters:
7   *   a – array to hold primes
8   *   n – how many primes to find
9   */
10 extern void find_primes ( int * a, unsigned n );
11
12 int main()
13 {
14     int status;
15     unsigned i;
16     unsigned max;
17     int * a;
18
19     printf ("How many primes do you wish to find? ");
20     scanf ("%u", &max);
21
22     a = calloc ( sizeof(int), max);
23
24     if ( a ) {
25
26         find_primes (a, max);
27
28         /* print out the last 20 primes found */
29         for(i = ( max > 20 ) ? max - 20 : 0; i < max; i++ )
30             printf ("%3d %d\n", i+1, a[i]);
31
32         free (a);
33         status = 0;

```

```

34 }
35 else {
36     fprintf (stderr , "Can not create array of %u ints\n", max);
37     status = 1;
38 }
39
40 return status;
41 }

```

fprime.c

Here is the assembly routine:

```

1 segment .text
2     global _find_primes
3 ;
4 ; function find_primes
5 ; finds the indicated number of primes
6 ; Parameters:
7 ;   array - array to hold primes
8 ;   n_find - how many primes to find
9 ; C Prototype:
10 ;extern void find_primes( int * array, unsigned n_find )
11 ;
12 %define array          ebp + 8
13 %define n_find        ebp + 12
14 %define n              ebp - 4          ; number of primes found so far
15 %define isqrt         ebp - 8          ; floor of sqrt of guess
16 %define orig_cntl_wd  ebp - 10         ; original control word
17 %define new_cntl_wd   ebp - 12         ; new control word
18
19 _find_primes:
20     enter    12,0                      ; make room for local variables
21
22     push    ebx                          ; save possible register variables
23     push    esi
24
25     fstcw   word [orig_cntl_wd]         ; get current control word
26     mov     ax, [orig_cntl_wd]
27     or     ax, 0C00h                    ; set rounding bits to 11 (truncate)
28     mov     [new_cntl_wd], ax
29     fldcw   word [new_cntl_wd]

```

```

30
31     mov     esi, [array]           ; esi points to array
32     mov     dword [esi], 2         ; array[0] = 2
33     mov     dword [esi + 4], 3     ; array[1] = 3
34     mov     ebx, 5                 ; ebx = guess = 5
35     mov     dword [n], 2          ; n = 2
36 ;
37 ; This outer loop finds a new prime each iteration, which it adds to the
38 ; end of the array. Unlike the earlier prime finding program, this function
39 ; does not determine primeness by dividing by all odd numbers. It only
40 ; divides by the prime numbers that it has already found. (That's why they
41 ; are stored in the array.)
42 ;
43 while_limit:
44     mov     eax, [n]
45     cmp     eax, [n_find]          ; while ( n < n_find )
46     jnb    short quit_limit
47
48     mov     ecx, 1                 ; ecx is used as array index
49     push   ebx                     ; store guess on stack
50     fld   dword [esp]              ; load guess onto coprocessor stack
51     pop    ebx                     ; get guess off stack
52     fsqrt                                ; find sqrt(guess)
53     fistp  dword [isqrt]           ; isqrt = floor(sqrt(guess))
54 ;
55 ; This inner loop divides guess (ebx) by earlier computed prime numbers
56 ; until it finds a prime factor of guess (which means guess is not prime)
57 ; or until the prime number to divide is greater than floor(sqrt(guess))
58 ;
59 while_factor:
60     mov     eax, dword [esi + 4*ecx] ; eax = array[ecx]
61     cmp     eax, [isqrt]            ; while ( isqrt < array[ecx]
62     jnbe   short quit_factor_prime
63     mov     eax, ebx
64     xor    edx, edx
65     div   dword [esi + 4*ecx]
66     or     edx, edx                ; && guess % array[ecx] != 0 )
67     jz    short quit_factor_not_prime
68     inc    ecx                     ; try next prime
69     jmp   short while_factor
70
71 ;

```



```
72 ; found a new prime !
73 ;
74 quit_factor_prime:
75     mov     eax, [n]
76     mov     dword [esi + 4*eax], ebx     ; add guess to end of array
77     inc     eax
78     mov     [n], eax                     ; inc n
79
80 quit_factor_not_prime:
81     add     ebx, 2                         ; try next odd number
82     jmp     short while_limit
83
84 quit_limit:
85
86     fldcw  word [orig_cntl_wd]           ; restore control word
87     pop     esi                           ; restore register variables
88     pop     ebx
89
90     leave
91     ret
```

prime2.asm

```
1 global _dmax
2
3 segment .text
4 ; function _dmax
5 ; returns the larger of its two double arguments
6 ; C prototype
7 ; double dmax( double d1, double d2 )
8 ; Parameters:
9 ;   d1 - first double
10 ;   d2 - second double
11 ; Return value:
12 ;   larger of d1 and d2 (in ST0)
13 %define d1    ebp+8
14 %define d2    ebp+16
15 _dmax:
16     enter    0, 0
17
18     fld     qword [d2]
19     fld     qword [d1]           ; ST0 = d1, ST1 = d2
20     fcomip  st1                 ; ST0 = d2
21     jna     short d2_bigger
22     fcomp   st0                 ; pop d2 from stack
23     fld     qword [d1]           ; ST0 = d1
24     jmp     short exit
25 d2_bigger:                       ; if d2 is max, nothing to do
26 exit:
27     leave
28     ret
```

Figure 6.7: FCOMIP example

```
1 segment .data
2 x          dq  2.75          ; converted to double format
3 five       dw  5
4
5 segment .text
6     fld    dword [five]      ; ST0 = 5
7     fld    qword [x]         ; ST0 = 2.75, ST1 = 5
8     fscale                                ; ST0 = 2.75 * 32, ST1 = 5
```

Figure 6.8: FSCALE example

Chapter 7

Structures and C++

7.1 Structures

7.1.1 Introduction

Structures are used in C to group together related data into a composite variable. This technique has several advantages:

1. It clarifies the code by showing that the data defined in the structure are intimately related.
2. It simplifies passing the data to functions. Instead of passing multiple variables separately, they can be passed as a single unit.
3. It increases the *locality*¹ of the code.

From the assembly standpoint, a structure can be considered as an array with elements of *varying* size. The elements of real arrays are always the same size and type. This property is what allows one to calculate the address of any element by knowing the starting address of the array, the size of the elements and the desired element's index.

A structure's elements do not have to be the same size (and usually are not). Because of this each element of a structure must be explicitly specified and is given a *tag* (or name) instead of a numerical index.

In assembly, the element of a structure will be accessed in a similar way as an element of an array. To access an element, one must know the starting address of the structure and the *relative offset* of that element from the beginning of the structure. However, unlike an array where this offset can be calculated by the index of the element, the element of a structure is assigned an offset by the compiler.

¹See the virtual memory management section of any Operating System text book for discussion of this term.

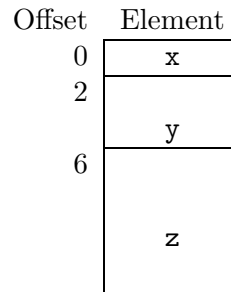


Figure 7.1: Structure S

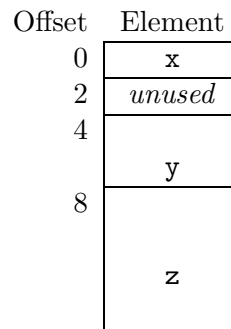


Figure 7.2: Structure S

For example, consider the following structure:

```

struct S {
  short int x;    /* 2-byte integer */
  int        y;   /* 4-byte integer */
  double    z;   /* 8-byte float  */
};

```

Figure 7.1 shows how a variable of type `S` might look in the computer's memory. The ANSI C standard states that the elements of a structure are arranged in the memory in the same order as they are defined in the `struct` definition. It also states that the first element is at the very beginning of the structure (*i.e.*, offset zero). It also defines another useful macro in the `stddef.h` header file named `offsetof()`. This macro computes and returns the offset of any element of a structure. The macro takes two parameters, the first is the name of the *type* of the structure, the second is the name of the element to find the offset of. Thus, the result of `offsetof(S, y)` would be 2 from Figure 7.1.

7.1.2 Memory alignment

If one uses the `offsetof` macro to find the offset of `y` using the `gcc` compiler, they will find that it returns 4, not 2! Why? Because `gcc` (and many other compilers) align variables on double word boundaries by default. In 32-bit protected mode, the CPU reads memory faster if the data starts at a double word boundary. Figure 7.2 shows how the `S` structure really looks using `gcc`. The compiler inserts two unused bytes into the structure to align `y` (and `z`) on a double word boundary. This shows why it is a good idea to use `offsetof` to compute the offsets instead of calculating them oneself when using structures defined in C.

Recall that an address is on a double word boundary if it is divisible by 4

Of course, if the structure is only used in assembly, the programmer can determine the offsets himself. However, if one is interfacing C and assembly, it is very important that both the assembly code and the C code agree on the offsets of the elements of the structure! One complication is that different C compilers may give different offsets to the elements. For example, as we have seen, the `gcc` compiler creates a `S` structure that looks like Figure 7.2; however, Borland's compiler would create a structure that looked like Figure 7.1. C compilers provide ways to specify the alignment used for data. However, the ANSI C standard does not specify how this will be done and thus, different compilers do it differently. Borland's compiler has a flag, `-a`, that can be used to define the alignment used for all data. Compiling with `-a 4` tells `bcc` to use double word alignment. Microsoft's compiler provides a `#pragma pack` directive that can be used to set the alignment (consult Microsoft's documentation for details).

The `gcc` compiler has a flexible and complicated method of specifying the alignment. The compiler allows one to specify the alignment of any type using a special syntax. For example, the following line:

```
typedef short int unaligned_int __attribute__((aligned (1)));
```

defines a new type named `unaligned_int` that is aligned on byte boundaries. (Yes, all the parenthesis after `__attribute__` are required!) The 1 in the `aligned` parameter can be replaced with other powers of two to specify other alignments. (2 for word alignment, 4 for double word alignment, *etc.*) If the `y` element of the was changed to be an `unaligned_int` type, `gcc` would put `y` at offset 2. However, `z` would still be at offset 8 since doubles are also double word aligned by default. The definition of `z`'s type would have to be changed as well for it to put at offset 6.

7.1.3 Using structures in assembly

As discussed above, accessing a structure in assembly is very much like accessing an array. For a simple example, consider how one would write an assembly routine that would zero out the `y` element of a `S` structure.

Assuming the prototype of the routine would be:

```
void zero_y( S * s_p );
```

the assembly routine would be:

```

1  %define      y_offset  4
2  _zero_y:
3      enter   0,0
4      mov     eax, [ebp + 8]      ; get s_p (struct pointer) from stack
5      mov     dword [eax + y_offset], 0
6      leave
7      ret

```

C allows one to pass a structure by value to a function; however, this is almost always a bad idea. When passed by value, the entire data in the structure must be copied to the stack and then retrieved by the routine. It is much more efficient to pass a pointer to a structure instead.

C also allows a structure type to be used as the return value of a function. Obviously a structure can not be returned in the EAX register. Different compilers handle this situation differently. A common solution that compilers use is to internally rewrite the function as one that takes a structure pointer as a parameter. The pointer is used to put the return value into a structure defined outside of the routine called.

Most assemblers (including NASM) have built-in support for defining structures in your assembly code. Consult your documentation for details.

7.2 Assembly and C++

The C++ programming language is an extension of the C language. Many of the basic rules of interfacing C and assembly language also apply to C++. However, some rules need to be modified. Also, some of the extensions of C++ are easier to understand with an knowledge of assembly language. This section assumes a basic knowledge of C++.

7.2.1 Overloading and Name Mangling

C++ allows different functions (and class member functions) with the same name to be defined. When more than one function share the same name, the functions are said to be *overloaded*. If two functions are defined with the same name in C, the linker will produce an error because it will find two definitions for the same symbol in the object files it is linking. For example, consider the code in Figure 7.3. The equivalent assembly code would define two labels named `_f` which will obviously be an error.


```

1 #include <stdio.h>
2
3 void f( int x )
4 {
5     printf ("%d\n", x);
6 }
7
8 void f( double x )
9 {
10    printf ("%g\n", x);
11 }

```

Figure 7.3: Two `f()` functions

C++ uses the same linking process as C, but avoids this error by performing *name mangling* or modifying the symbol used to label the function. In a way, C already uses name mangling, too. It adds an underscore to the name of the C function when creating the label for the function. However, C will mangle the name of both functions in Figure 7.3 the same way and produce an error. C++ uses a more sophisticated mangling process that produces two different labels for the functions. For example, the first function in Figure 7.3 would be assigned by DJGPP the label `_f_Fi` and the second function, `_f_Fd`. This avoids any linker errors.

Unfortunately, there is no standard for how to manage names in C++ and different compilers mangle names differently. For example, Borland C++ would use the labels `@f$qi` and `@f$qd` for the two functions in Figure 7.3. However, the rules are not completely arbitrary. The mangled name encodes the *signature* of the function. The signature of a function is defined by the order and the type of its parameters. Notice that the function that takes a single `int` argument has an *i* at the end of its mangled name (for both DJGPP and Borland) and that the one that takes a `double` argument has a *d* at the end of its mangled name. If there was a function named `f` with the prototype:

```
void f( int x, int y, double z);
```

DJGPP would mangle its name to be `_f_Fiid` and Borland to `@f$qiid`.

The return type of the function is *not* part of a function's signature and is not encoded in its mangled name. This fact explains a rule of overloading in C++. Only functions whose signatures are unique may be overloaded. As one can see, if two functions with the same name and signature are defined in C++, they will produce the same mangled name and will create a linker error. By default, all C++ functions are name mangled, even ones that are

not overloaded. When it is compiling a file, the compiler has no way of whether a particular function is overloaded or not, so it mangles all names. In fact, it also mangles the names of global variables as well by encoding the type of the variable in a similar way as function signatures. Thus, if one defines a global variable in one file as a certain type and then tries to use in another file as the wrong type, a linker error will be produced. This characteristic of C++ is known as *typesafe linking*. It also exposes another type of error, inconsistent prototypes. This occurs when the definition of a function in one module does not agree with the prototype used by another module. In C, this can be a very difficult problem to debug. C does not catch this error. The program will compile and link, but will have undefined behavior as the calling code will be pushing different types on the stack than the function expects. In C++, it will produce a linker error.

When the C++ compiler is parsing a function call, it looks for a matching function by looking at the types of the arguments passed to the function². If it finds a match, it then creates a `CALL` to the correct function using the compiler's name mangling rules.

Since different compilers use different name mangling rules, C++ code compiled by different compilers may not be able to be linked together. This fact is important when considering using a precompiled C++ library! If one wishes to write a function in assembly that will be used with C++ code, she must know the name mangling rules for the C++ compiler to be used (or use the technique explained below).

The astute student may question whether the code in Figure 7.3 will work as expected. Since C++ name mangles all functions, then the `printf` function will be mangled and the compiler will not produce a `CALL` to the label `_printf`. This is a valid concern! If the prototype for `printf` was simply placed at the top of the file, this would happen. The prototype is:

```
int printf ( const char *, ...);
```

DJGPP would mangle this to be `_printf_FPCce`. (The `F` is for *function*, `P` for *pointer*, `C` for *const*, `c` for *char* and `e` for ellipsis.) This would not call the regular C library's `printf` function! Of course, there must be a way for C++ code to call C code. This is very important because there is *a lot* of useful old C code around. In addition to allowing one to call legacy C code, C++ also allows one to call assembly code using the normal C mangling conventions.

C++ extends the `extern` keyword to allow it to specify that the function or global variable it modifies uses the normal C conventions. In C++ terminology, the function or global variable uses *C linkage*. For example, to

²The match does not have to be an exact match, the compiler will consider matches made by casting the arguments. The rules for this process are beyond the scope of this book. Consult a C++ book for details.

```

1 void f( int & x )    // the & denotes a reference parameter
2 { x++; }
3
4 int main()
5 {
6     int y = 5;
7     f(y);           // reference to y is passed, note no & here!
8     printf ("%d\n", y); // prints out 6!
9     return 0;
10 }

```

Figure 7.4: Reference example

declare `printf` to have C linkage, use the prototype:

```
extern "C" int printf ( const char *, ... );
```

This instructs the compiler not to use the C++ name mangling rules on this function, but instead to use the C rules. However, by doing this, the `printf` function may not be overloaded. This provides the easiest way to interface C++ and assembly, define the function to use C linkage and then use the C calling convention.

For convenience, C++ also allows the linkage of a block of functions and global variables to be defined. The block is denoted by the usual curly braces.

```
extern "C" {
    /* C linkage global variables and function prototypes */
}
```

If one examines the ANSI C header files that come with C/C++ compilers today, they will find the following near the top of each header file:

```
#ifdef _cplusplus
extern "C" {
#endif
```

And a similar construction near the bottom containing a closing curly brace. C++ compilers define the `_cplusplus` macro (with *two* leading underscores). The snippet above encloses the entire header file within an `extern "C"` block if the header file is compiled as C++, but does nothing if compiled as C (since a C compiler would give a syntax error for `extern "C"`). This same technique can be used by any programmer to create a header file for assembly routines that can be used with either C or C++.

7.2.2 References

References are another new feature of C++. They allow one to pass parameters to functions without explicitly using pointers. For example, consider the code in Figure 7.4. Actually, reference parameters are pretty simple, they really are just pointers. The compiler just hides this from the programmer (just as Pascal compilers implement `var` parameters as pointers). When the compiler generates assembly for the function call on line 7, it passes the *address* of `y`. If one was writing function `f` in assembly, they would act as if the prototype was³:

```
void f ( int * xp);
```

References are just a convenience that are especially useful for operator overloading. This is another feature of C++ that allows one to define meanings for common operators on structure or class types. For example, a common use is to define the plus (+) operator to concatenate string objects. Thus, if `a` and `b` were strings, `a + b` would return the concatenation of the strings `a` and `b`. C++ would actually call a function to do this (in fact, these expression could be rewritten in function notation as `operator +(a,b)`). For efficiency, one would like to pass the address of the string objects instead of passing them by value. Without references, this could be done as `operator +(&a,&b)`, but this would require one to write in operator syntax as `&a + &b`. This would be very awkward and confusing. However, by using references, one can write it as `a + b`, which looks very natural.

7.2.3 Inline functions

Inline functions are yet another feature of C++⁴. Inline functions are meant to replace the error-prone, preprocessor-based macros that take parameters. Recall from C, that writing a macro that squares a number might look like:

```
#define SQR(x) ((x)*(x))
```

Because the preprocessor does not understand C and does simple substitutions, the parenthesis are required to compute the correct answer in most cases. However, even this version will not give the correct answer for `SQR(x++)`.

Macros are used because they eliminate the overhead of making a function call for a simple function. As the chapter on subprograms demonstrated, performing a function call involves several steps. For a very simple function, the time it takes to make the function call may be more than the time to actually perform the operations in the function! Inline functions are a much

³Of course, they might want to declare the function with C linkage to avoid name mangling as discussed in Section 7.2.1

⁴ C compilers often support this feature as an extension of ANSI C

```

1 inline int inline_f ( int x )
2 { return x*x; }
3
4 int f( int x )
5 { return x*x; }
6
7 int main()
8 {
9   int y, x = 5;
10  y = f(x);
11  y = inline_f (x);
12  return 0;
13 }
```

Figure 7.5: Inlining example

more friendly way to write code that looks like a normal function, but that does *not* CALL a common block of code. Instead, calls to inline functions are replaced by code that performs the function. C++ allows a function to be made inline by placing the keyword `inline` in front of the function definition. For example, consider the functions declared in Figure 7.5. The call to function `f` on line 10 does a normal function call (in assembly, assuming `x` is at address `ebp-8` and `y` is at `ebp-4`):

```

1   push   dword [ebp-8]
2   call   _f
3   pop    ecx
4   mov    [ebp-4], eax
```

However, the call to function `inline_f` on line 11 would look like:

```

1   mov    eax, [ebp-8]
2   imul  eax, eax
3   mov    [ebp-4], eax
```

In this case, there are two advantages to inlining. First, the inline function is faster. No parameters are pushed on the stack, no stack frame is created and then destroyed, no branch is made. Secondly, the inline function call uses less code! This last point is true for this example, but does not hold true in all cases.

```
1 class Simple {  
2 public:  
3     Simple();           // default constructor  
4     ~Simple();         // destructor  
5     int get_data() const; // member functions  
6     void set_data( int );  
7 private:  
8     int data;         // member data  
9 };  
10  
11 Simple::Simple()  
12 { data = 0; }  
13  
14 Simple::~~Simple()  
15 { /* null body */ }  
16  
17 int Simple::get_data() const  
18 { return data; }  
19  
20 void Simple::set_data( int x )  
21 { data = x; }
```

Figure 7.6: A simple C++ class

The main disadvantage of inlining is that inline code is not linked and so the code of an inline function must be available to *all* files that use it. The previous example assembly code shows this. The call of the non-inline function only requires knowledge of the parameters, the return value type, calling convention and the name of the label for the function. All this information is available from the prototype of the function. However, using the inline function requires knowledge of all the code of the function. This means that if *any* part of an inline function is changed, *all* source files that use the function must be recompiled. Recall that for non-inline functions, if the prototype does not change, often the files that use the function need not be recompiled. For all these reasons, the code for inline functions are usually placed in header files. This practice is contrary to the normal hard and fast rule in C that executable code statements are *never* placed in header files.

```

void set_data ( Simple * object , int x )
{
    object->data = x;
}

```

Figure 7.7: C Version of Simple::set_data()

```

1  _set_data__6Simplei:          ; mangled name
2      push    ebp
3      mov     ebp, esp
4
5      mov     eax, [ebp + 8]    ; eax = pointer to object (this)
6      mov     edx, [ebp + 12]  ; edx = integer parameter
7      mov     [eax], edx      ; data is at offset 0
8
9      leave
10     ret

```

Figure 7.8: Compiler output of Simple::set_data(int)

7.2.4 Classes

A C++ class describes a type of *object*. An object has both data members and function members⁵. In other words, it's a **struct** with data and functions associated with it. Consider the simple class defined in Figure 7.6. A variable of **Simple** type would look just like a normal C **struct** with a single **int** member. The functions are *not* stored in memory assigned to the structure. However, member functions are different from other functions. They are passed a *hidden* parameter. This parameter is a pointer to the object that the member function is acting on.

*Actually, C++ uses the **this** keyword to access the pointer to the object acted on from inside the member function.*

For example, consider the **set_data** method of the **Simple** class of Figure 7.6. If it was written in C, it would look like a function that was passed explicitly passed a pointer to the object being acted on as the code in Figure 7.7 shows. The **-S** switch on the *DJGPP* compiler (and the *gcc* and Borland compilers as well) tells the compiler to produce an assembly file containing the equivalent assembly language for the code produced. For *DJGPP* and *gcc* the assembly file ends in an **.s** extension and unfortunately uses AT&T assembly language syntax which is quite different from NASM and MASM syntaxes⁶. (Borland and MS compilers generate a file

⁵Often called *member functions* in C++ or more generally *methods*.

⁶The *gcc* compiler system includes its own assembler called *gas*. The *gas* assembler

with a `.asm` extension using MASM syntax.) Figure 7.8 shows the output of *DJGPP* converted to NASM syntax and with comments added to clarify the purpose of the statements. On the very first line, note that the `set_data` method is assigned a mangled label that encodes the name of the method, the name of the class and the parameters. The name of the class is encoded because other classes might have a method named `set_data` and the two methods *must* be assigned different labels. The parameters are encoded so that the class can overload the `set_data` method to take other parameters just as normal C++ functions. However, just as before, different compilers will encode this information differently in the mangled label.

Next on lines 2 and 3, the familiar function prologue appears. On line 5, the first parameter on the stack is stored into `EAX`. This is *not* the `x` parameter! Instead it is the hidden parameter⁷ that points to the object being acted on. Line 6 stores the `x` parameter into `EDX` and line 7 stores `EDX` into the double word that `EAX` points to. This is the `data` member of the `Simple` object being acted on, which being the only data in the class, is stored at offset 0 in the `Simple` structure.

Example

This section uses the ideas of the chapter to create a C++ class that represents an unsigned integer of arbitrary size. Since the integer can be any size, it will be stored in an array of unsigned integers (double words). It can be made any size by using dynamical allocation. The double words are stored in little endian order (*i.e.*, the least significant double word is at index 0). Figure 7.9 shows the definition of the `Big_int` class⁸. The size of a `Big_int` is measured by the size of the `unsigned` array that is used to store its data. The `size_` data member of the class is assigned offset zero and the `number_` member is assigned offset 4.

To simplify these example, only object instances with the same size arrays can be added to or subtracted from each other.

The class has three constructors: the first (line 9) initializes the class instance by using a normal unsigned integer; the second (line 18) initializes the instance by using a string that contains a hexadecimal value. The third constructor (line 21) is the *copy constructor*.

This discussion focuses on how the addition and subtraction operators

uses AT&T syntax and thus the compiler outputs the code in the format for *gas*. There are several pages on the web that discuss the differences in INTEL and AT&T formats. There is also a free program named `a2i` (<http://www.multimania.com/placr/a2i.html>), that converts AT&T format to NASM format.

⁷As usual, *nothing* is hidden in the assembly code!

⁸See the code example source for the complete code for this example. The text will only refer to some of the code.


```

1  class Big_int {
2  public:
3      /*
4       * Parameters:
5       *   size           – size of integer expressed as number of
6       *                   normal unsigned int 's
7       *   initial_value – initial value of Big_int as a normal unsigned int
8       */
9      explicit Big_int ( size_t   size ,
10                       unsigned initial_value = 0);
11
12     /*
13     * Parameters:
14     *   size           – size of integer expressed as number of
15     *                   normal unsigned int 's
16     *   initial_value – initial value of Big_int as a string holding
17     *                   hexadecimal representation of value.
18     */
19     Big_int ( size_t   size ,
20              const char * initial_value );
21
22     Big_int ( const Big_int & big_int_to_copy );
23     ~Big_int ();
24
25     // returns size of Big_int (in terms of unsigned int 's)
26     size_t size () const;
27
28     const Big_int & operator = ( const Big_int & big_int_to_copy );
29     friend Big_int operator + ( const Big_int & op1,
30                                const Big_int & op2 );
31     friend Big_int operator – ( const Big_int & op1,
32                                const Big_int & op2);
33     friend bool operator == ( const Big_int & op1,
34                               const Big_int & op2 );
35     friend bool operator < ( const Big_int & op1,
36                              const Big_int & op2);
37     friend ostream & operator << ( ostream &   os,
38                                     const Big_int & op );
39 private:
40     size_t   size_ ;    // size of unsigned array
41     unsigned * number_ ; // pointer to unsigned array holding value
42 };

```

Figure 7.9: Definition of Big_int class

```
1 // prototypes for assembly routines
2 extern "C" {
3     int add_big_ints ( Big_int &      res ,
4                       const Big_int & op1,
5                       const Big_int & op2);
6     int sub_big_ints ( Big_int &      res ,
7                       const Big_int & op1,
8                       const Big_int & op2);
9 }
10
11 inline Big_int operator + ( const Big_int & op1, const Big_int & op2)
12 {
13     Big_int result (op1.size ());
14     int res = add_big_ints ( result , op1, op2);
15     if ( res == 1)
16         throw Big_int :: Overflow ();
17     if ( res == 2)
18         throw Big_int :: Size_mismatch ();
19     return result ;
20 }
21
22 inline Big_int operator - ( const Big_int & op1, const Big_int & op2)
23 {
24     Big_int result (op1.size ());
25     int res = sub_big_ints ( result , op1, op2);
26     if ( res == 1)
27         throw Big_int :: Overflow ();
28     if ( res == 2)
29         throw Big_int :: Size_mismatch ();
30     return result ;
31 }
```

Figure 7.10: Big_int Class Arithmetic Code

work since this is where the assembly language is used. Figure 7.10 shows the relevant parts of the header file for these operators. They show how the operators are set up to call the assembly routines. Since different compilers use radically different mangling rules for operator functions, inline operator functions are used to set up a calls to C linkage assembly routines. This makes it relatively easy to port to different compilers and is just as fast as direct calls. This technique also eliminates the need to throw an exception from assembly!

Why is assembly used at all here? Recall that to perform multiple precision arithmetic, the carry must be moved from one dword to be added to the next significant dword. C++ (and C) do not allow the programmer to access the CPU's carry flag. Performing the addition could only be done by using C++ to independently recalculate the carry flag and conditionally add it to the next dword. It is much more efficient to write the code in assembly where the carry flag can be accessed and using the ADC instruction which automatically adds the carry flag in makes a lot of sense.

For brevity, only the `add_big_ints` assembly routine will be discussed here. Below is the code for this routine (from `big_math.asm`):

```

----- big_math.asm -----
1 segment .text
2     global  add_big_ints, sub_big_ints
3 #define size_offset 0
4 #define number_offset 4
5
6 #define EXIT_OK 0
7 #define EXIT_OVERFLOW 1
8 #define EXIT_SIZE_MISMATCH 2
9
10 ; Parameters for both add and sub routines
11 #define res ebp+8
12 #define op1 ebp+12
13 #define op2 ebp+16
14
15 add_big_ints:
16     push    ebp
17     mov     ebp, esp
18     push    ebx
19     push    esi
20     push    edi
21     ;
22     ; first set up esi to point to op1
23     ;             edi to point to op2

```

```

24         ;           ebx to point to res
25     mov     esi, [op1]
26     mov     edi, [op2]
27     mov     ebx, [res]
28         ;
29     ; make sure that all 3 Big_int's have the same size
30         ;
31     mov     eax, [esi + size_offset]
32     cmp     eax, [edi + size_offset]
33     jne     sizes_not_equal           ; op1.size_ != op2.size_
34     cmp     eax, [ebx + size_offset]
35     jne     sizes_not_equal           ; op1.size_ != res.size_
36
37     mov     ecx, eax                   ; ecx = size of Big_int's
38         ;
39     ; now, point registers to point to their respective arrays
40         ;     esi = op1.number_
41         ;     edi = op2.number_
42         ;     ebx = res.number_
43         ;
44     mov     ebx, [ebx + number_offset]
45     mov     esi, [esi + number_offset]
46     mov     edi, [edi + number_offset]
47
48     cld                                     ; clear carry flag
49     xor     edx, edx                       ; edx = 0
50         ;
51     ; addition loop
52 add_loop:
53     mov     eax, [edi+4*edx]
54     adc     eax, [esi+4*edx]
55     mov     [ebx + 4*edx], eax
56     inc     edx                             ; does not alter carry flag
57     loop   add_loop
58
59     jc     overflow
60 ok_done:
61     xor     eax, eax                       ; return value = EXIT_OK
62     jmp    done
63 overflow:
64     mov     eax, EXIT_OVERFLOW
65     jmp    done

```

```

66 sizes_not_equal:
67     mov     eax, EXIT_SIZE_MISMATCH
68 done:
69     pop     edi
70     pop     esi
71     pop     ebx
72     leave
73     ret

```

big_math.asm

Hopefully, most of this code should be straightforward to the reader by now. Lines 25 to 27 store pointers to the `Big_int` objects passed to the function into registers. Remember that references really are just pointers. Lines 31 to 35 check to make sure that the sizes of the three object's arrays are the same. (Note that the offset of `size_` is added to the pointer to access the data member.) Lines 44 to 46 adjust the registers to point to the array used by the respective objects instead of the objects themselves. (Again, the offset of the `number_` member is added to the object pointer.)

The loop in lines 52 to 57 adds the integers stored in the arrays together by adding the least significant dword first, then the next least significant dwords, *etc.* The addition must be done in this sequence for extended precision arithmetic (see Section 2.1.5). Line 59 checks for overflow, on overflow the carry flag will be set by the last addition of the most significant dword. Since the dwords in the array are stored in little endian order, the loop starts at the beginning of the array and moves forward toward the end.

Figure 7.11 shows a short example using the `Big_int` class. Note that `Big_int` constants must be declared explicitly as on line 16. This is necessary for two reasons. First, there is no conversion constructor that will convert an unsigned int to a `Big_int`. Secondly, only `Big_int`'s of the same size can be added. This makes conversion problematic since it would be difficult to know what size to convert to. A more sophisticated implementation of the class would allow any size to be added to any other size. The author did not wish to over complicate this example by implementing this here. (However, the reader is encouraged to do this.)

7.2.5 Inheritance and Polymorphism

Inheritance allows one class to inherit the data and methods of another. For example, consider the code in Figure 7.12. It shows two classes, A and B, where class B inherits from A. The output of the program is:

```

Size of a: 4 Offset of ad: 0
Size of b: 8 Offset of ad: 0 Offset of bd: 4
A::m()
A::m()

```

```
1 #include "big_int.hpp"
2 #include <iostream>
3 using namespace std;
4
5 int main()
6 {
7     try {
8         Big_int b(5,"800000000000a00b");
9         Big_int a(5,"8000000000010230");
10        Big_int c = a + b;
11        cout << a << " + " << b << " = " << c << endl;
12        for( int i=0; i < 2; i++ ) {
13            c = c + a;
14            cout << "c = " << c << endl;
15        }
16        cout << "c-1 = " << c - Big_int(5,1) << endl;
17        Big_int d(5, "12345678");
18        cout << "d = " << d << endl;
19        cout << "c == d " << (c == d) << endl;
20        cout << "c > d " << (c > d) << endl;
21    }
22    catch( const char * str ) {
23        cerr << "Caught: " << str << endl;
24    }
25    catch( Big_int :: Overflow ) {
26        cerr << "Overflow" << endl;
27    }
28    catch( Big_int :: Size_mismatch ) {
29        cerr << "Size mismatch" << endl;
30    }
31    return 0;
32 }
```

Figure 7.11: Simple Use of Big_int

```
1 #include <cstdint>
2 #include <iostream>
3 using namespace std;
4
5 class A {
6 public:
7     void __cdecl m() { cout << "A::m()" << endl; }
8     int ad;
9 };
10
11 class B : public A {
12 public:
13     void __cdecl m() { cout << "B::m()" << endl; }
14     int bd;
15 };
16
17 void f( A * p )
18 {
19     p->ad = 5;
20     p->m();
21 }
22
23 int main()
24 {
25     A a;
26     B b;
27     cout << "Size of a: " << sizeof(a)
28         << " Offset of ad: " << offsetof(A,ad) << endl;
29     cout << "Size of b: " << sizeof(b)
30         << " Offset of ad: " << offsetof(B,ad)
31         << " Offset of bd: " << offsetof(B,bd) << endl;
32     f(&a);
33     f(&b);
34     return 0;
35 }
```

Figure 7.12: Simple Inheritance

```

1  _f__FP1A:                ; mangled function name
2      push    ebp
3      mov     ebp, esp
4      mov     eax, [ebp+8]    ; eax points to object
5      mov     dword [eax], 5 ; using offset 0 for ad
6      mov     eax, [ebp+8]    ; passing address of object to A::m()
7      push    eax
8      call   _m__1A          ; mangled method name for A::m()
9      add     esp, 4
10     leave
11     ret

```

Figure 7.13: Assembly Code for Simple Inheritance

```

1  class A {
2  public:
3      virtual void __cdecl m() { cout << "A::m()" << endl; }
4      int ad;
5  };
6
7  class B : public A {
8  public:
9      virtual void __cdecl m() { cout << "B::m()" << endl; }
10     int bd;
11 };

```

Figure 7.14: Polymorphic Inheritance

Notice that the `ad` data members of both classes (B inherits it from A) are at the same offset. This is important since the `f` function may be passed a pointer to either an A object or any object of a type derived (*i.e.*, inherited from) A. Figure 7.13 shows the (edited) asm code for the function (generated by `gcc`).

Note that in the output that A's `m` method was called for both the `a` and `b` objects. From the assembly, one can see that the call to `A::m()` is hard-coded into the function. For true object-oriented programming, the method called should depend on what type of object is passed to the function. This is known as *polymorphism*. C++ turns this feature off by default. One uses the *virtual* keyword to enable it. Figure 7.14 shows how the two classes would be changed. None of the other code needs to be changed. Polymor-

```

1  ?f@@YAXPAVA@@@Z:
2      push    ebp
3      mov     ebp, esp
4
5      mov     eax, [ebp+8]
6      mov     dword [eax+4], 5 ; p->ad = 5;
7
8      mov     ecx, [ebp + 8] ; ecx = p
9      mov     edx, [ecx] ; edx = pointer to vtable
10     mov     eax, [ebp + 8] ; eax = p
11     push    eax ; push "this" pointer
12     call   dword [edx] ; call first function in vtable
13     add     esp, 4 ; clean up stack
14
15     pop     ebp
16     ret

```

Figure 7.15: Assembly Code for `f()` Function

phism can be implemented many ways. Unfortunately, *gcc*'s implementation is in transition at the time of this writing and is becoming significantly more complicated than its initial implementation. In the interest of simplifying this discussion, the author will only cover the implementation of polymorphism which the Windows based, Microsoft and Borland compilers use. This implementation has not changed in many years and probably will not change in the foreseeable future.

With these changes, the output of the program changes:

```

Size of a: 8 Offset of ad: 4
Size of b: 12 Offset of ad: 4 Offset of bd: 8
A::m()
B::m()

```

Now the second call to `f` calls the `B::m()` method because it is passed a `B` object. This is not the only change however. The size of an `A` is now 8 (and `B` is 12). Also, the offset of `ad` is 4, not 0. What is at offset 0? The answer to these questions are related to how polymorphism is implemented.

A C++ class that has any virtual methods is given an extra hidden field that is a pointer to an array of method pointers⁹. This table is often called the *vtable*. For the `A` and `B` classes this pointer is stored at offset 0. The

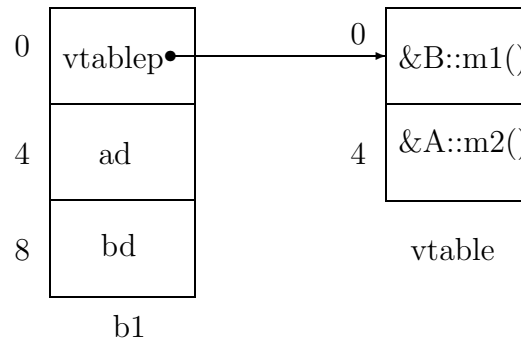
⁹For classes without virtual methods C++ compilers always make the class compatible with the a normal C struct with the same data members.

```

1  class A {
2  public:
3      virtual void __cdecl m1() { cout << "A::m1()" << endl; }
4      virtual void __cdecl m2() { cout << "A::m2()" << endl; }
5      int ad;
6  };
7
8  class B : public A { // B inherits A's m2()
9  public:
10     virtual void __cdecl m1() { cout << "B::m1()" << endl; }
11     int bd;
12 };
13 /* prints the vtable of given object */
14 void print_vtable ( A * pa )
15 {
16     // p sees pa as an array of dwords
17     unsigned * p = reinterpret_cast<unsigned *>(pa);
18     // vt sees vtable as an array of pointers
19     void ** vt = reinterpret_cast<void **>(p[0]);
20     cout << hex << "vtable address = " << vt << endl;
21     for ( int i=0; i < 2; i++ )
22         cout << "dword " << i << ": " << vt[i] << endl;
23
24     // call virtual functions in EXTREMELY non-portable way!
25     void (*m1func_pointer)(A *); // function pointer variable
26     m1func_pointer = reinterpret_cast<void (*)(A*)>(vt[0]);
27     m1func_pointer(pa); // call method m1 via function pointer
28
29     void (*m2func_pointer)(A *); // function pointer variable
30     m2func_pointer = reinterpret_cast<void (*)(A*)>(vt[1]);
31     m2func_pointer(pa); // call method m2 via function pointer
32 }
33
34 int main()
35 {
36     A a; B b1; B b2;
37     cout << "a: " << endl; print_vtable (&a);
38     cout << "b1: " << endl; print_vtable (&b);
39     cout << "b2: " << endl; print_vtable (&b2);
40     return 0;
41 }

```

Figure 7.16: More complicated example

Figure 7.17: Internal representation of `b1`

Windows compilers always puts this pointer at the beginning of the class at the top of the inheritance tree. Looking at the assembly code (Figure 7.15) generated for function `f` (from Figure 7.12) for the virtual method version of the program, one can see that the call to method `m` is not to a label. Line 9 finds the address of the vtable from the object. The address of the object is pushed on the stack in line 11. Line 12 calls the virtual method by branching to the first address in the vtable¹⁰. This call does not use a label, it branches to the code address pointed to by `EDX`. This type of call is an example of *late binding*. Late binding delays the decision of which method to call until the code is running. This allows the code to call the appropriate method for the object. The normal case (Figure 7.13) hard-codes a call to a certain method and is called *early binding* (since here the method is bound early, at compile time).

The attentive reader will be wondering why the class methods in Figure 7.14 are explicitly declared to use the C calling convention by using the `_cdecl` keyword. By default, Microsoft uses a different calling convention for C++ class methods than the standard C convention. It passes the pointer to the object acted on by the method in the `ECX` register instead of using the stack. The stack is still used for the other explicit parameters of the method. The `_cdecl` modifier tells it to use the standard C calling convention. Borland C++ uses the C calling convention by default.

Next let's look at a slightly more complicated example (Figure 7.16). In it the classes `A` and `B` each have two methods: `m1` and `m2`. Remember that since class `B` does not define its own `m2` method, it inherits the `A` class's method. Figure 7.17 shows how the `b` object appears in memory. Figure 7.18 shows the output of the program. First, look at the address of the vtable for each object. The two `B` object's addresses are the same and thus, they share

¹⁰Of course, this value is already in the `ECX` register. It was put there in line 8 and line 10 could be removed and the next line changed to push `ECX`. The code is not very efficient because it was generated without compiler optimizations turned on.

```

a:
vtable address = 004120E8
dword 0: 00401320
dword 1: 00401350
A::m1()
A::m2()
b1:
vtable address = 004120F0
dword 0: 004013A0
dword 1: 00401350
B::m1()
A::m2()
b2:
vtable address = 004120F0
dword 0: 004013A0
dword 1: 00401350
B::m1()
A::m2()

```

Figure 7.18: Output of program in Figure 7.16

the same vtable. A vtable is a property of the class not an object (like a `static` data member). Next, look at the addresses in the vttables. From looking at assembly output, one can determine that the `m1` method pointer is at offset 0 (or dword 0) and `m2` is at offset 4 (dword 1). The `m2` method pointers are the same for the A and B class vttables because class B inherits the `m2` method from the A class.

Lines 25 to 32 show how one could call a virtual function by reading its address out of the vtable for the object¹¹. The method address is stored into a C-type function pointer with an explicit *this* pointer. From the output in Figure 7.18, one can see that it does work. However, please do *not* write code like this! This is only used to illustrate how the virtual methods use the vtable.

There are some practical lessons to learn from this. One important fact is that one would have to be very careful when reading and writing class variables to a binary file. One can not just use a binary read or write on the entire object as this would read or write out the vtable pointer to the file! This is a pointer to where the vtable resides in the program's memory and will vary from program to program. This same problem can occur in C with structs, but in C, structs only have pointers in them if the programmer explicitly

¹¹Remember this code only works with the MS and Borland compilers, not *gcc*.

puts them in. There are no obvious pointers defined in either the A or B classes.

Again, it is important to realize that different compilers implement virtual methods differently. In Windows, COM (Component Object Model) class objects use vtables to implement COM interfaces¹². Only compilers that implement virtual method vtables as Microsoft does can create COM classes. This is why Borland uses the same implementation as Microsoft and one of the reasons why *gcc* can not be used to create COM classes.

The code for the virtual method looks exactly like a non-virtual one. Only the code that calls it is different. If the compiler can be absolutely sure of what virtual method will be called, it can ignore the vtable and call the method directly (*e.g.*, use early binding).

7.2.6 Other C++ features

The workings of other C++ features (*e.g.*, RunTime Type Information, and multiple inheritance) are beyond the scope of this text. If the reader wishes to go further, a good starting point is *The Annotated C++ Reference Manual* by Ellis and Stroustrup and *The Design and Evolution of C++* by Stroustrup.

¹²COM classes also use the `__stdcall` calling convention, not the standard C one.

Appendix A

80x86 Instructions

A.1 Non-floating Point Instructions

This section lists and describes the actions and formats of the non-floating point instructions of the Intel 80x86 CPU family.

The formats use the following abbreviations:

R	general register
R8	8-bit register
R16	16-bit register
R32	32-bit register
SR	segment register
M	memory
M8	byte
M16	word
M32	double word
I	immediate value

These can be combined for the multiple operand instructions. For example, the format R, R means that the instruction takes two register operands. Many of the two operand instructions allow the same operands. The abbreviation $O2$ is used to represent these operands: $R, R, R, M, R, I, M, R, M, I$. If a 8-bit register or memory can be used for an operand, the abbreviation, $R/M8$ is used.

The table also shows how various bits of the FLAGS register are affected by each instruction. If the column is blank, the corresponding bit is not affected at all. If the bit is always changed to a particular value, a 1 or 0 is shown in the column. If the bit is changed to a value that depends on the operands of the instruction, a C is placed in the column. Finally, if the bit is modified in some undefined way a $?$ appears in the column. Because the

only instructions that change the direction flag are CLD and STD, it is not listed under the FLAGS columns.

Name	Description	Formats	Flags					
			O	S	Z	A	P	C
ADC	Add with Carry	O2	C	C	C	C	C	C
ADD	Add Integers	O2	C	C	C	C	C	C
AND	Bitwise AND	O2	0	C	C	?	C	0
CALL	Call Routine	R M I						
CBW	Convert Byte to Word							
CDQ	Convert Dword to Qword							
CLC	Clear Carry							0
CLD	Clear Direction Flag							
CMC	Complement Carry							C
CMP	Compare Integers	O2	C	C	C	C	C	C
CMPSB	Compare Bytes		C	C	C	C	C	C
CMPSW	Compare Words		C	C	C	C	C	C
CMPSD	Compare Dwords		C	C	C	C	C	C
CWD	Convert Word to Dword into DX:AX							
CWDE	Convert Word to Dword into EAX							
DEC	Decrement Integer	R M	C	C	C	C	C	
DIV	Unsigned Divide	R M	?	?	?	?	?	?
ENTER	Make stack frame	I,0						
IDIV	Signed Divide	R M	?	?	?	?	?	?
IMUL	Signed Multiply	R M R16,R/M16 R32,R/M32 R16,I R32,I R16,R/M16,I R32,R/M32,I	C	?	?	?	?	C
INC	Increment Integer	R M	C	C	C	C	C	
INT	Generate Interrupt	I						
JA	Jump Above	I						
JAE	Jump Above or Equal	I						
JB	Jump Below	I						
JBE	Jump Below or Equal	I						
JC	Jump Carry	I						
JCXZ	Jump if CX = 0	I						

Name	Description	Formats	Flags					
			O	S	Z	A	P	C
JE	Jump Equal	I						
JG	Jump Greater	I						
JGE	Jump Greater or Equal	I						
JL	Jump Less	I						
JLE	Jump Less or Equal	I						
JMP	Unconditional Jump	R M I						
JNA	Jump Not Above	I						
JNAE	Jump Not Above or Equal	I						
JNB	Jump Not Below	I						
JNBE	Jump Not Below or Equal	I						
JNC	Jump No Carry	I						
JNE	Jump Not Equal	I						
JNG	Jump Not Greater	I						
JNGE	Jump Not Greater or Equal	I						
JNL	Jump Not Less	I						
JNLE	Jump Not Less or Equal	I						
JNO	Jump No Overflow	I						
JNS	Jump No Sign	I						
JNZ	Jump Not Zero	I						
JO	Jump Overflow	I						
JPE	Jump Parity Even	I						
JPO	Jump Parity Odd	I						
JS	Jump Sign	I						
JZ	Jump Zero	I						
LAHF	Load FLAGS into AH							
LEA	Load Effective Address	R32,M						
LEAVE	Leave Stack Frame							
LODSB	Load Byte							
LODSW	Load Word							
LODSD	Load Dword							
LOOP	Loop	I						
LOOPE/LOOPZ	Loop If Equal	I						
LOOPNE/LOOPNZ	Loop If Not Equal	I						

Name	Description	Formats	Flags					
			O	S	Z	A	P	C
MOV	Move Data	O2 SR,R/M16 R/M16,SR						
MOVSB	Move Byte							
MOVSW	Move Word							
MOVSD	Move Dword							
MOVSX	Move Signed	R16,R/M8 R32,R/M8 R32,R/M16						
MOVZX	Move Unsigned	R16,R/M8 R32,R/M8 R32,R/M16						
MUL	Unsigned Multiply	R M	C	?	?	?	?	C
NEG	Negate	R M	C	C	C	C	C	C
NOP	No Operation							
NOT	1's Complement	R M						
OR	Bitwise OR	O2	0	C	C	?	C	0
POP	Pop From Stack	R/M16 R/M32						
POPA	Pop All							
POPF	Pop FLAGS		C	C	C	C	C	C
PUSH	Push to Stack	R/M16 R/M32 I						
PUSHA	Push All							
PUSHF	Push FLAGS							
RCL	Rotate Left with Carry	R/M,I R/M,CL	C					C
RCR	Rotate Right with Carry	R/M,I R/M,CL	C					C
REP	Repeat							
REPE/REPZ	Repeat If Equal							
REPNE/REPNZ	Repeat If Not Equal							
RET	Return							
ROL	Rotate Left	R/M,I R/M,CL	C					C
ROR	Rotate Right	R/M,I R/M,CL	C					C
SAHF	Copies AH into FLAGS			C	C	C	C	C

Name	Description	Formats	Flags						
			O	S	Z	A	P	C	
SAL	Shifts to Left	R/M,I R/M, CL							C
SBB	Subtract with Borrow	O2	C	C	C	C	C	C	C
SCASB	Scan for Byte		C	C	C	C	C	C	C
SCASW	Scan for Word		C	C	C	C	C	C	C
SCASD	Scan for Dword		C	C	C	C	C	C	C
SETA	Set Above	R/M8							
SETAE	Set Above or Equal	R/M8							
SETB	Set Below	R/M8							
SETBE	Set Below or Equal	R/M8							
SETC	Set Carry	R/M8							
SETE	Set Equal	R/M8							
SETG	Set Greater	R/M8							
SETGE	Set Greater or Equal	R/M8							
SETL	Set Less	R/M8							
SETLE	Set Less or Equal	R/M8							
SETNA	Set Not Above	R/M8							
SETNAE	Set Not Above or Equal	R/M8							
SETNB	Set Not Below	R/M8							
SETNBE	Set Not Below or Equal	R/M8							
SETNC	Set No Carry	R/M8							
SETNE	Set Not Equal	R/M8							
SETNG	Set Not Greater	R/M8							
SETNGE	Set Not Greater or Equal	R/M8							
SETNL	Set Not Less	R/M8							
SETNLE	Set Not LEss or Equal	R/M8							
SETNO	Set No Overflow	R/M8							
SETNS	Set No Sign	R/M8							
SETNZ	Set Not Zero	R/M8							
SETO	Set Overflow	R/M8							
SETPE	Set Parity Even	R/M8							
SETPO	Set Parity Odd	R/M8							
SETS	Set Sign	R/M8							
SETZ	Set Zero	R/M8							
SAR	Arithmetic Shift to Right	R/M,I R/M, CL							C

Name	Description	Formats	Flags					
			O	S	Z	A	P	C
SHR	Logical Shift to Right	R/M,I R/M, CL						C
SHL	Logical Shift to Left	R/M,I R/M, CL						C
STC	Set Carry							1
STD	Set Direction Flag							
STOSB	Store Btyle							
STOSW	Store Word							
STOSD	Store Dword							
SUB	Subtract	O2	C	C	C	C	C	C
TEST	Logical Compare	R/M,R R/M,I	0	C	C	?	C	0
XCHG	Exchange	R/M,R R,R/M						
XOR	Bitwise XOR	O2	0	C	C	?	C	0

A.2 Floating Point Instructions

In this section, many of the 80x86 math coprocessor instructions are described. The description section briefly describes the operation of the instruction. To save space, information about whether the instruction pops the stack is not given in the description.

The format column shows what type of operands can be used with each instruction. The following abbreviations are used:

ST n	A coprocessor register
F	Single precision number in memory
D	Double precision number in memory
E	Extended precision number in memory
I16	Integer word in memory
I32	Integer double word in memory
I64	Integer quad word in memory

Instructions requiring a Pentium Pro or better are marked with an asterisk(*).

Instruction	Description	Format
FABS	ST0 = ST0	
FADD <i>src</i>	ST0 += <i>src</i>	ST n F D
FADD <i>dest</i> , ST0	<i>dest</i> += ST0	ST n
FADDP <i>dest</i> [,ST0]	<i>dest</i> += ST0	ST n
FCHS	ST0 = -ST0	
FCOM <i>src</i>	Compare ST0 and <i>src</i>	ST n F D
FCOMP <i>src</i>	Compare ST0 and <i>src</i>	ST n F D
FCOMPP <i>src</i>	Compares ST0 and ST1	
FCOMI* <i>src</i>	Compares into FLAGS	ST n
FCOMIP* <i>src</i>	Compares into FLAGS	ST n
FDIV <i>src</i>	ST0 /= <i>src</i>	ST n F D
FDIV <i>dest</i> , ST0	<i>dest</i> /= ST0	ST n
FDIVP <i>dest</i> [,ST0]	<i>dest</i> /= ST0	ST n
FDIVR <i>src</i>	ST0 = <i>src</i> /ST0	ST n F D
FDIVR <i>dest</i> , ST0	<i>dest</i> = ST0/ <i>dest</i>	ST n
FDIVRP <i>dest</i> [,ST0]	<i>dest</i> = ST0/ <i>dest</i>	ST n
FFREE <i>dest</i>	Marks as empty	ST n
FIADD <i>src</i>	ST0 += <i>src</i>	I16 I32
FICOM <i>src</i>	Compare ST0 and <i>src</i>	I16 I32
FICOMP <i>src</i>	Compare ST0 and <i>src</i>	I16 I32
FIDIV <i>src</i>	ST0 /= <i>src</i>	I16 I32
FIDIVR <i>src</i>	ST0 = <i>src</i> /ST0	I16 I32

Instruction	Description	Format
FILD <i>src</i>	Push <i>src</i> on Stack	I16 I32 I64
FIMUL <i>src</i>	ST0 *= <i>src</i>	I16 I32
FINIT	Initialize Coprocessor	
FIST <i>dest</i>	Store ST0	I16 I32
FISTP <i>dest</i>	Store ST0	I16 I32 I64
FISUB <i>src</i>	ST0 -= <i>src</i>	I16 I32
FISUBR <i>src</i>	ST0 = <i>src</i> - ST0	I16 I32
FLD <i>src</i>	Push <i>src</i> on Stack	ST _n F D E
FLD1	Push 1.0 on Stack	
FLDCW <i>src</i>	Load Control Word Register	I16
FLDPI	Push π on Stack	
FLDZ	Push 0.0 on Stack	
FMUL <i>src</i>	ST0 *= <i>src</i>	ST _n F D
FMUL <i>dest</i> , ST0	<i>dest</i> *= ST0	ST _n
FMULP <i>dest</i> [,ST0]	<i>dest</i> *= ST0	ST _n
FRNDINT	Round ST0	
FSCALE	ST0 = ST0 $\times 2^{[ST1]}$	
FSQRT	ST0 = $\sqrt{ST0}$	
FST <i>dest</i>	Store ST0	ST _n F D
FSTP <i>dest</i>	Store ST0	ST _n F D E
FSTCW <i>dest</i>	Store Control Word Register	I16
FSTSW <i>dest</i>	Store Status Word Register	I16 AX
FSUB <i>src</i>	ST0 -= <i>src</i>	ST _n F D
FSUB <i>dest</i> , ST0	<i>dest</i> -= ST0	ST _n
FSUBP <i>dest</i> [,ST0]	<i>dest</i> -= ST0	ST _n
FSUBR <i>src</i>	ST0 = <i>src</i> - ST0	ST _n F D
FSUBR <i>dest</i> , ST0	<i>dest</i> = ST0 - <i>dest</i>	ST _n
FSUBP <i>dest</i> [,ST0]	<i>dest</i> = ST0 - <i>dest</i>	ST _n
FTST	Compare ST0 with 0.0	
FXCH <i>dest</i>	Exchange ST0 and <i>dest</i>	ST _n